

FROM ALGORITHMS TO ASTROPHYSICS: MACHINE LEARNING IN GRAVITATIONAL WAVE ASTRONOMY

NIKOLAOS STERGIOULAS

DEPARTMENT OF PHYSICS

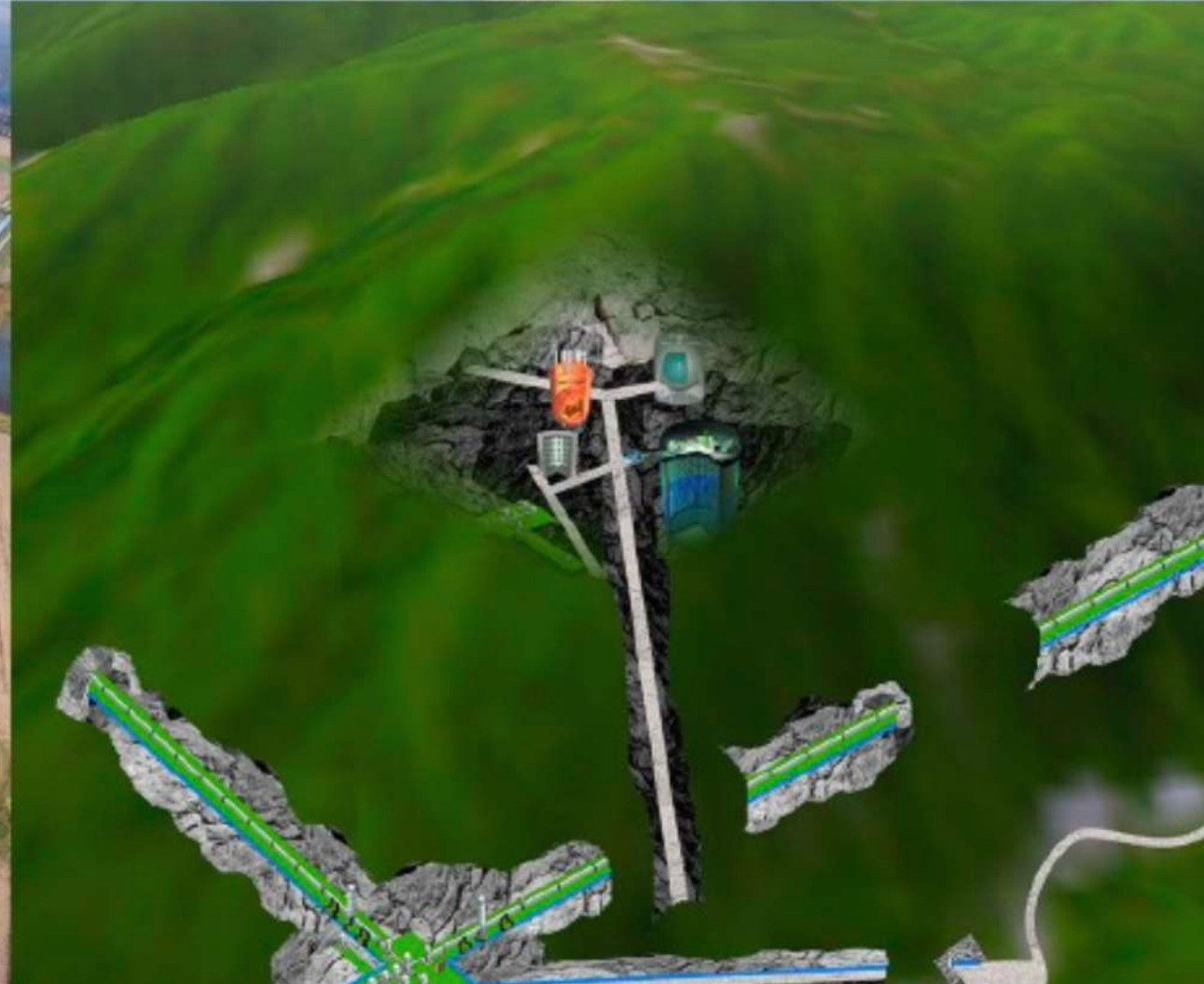
ARISTOTLE UNIVERSITY OF THESSALONIKI



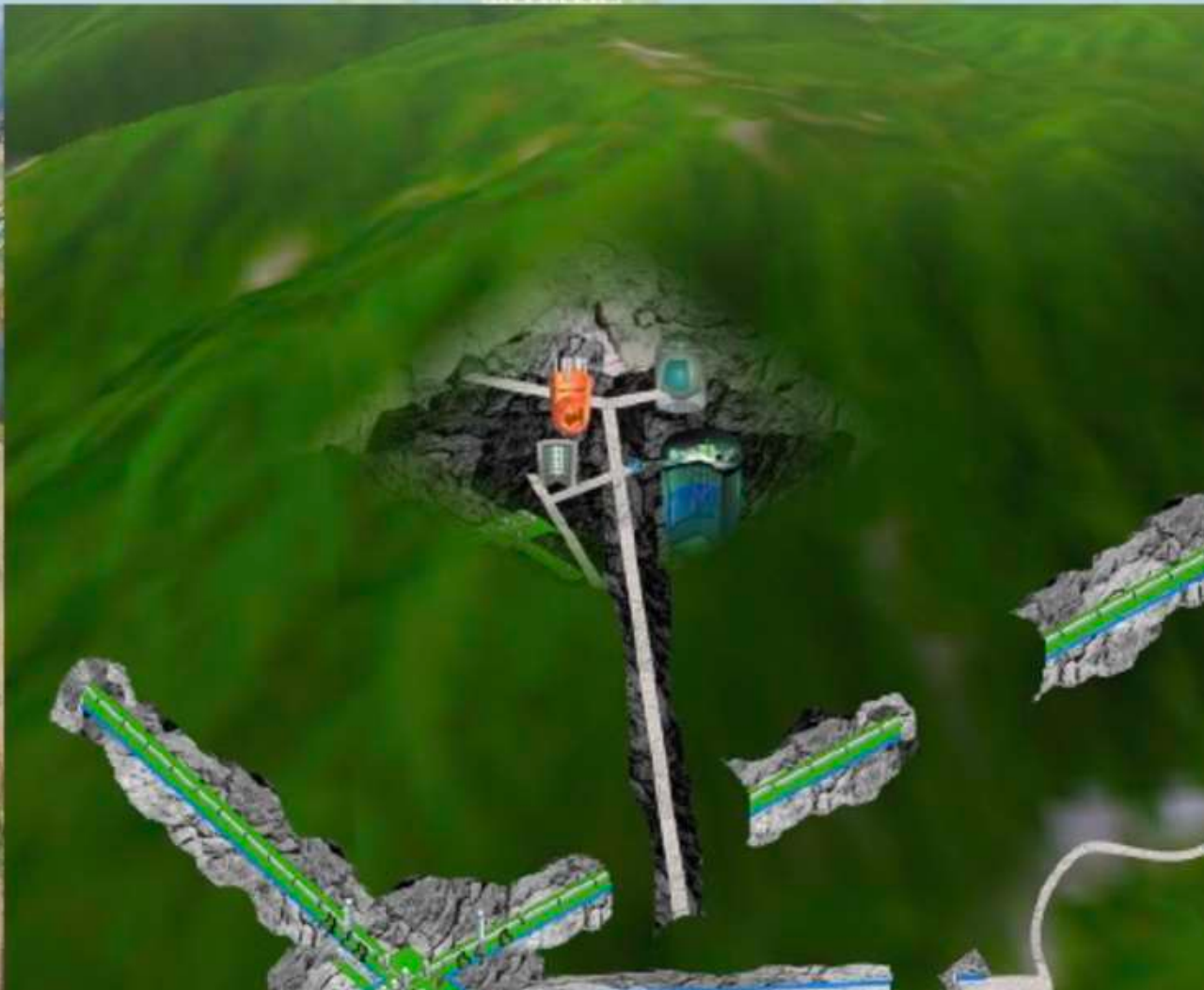
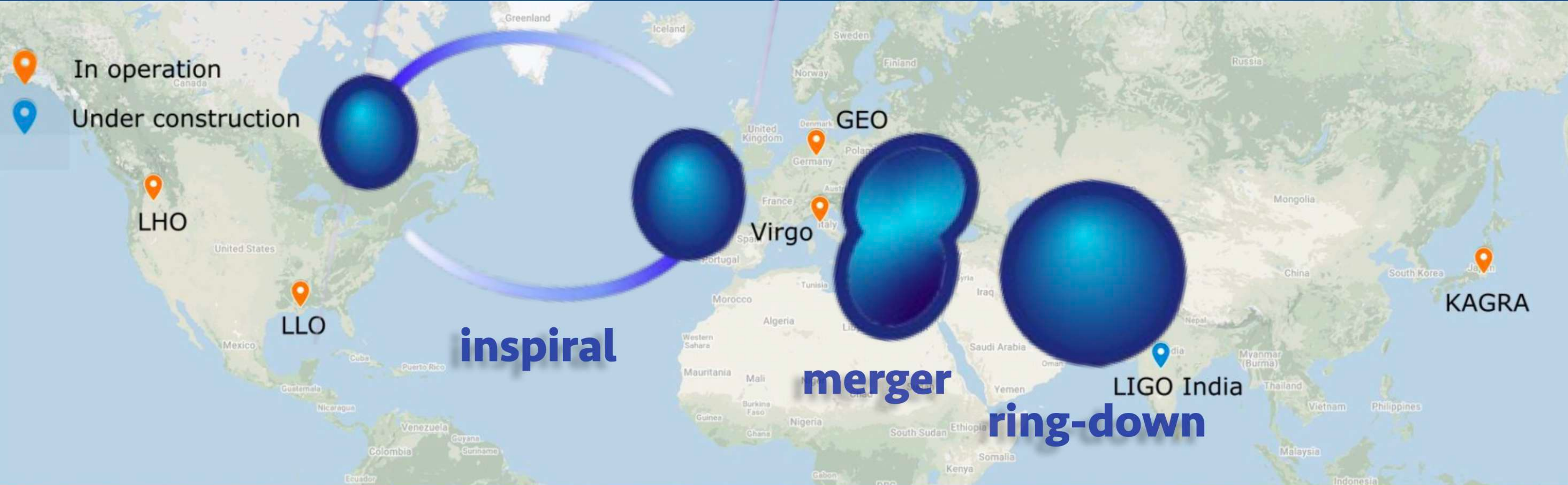
AI&GW@CZ, Prague, November 28, 2025

PART A. BINARY BLACK HOLE MERGERS

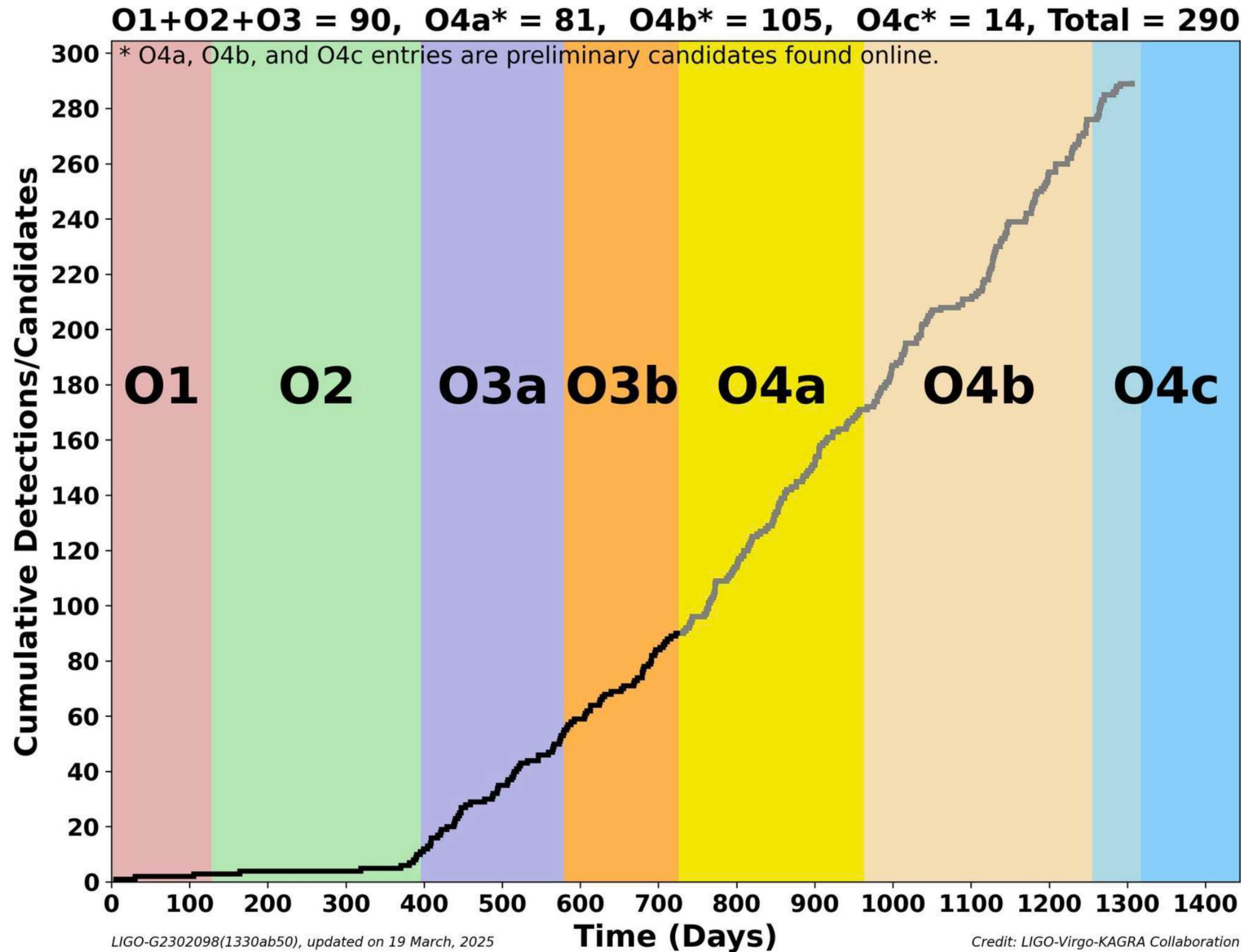
INTERNATIONAL GRAVITATIONAL-WAVE OBSERVATORY NETWORK (IGWN)



INTERNATIONAL GRAVITATIONAL-WAVE OBSERVATORY NETWORK (IGWN)



TOTAL NUMBER OF DETECTIONS BY LVK COLLABORATION IN 2015-2025



LIGO-Virgo-KAGRA (LVK):

290 published detections

+ *additional detections in O3 data by:*

AEI Hannover

IAS

AUTH (AresGW)

NEXT-GENERATION DETECTORS

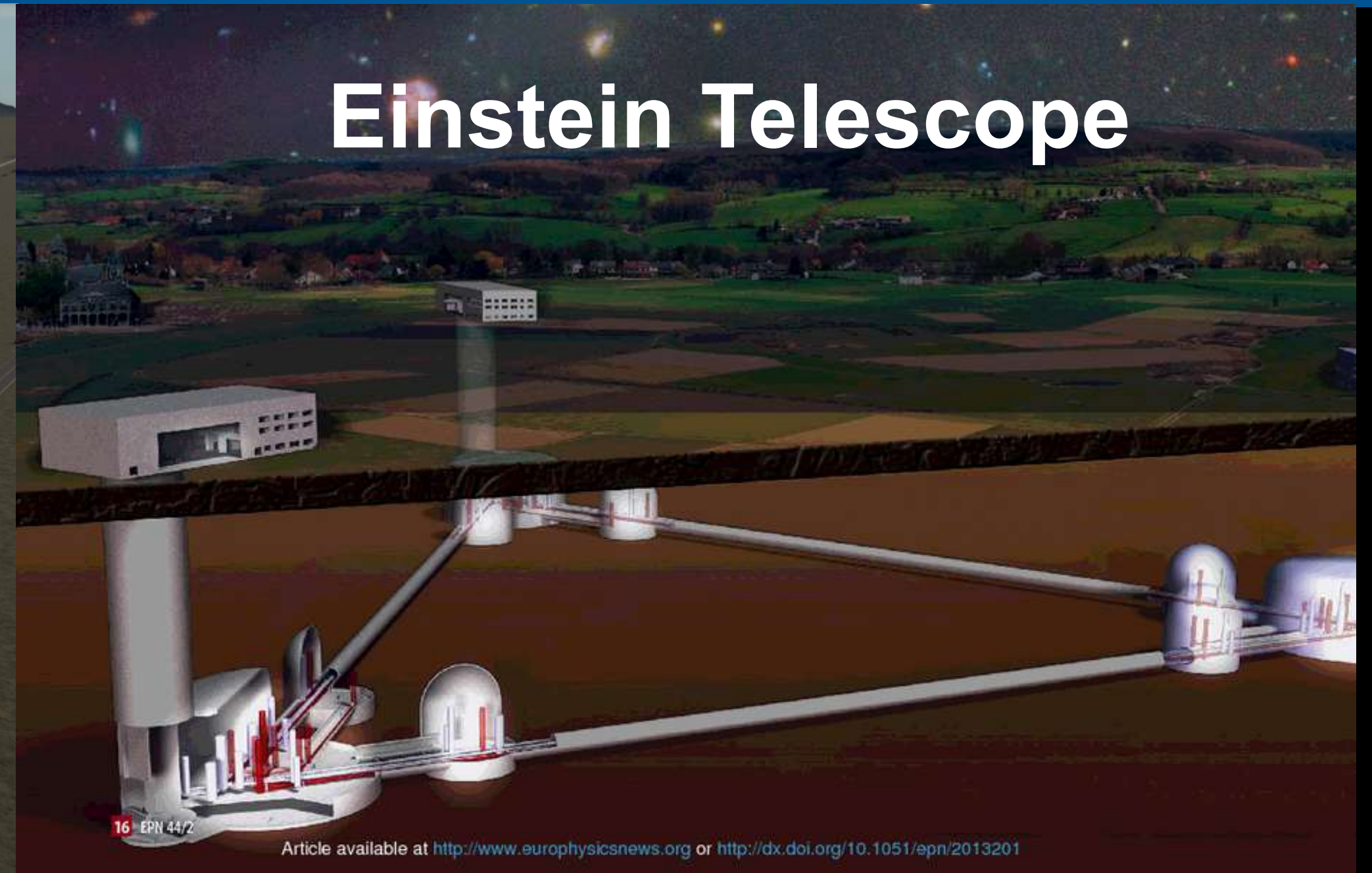
Cosmic Explorer

next-generation gravitational-wave observatories

[Join the Cosmic Explorer Consortium](#)



Einstein Telescope

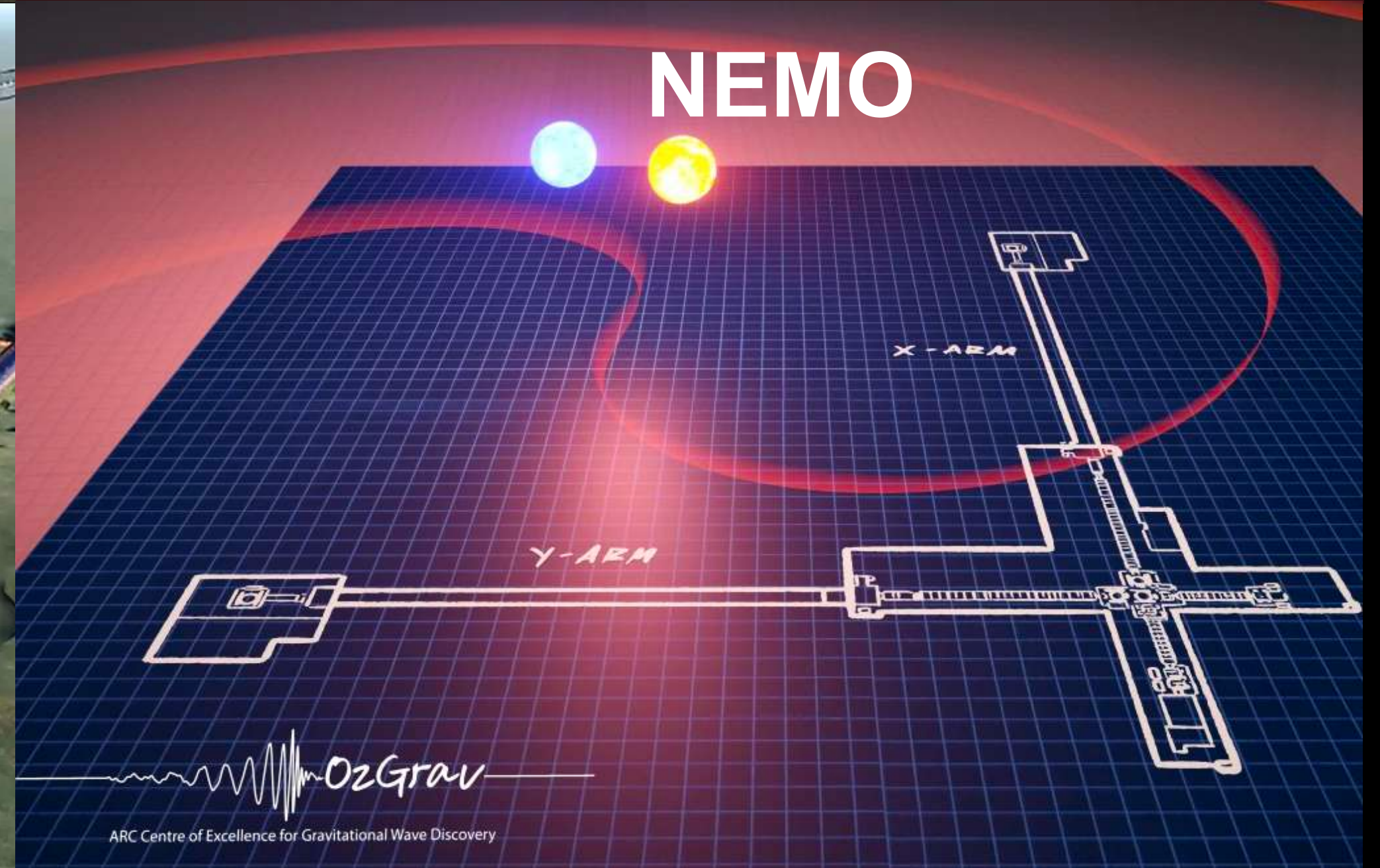


Article available at <http://www.europhysicsnews.org> or <http://dx.doi.org/10.1051/epn/2013201>

LIGO-India

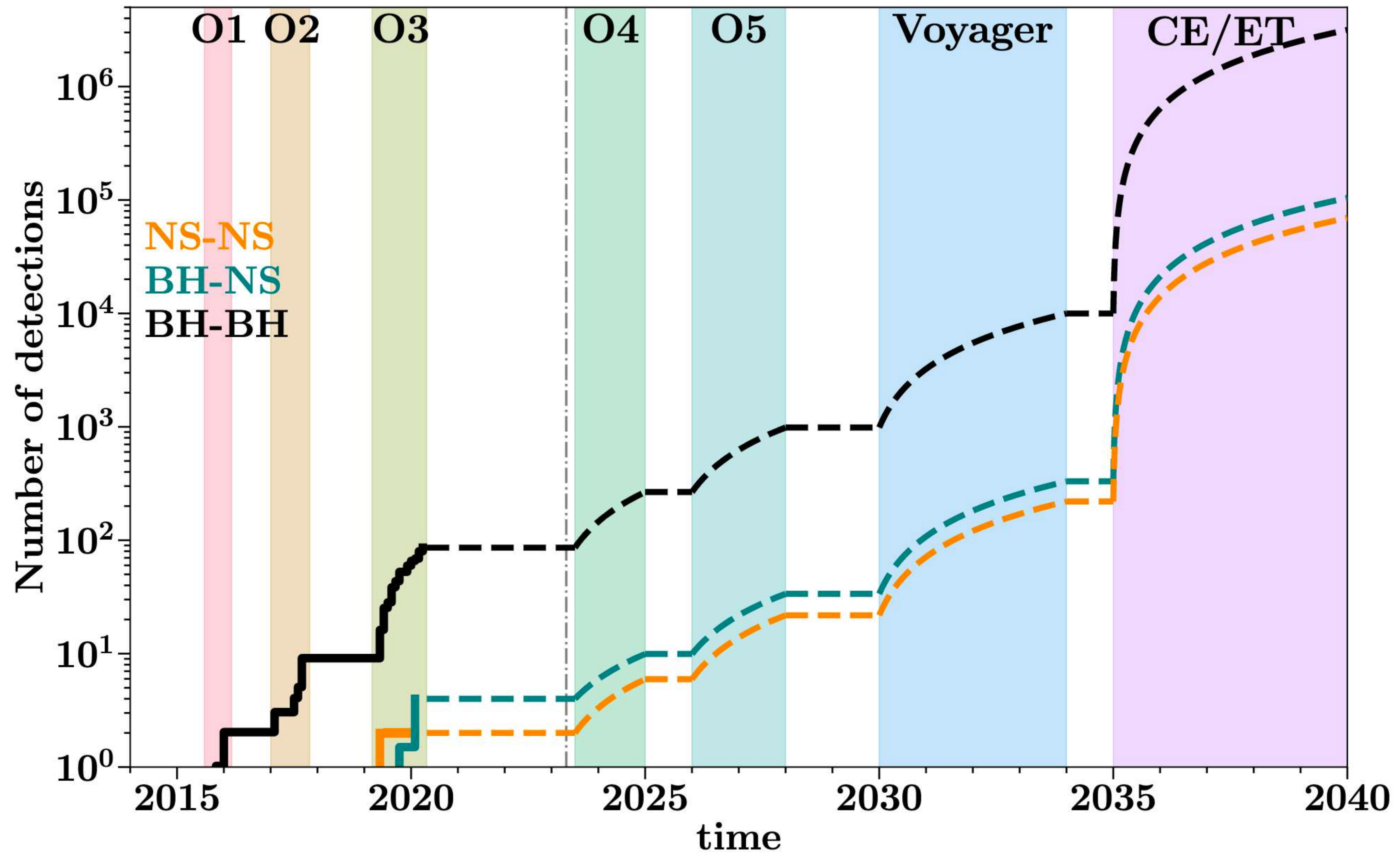


NEMO



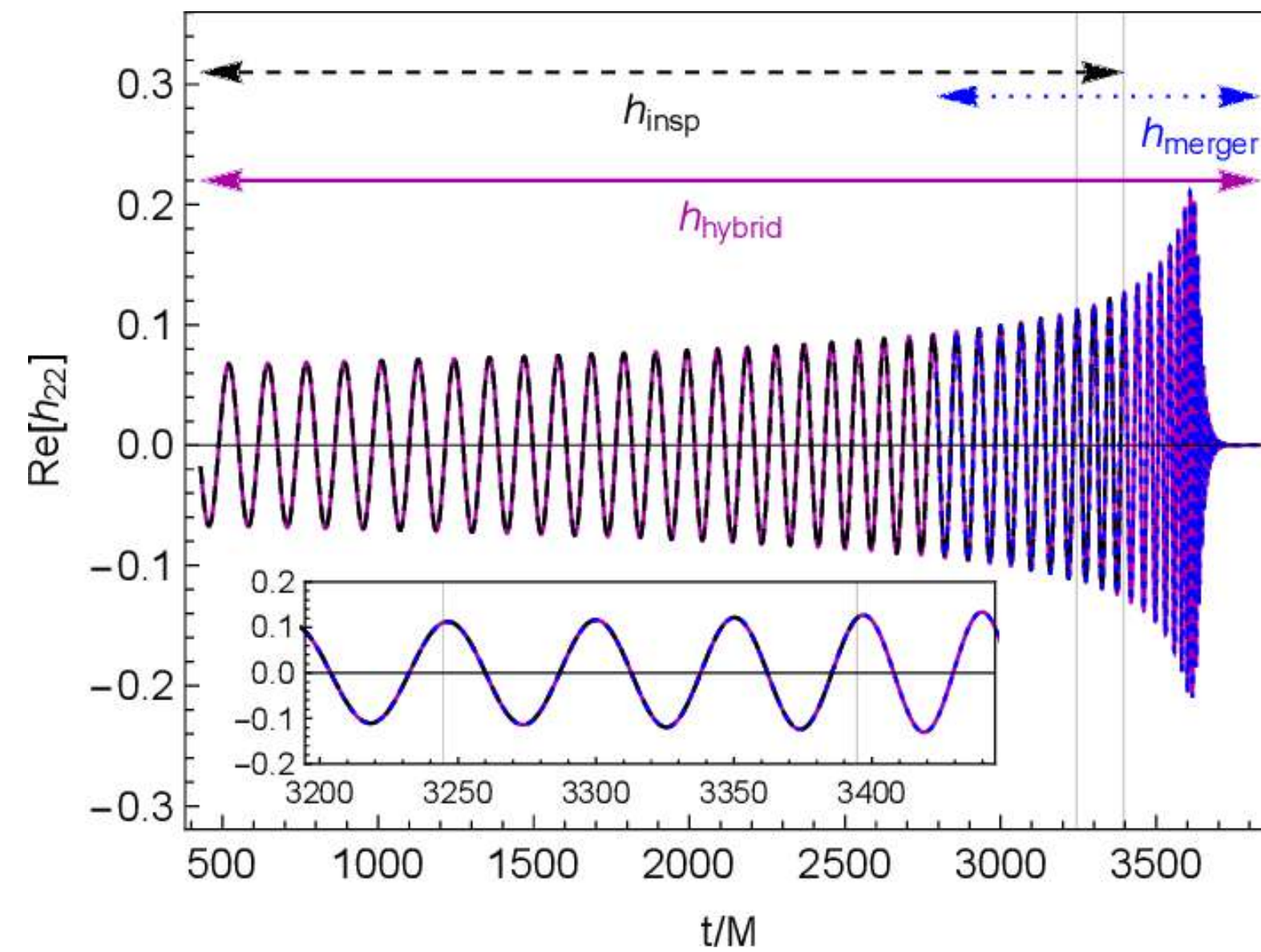
OzGrav
ARC Centre of Excellence for Gravitational Wave Discovery

EXPECTED NUMBER OF DETECTIONS

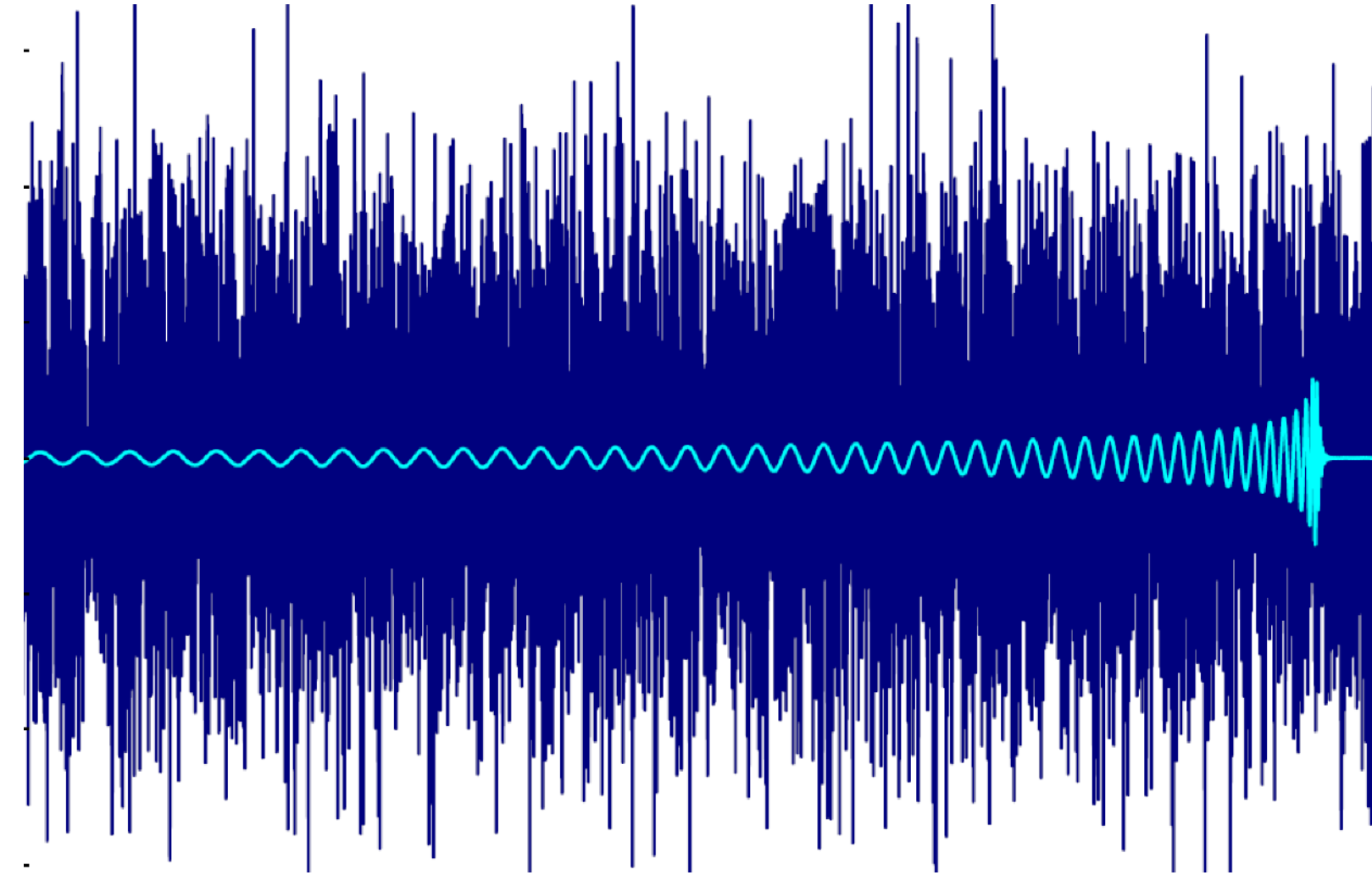


MACHINE LEARNING IN GRAVITATIONAL WAVE ASTRONOMY

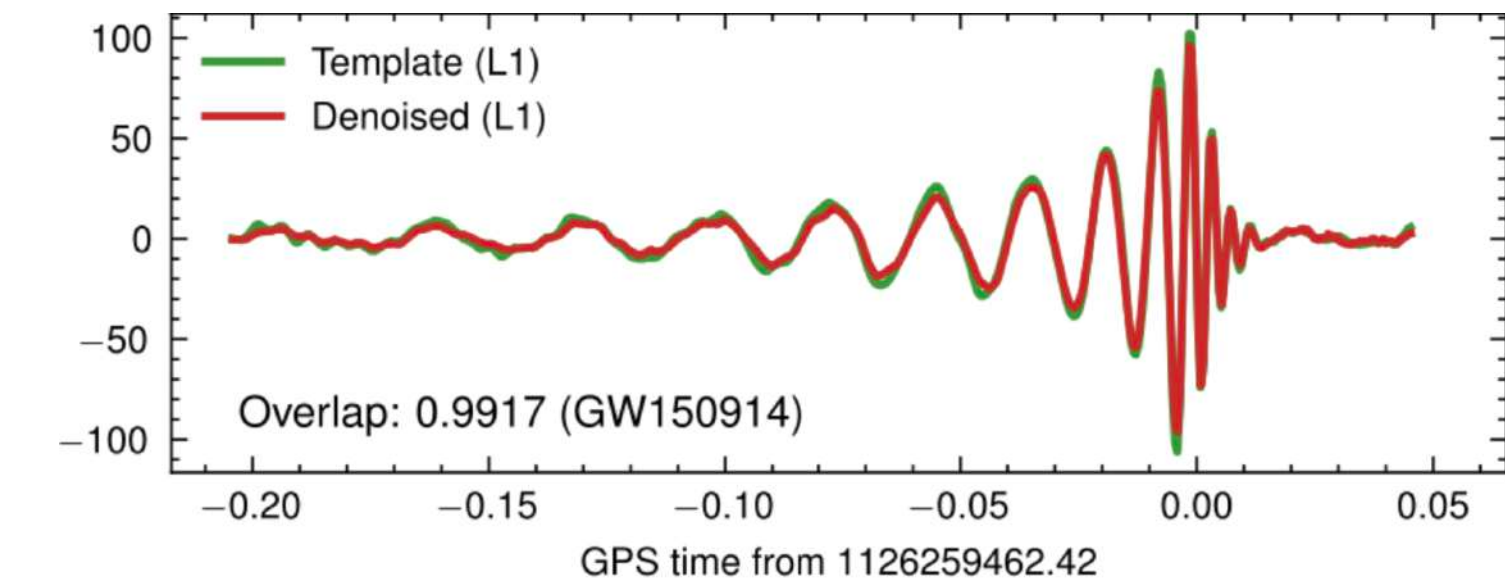
Waveform Modeling



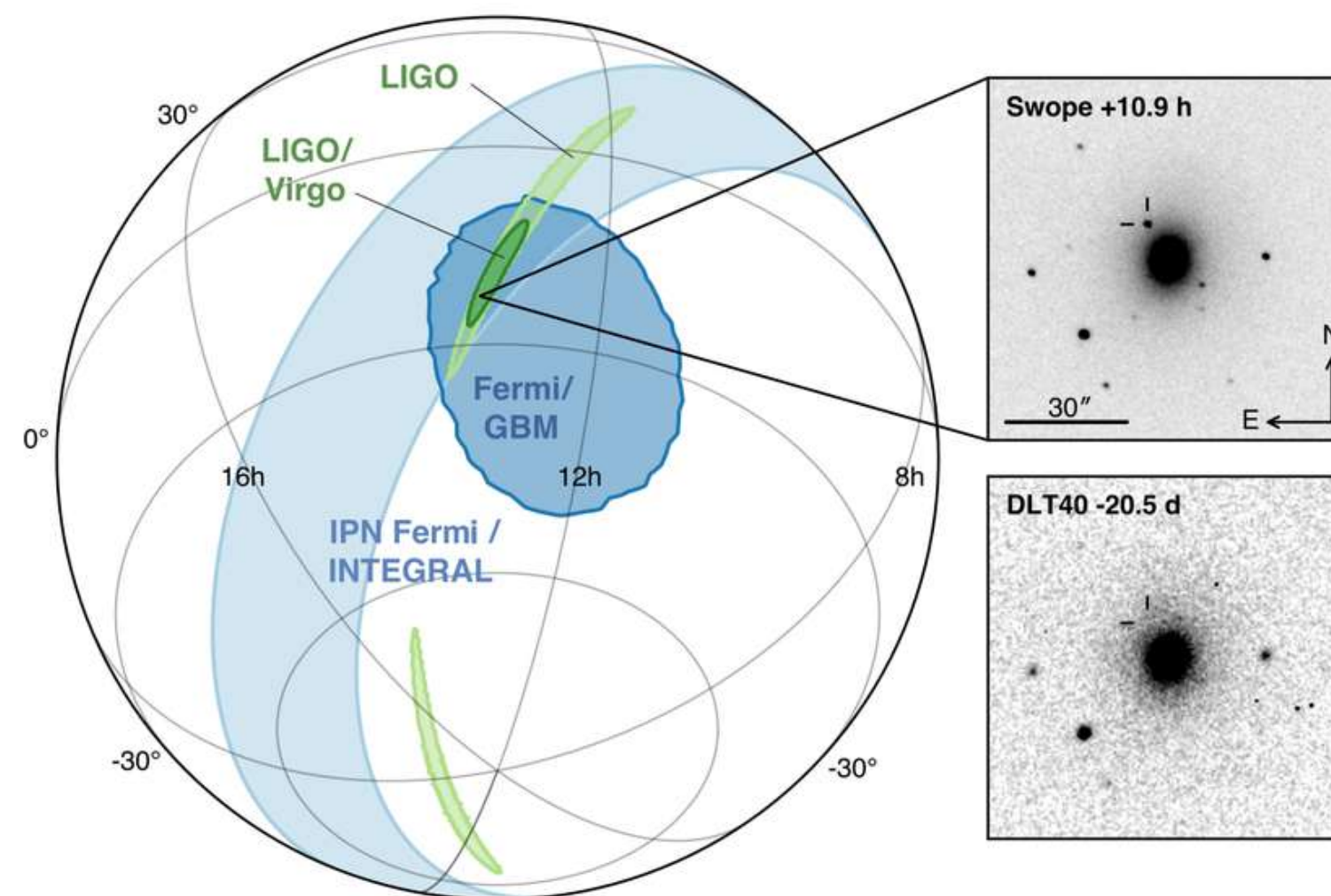
Detection



Denoising

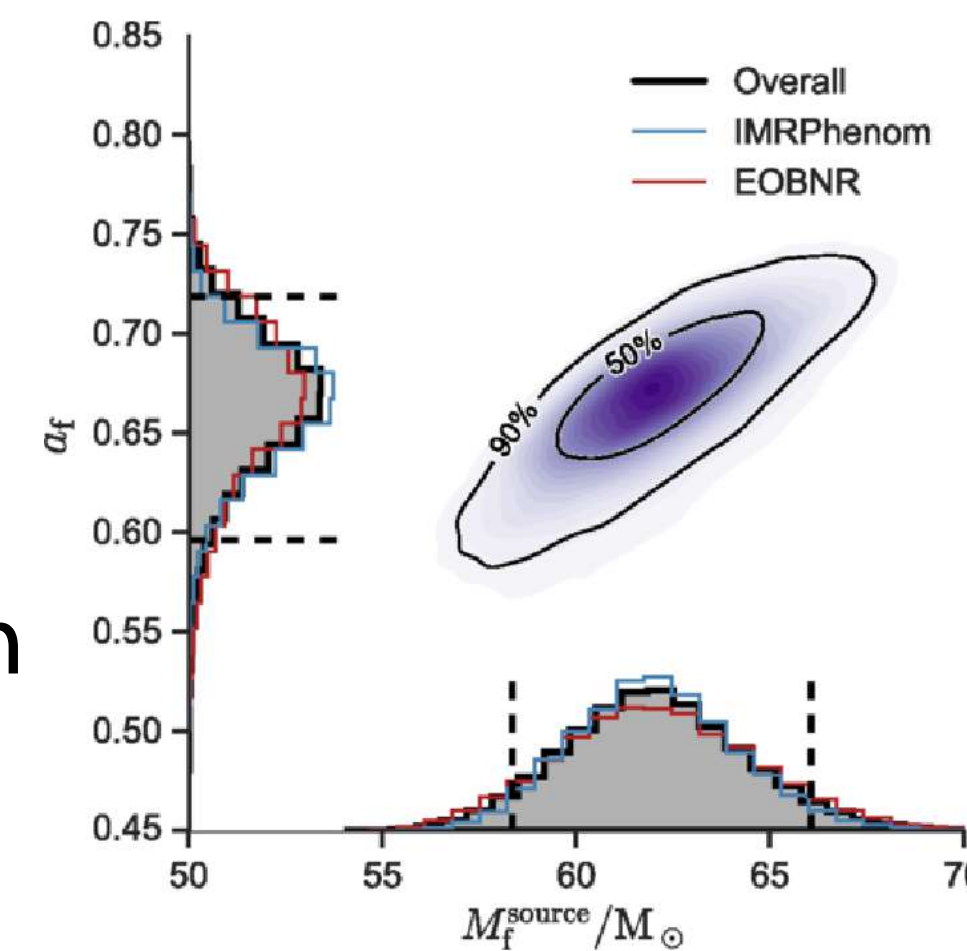


Glitch Classification

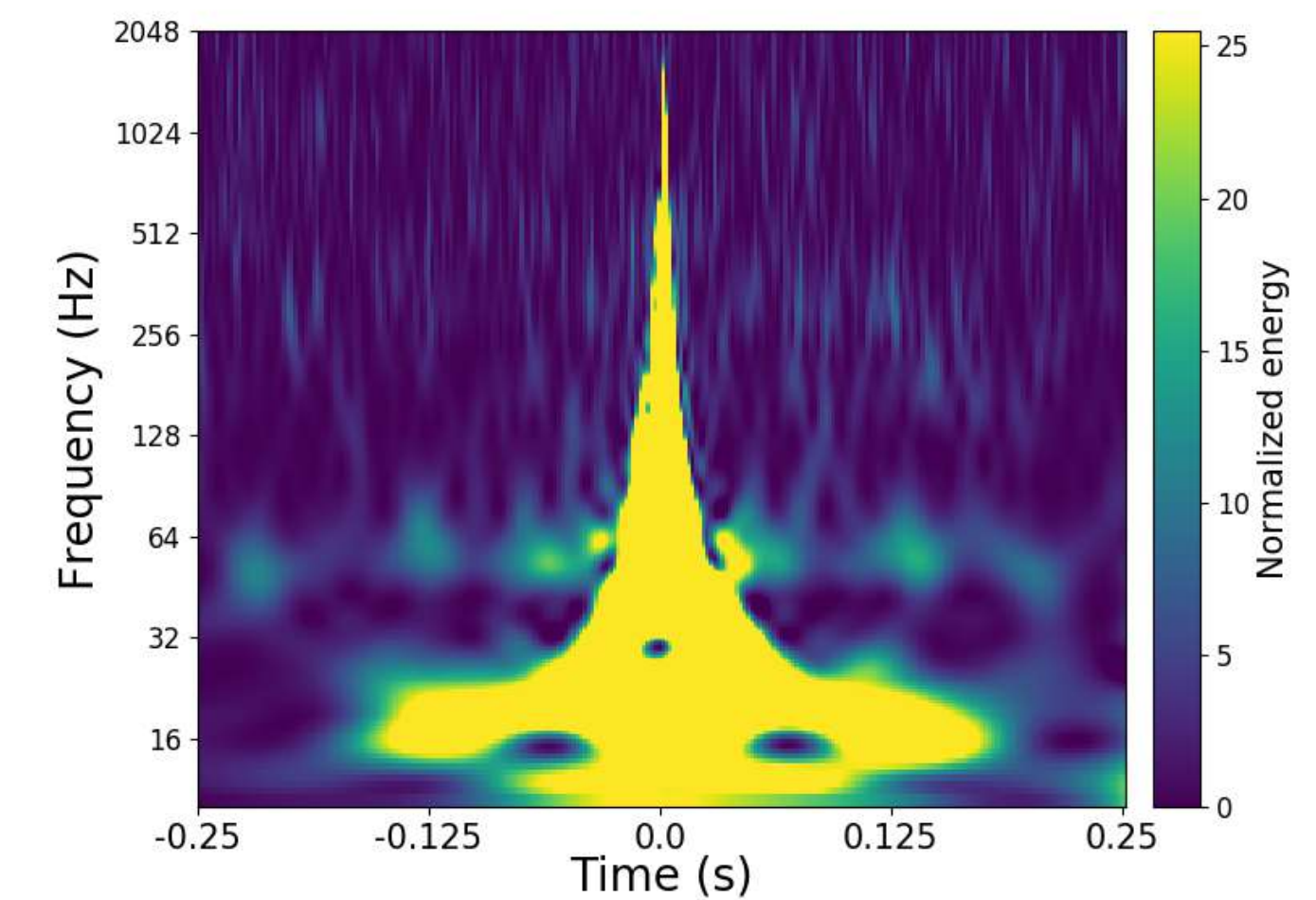


Parameter Estimation

Sky Localization

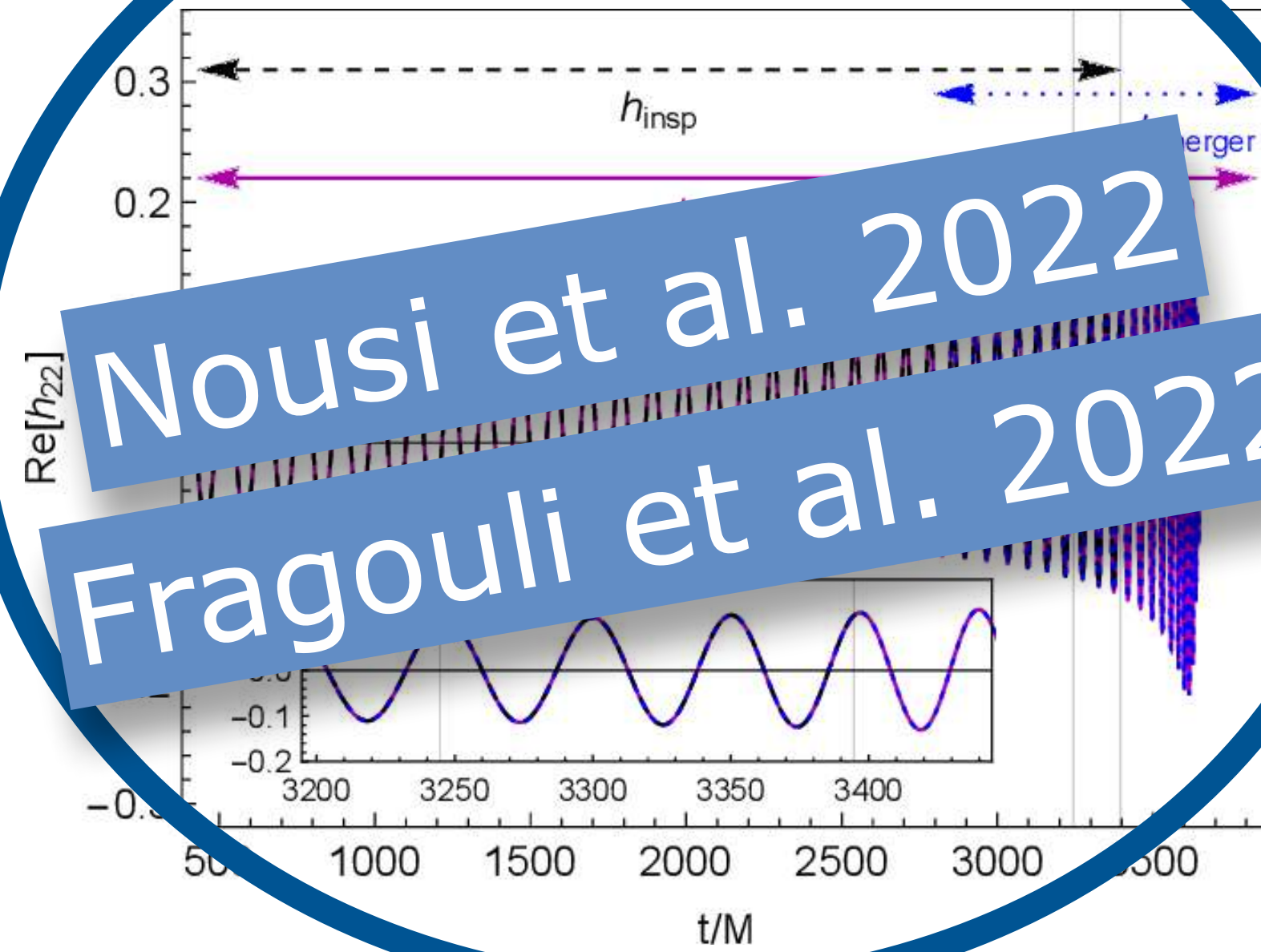


Livingston - O2a

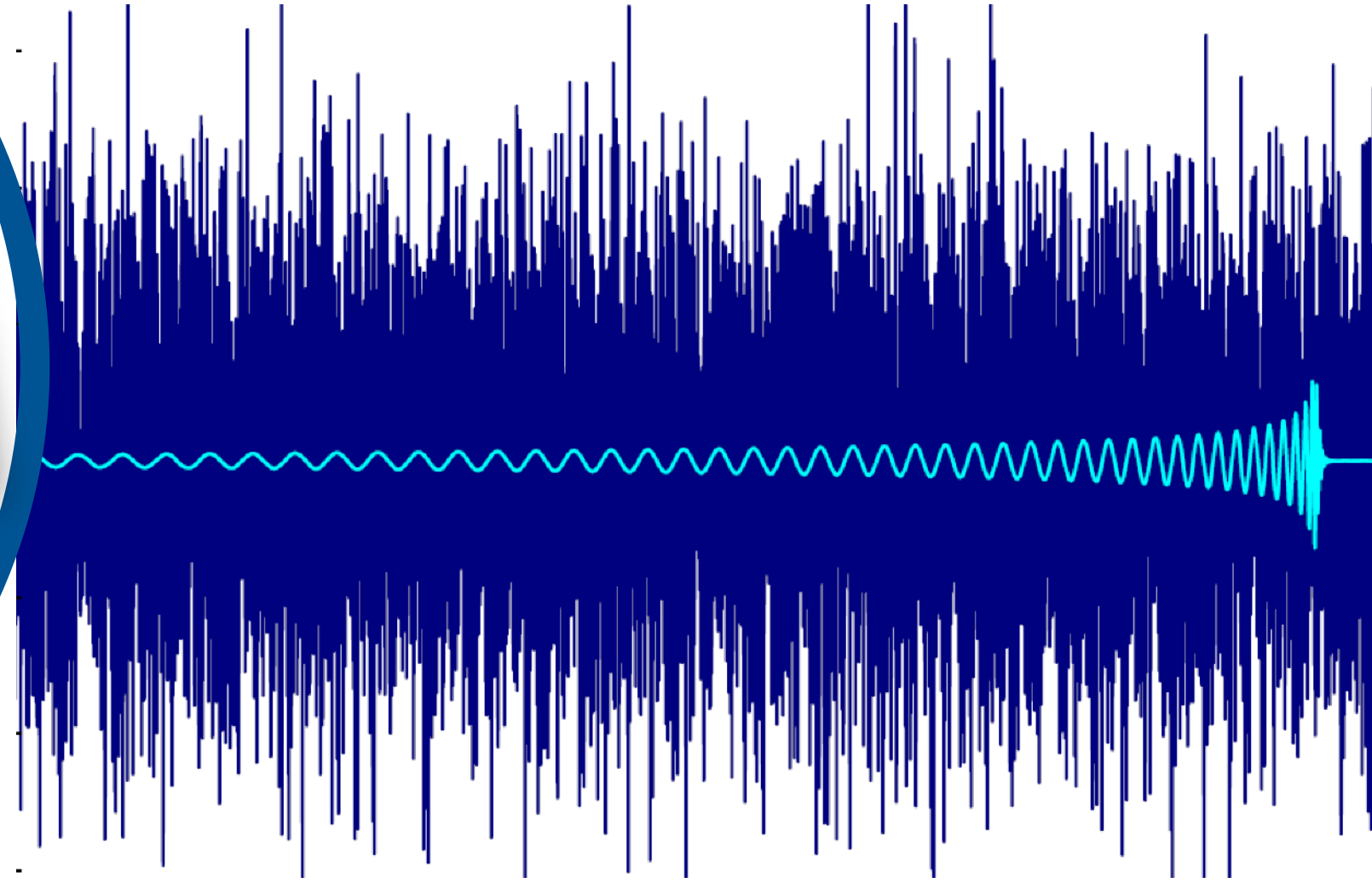


MACHINE LEARNING IN GRAVITATIONAL WAVE ASTRONOMY

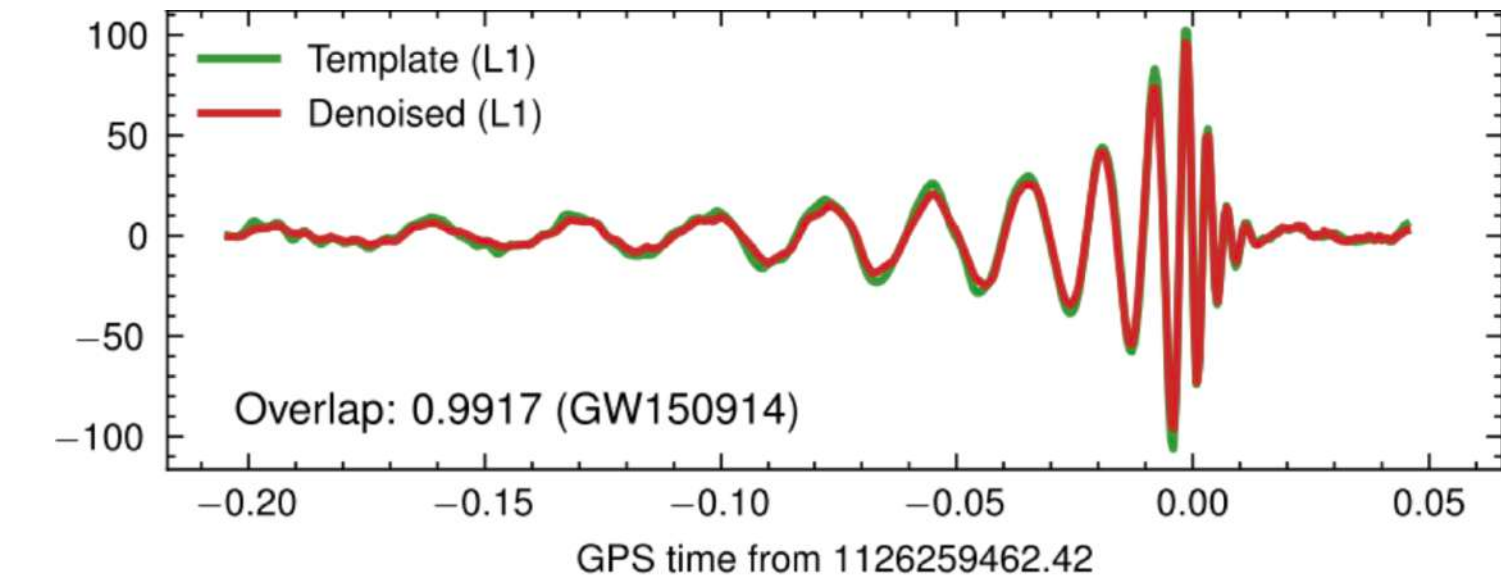
Waveform Modeling



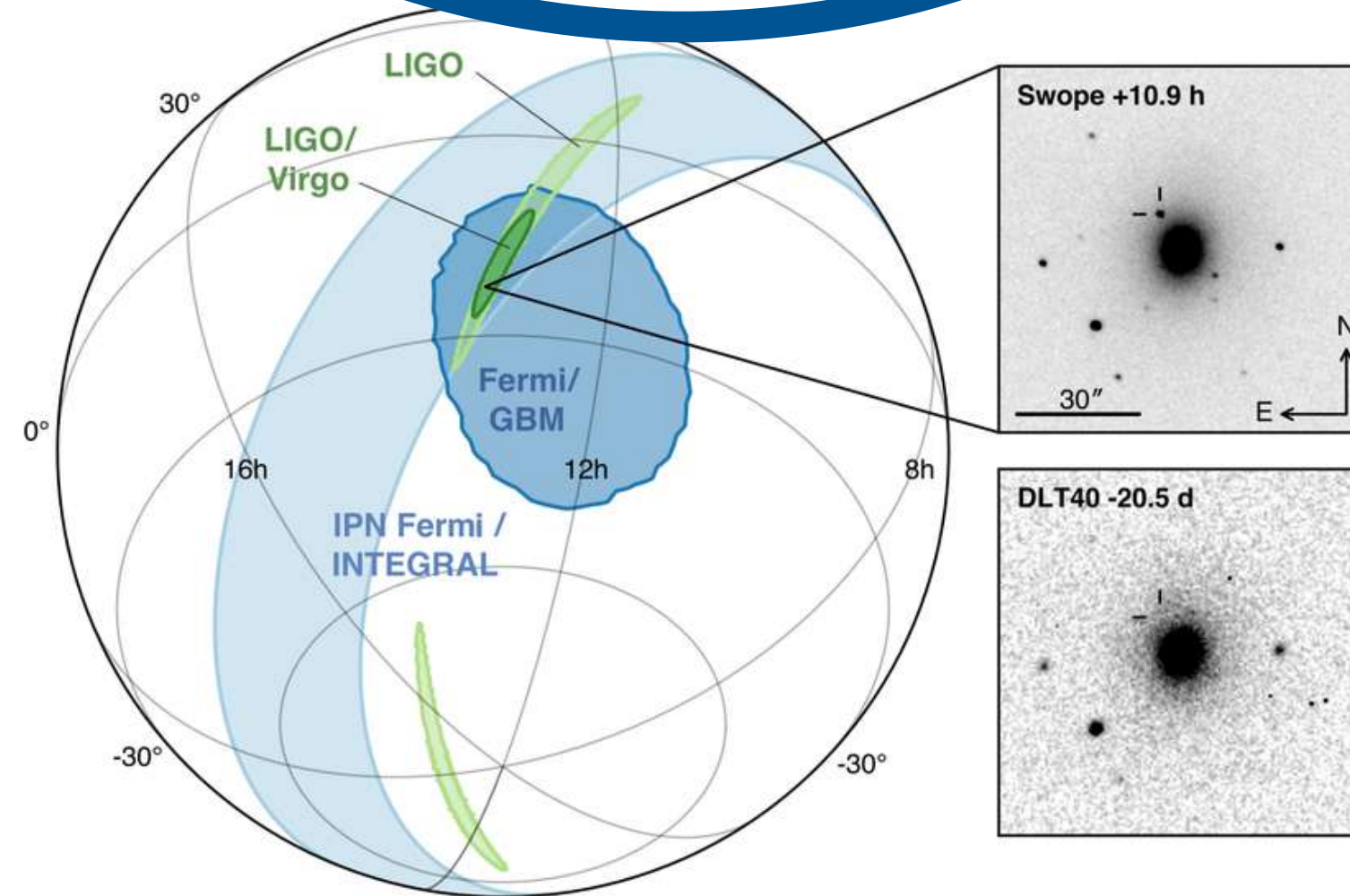
Detection



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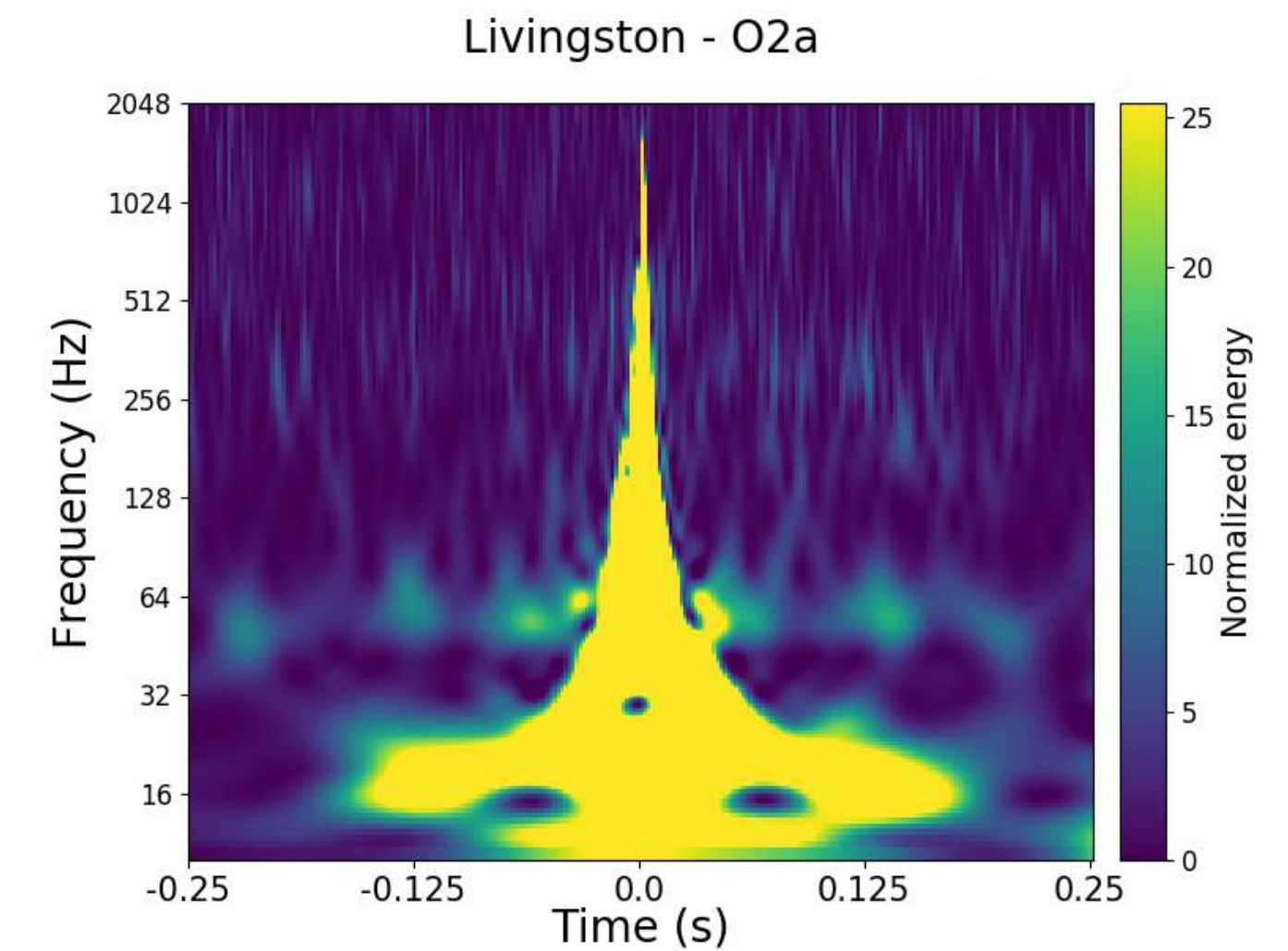
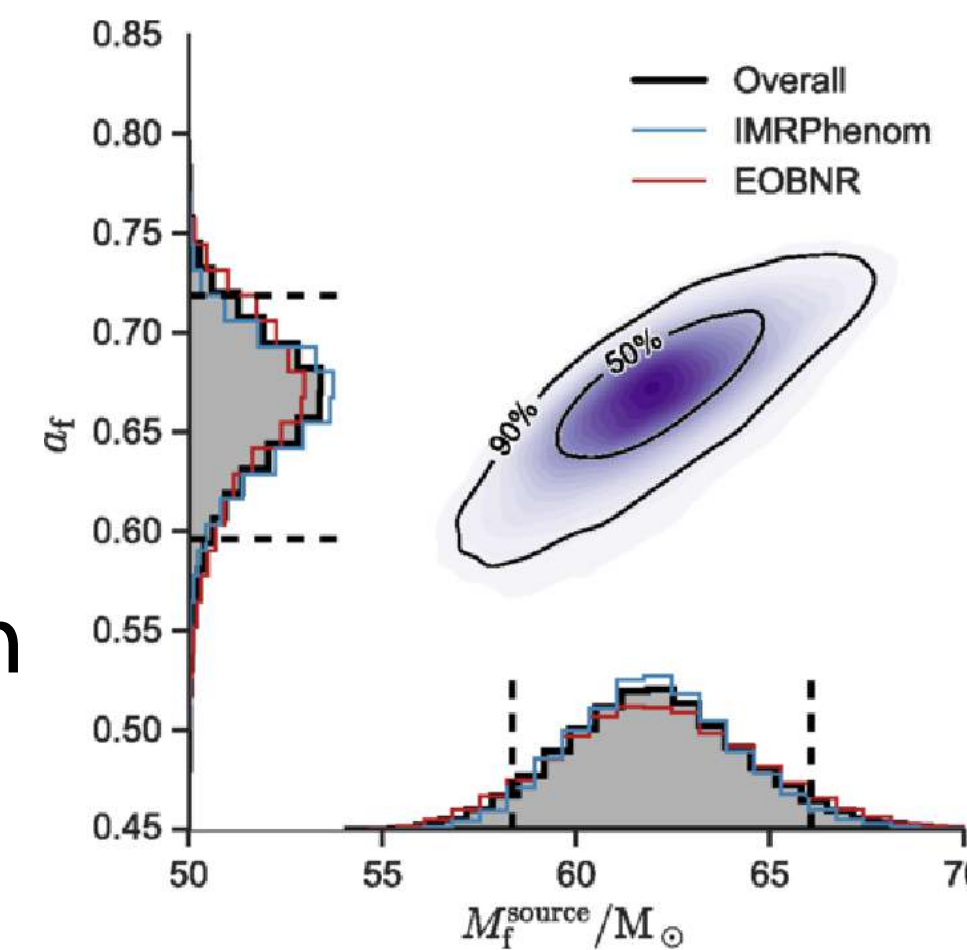


Glitch Classification



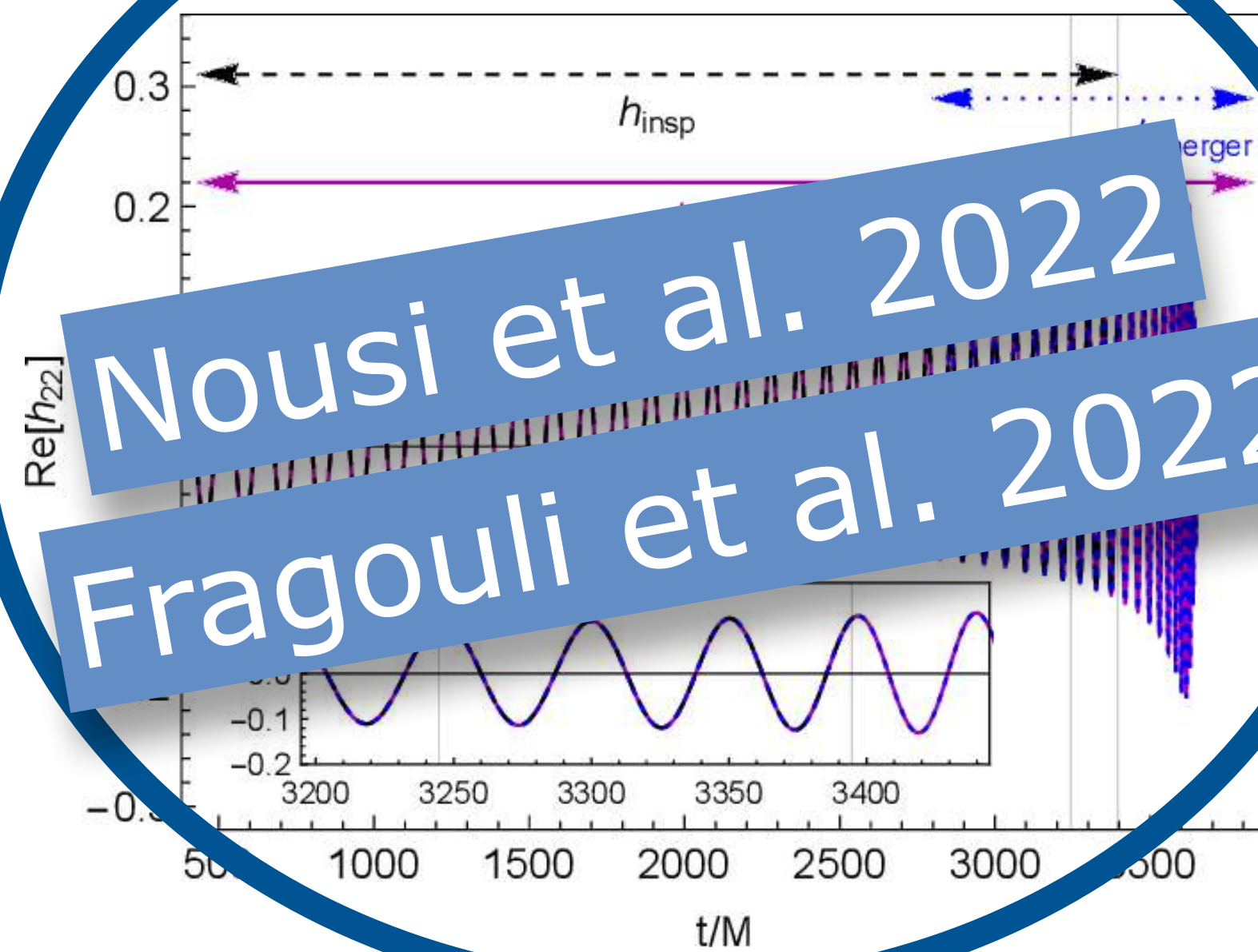
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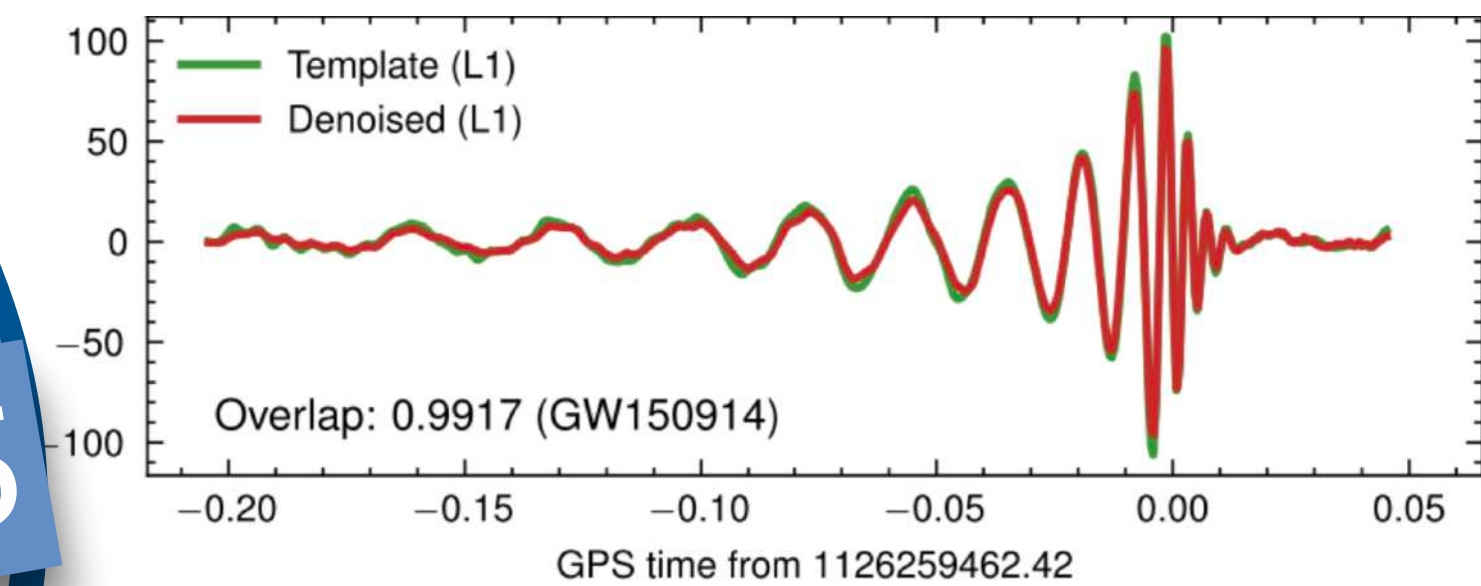
Waveform Modeling



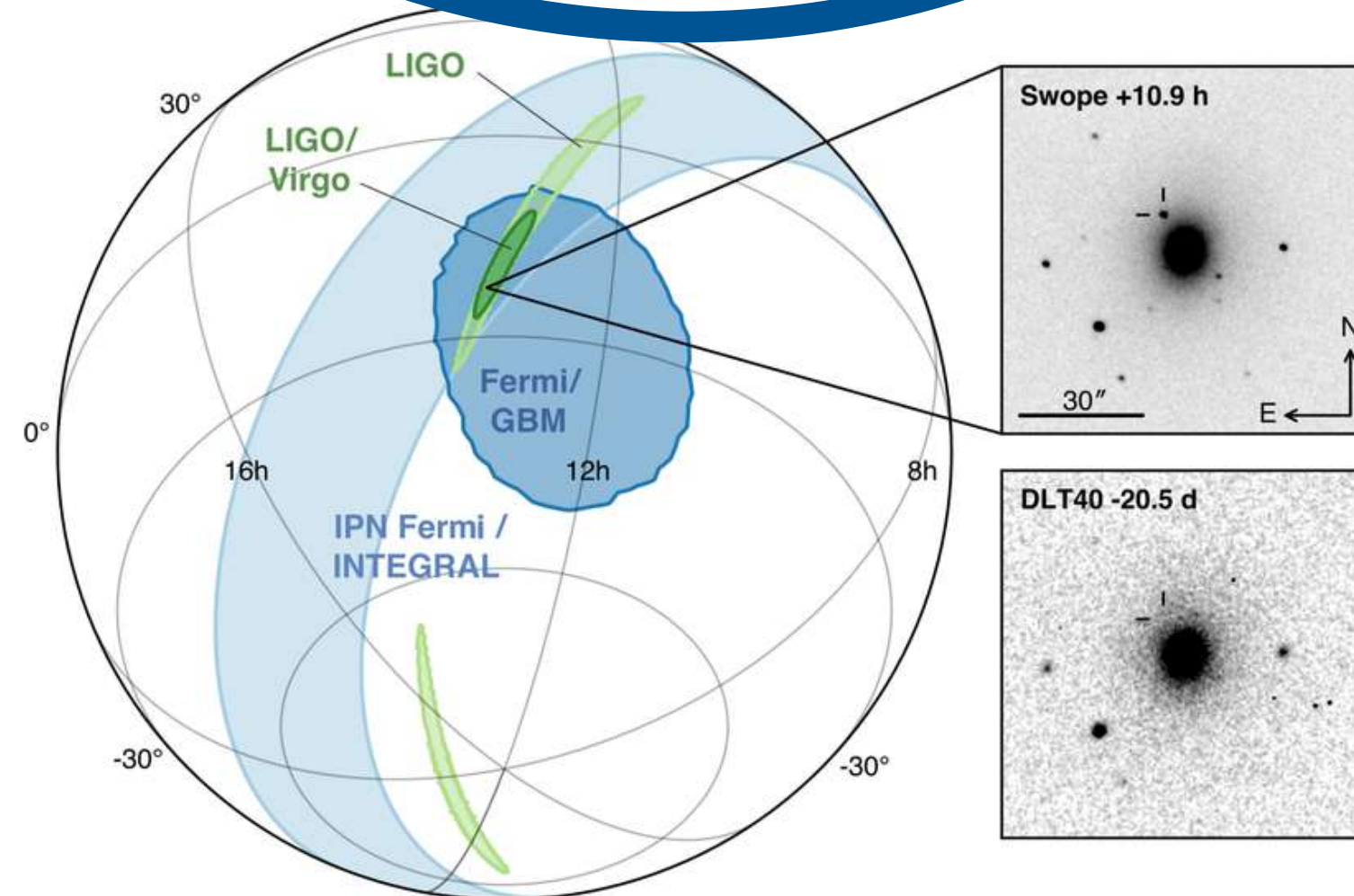
Detection



Denoising

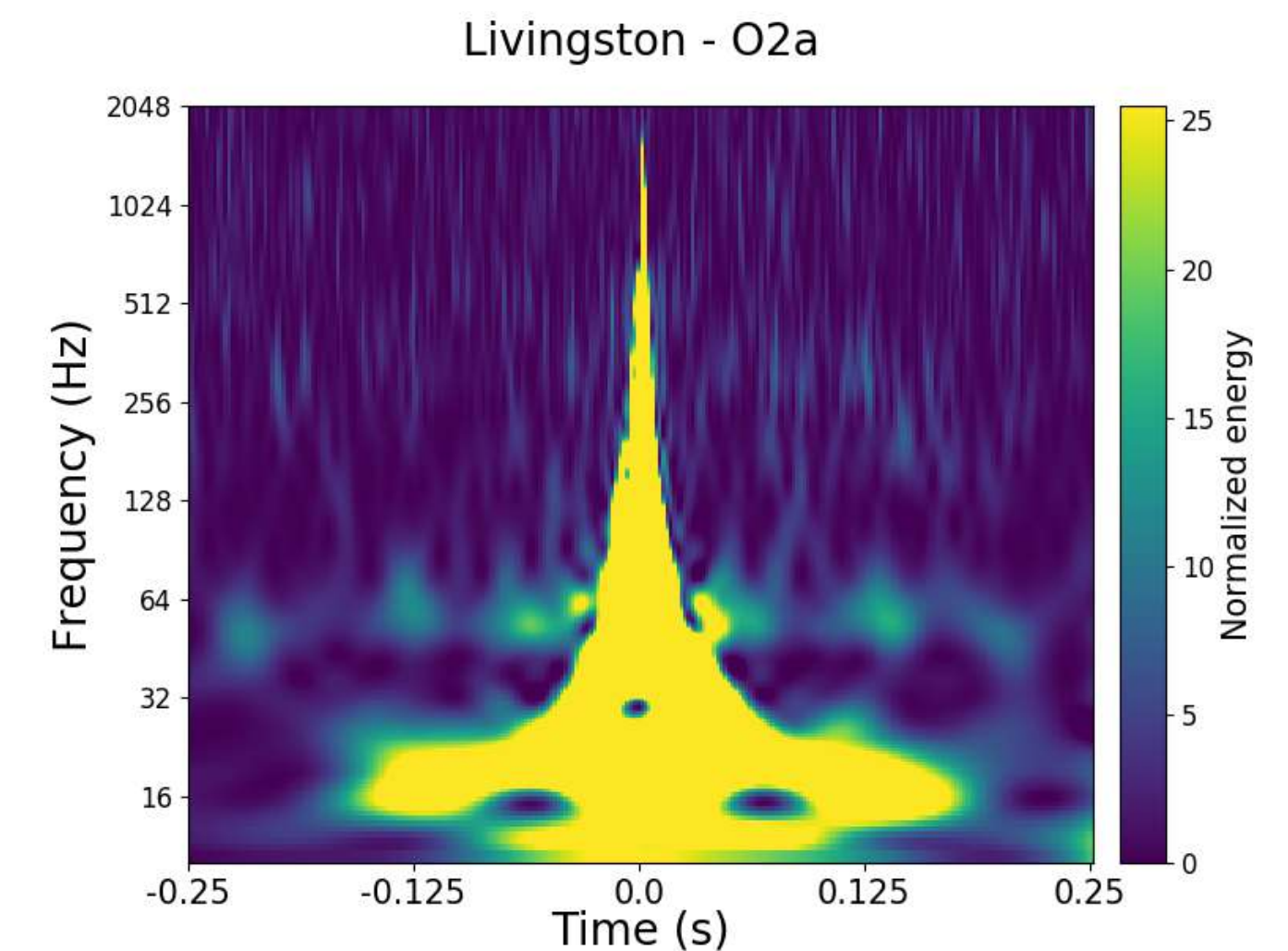
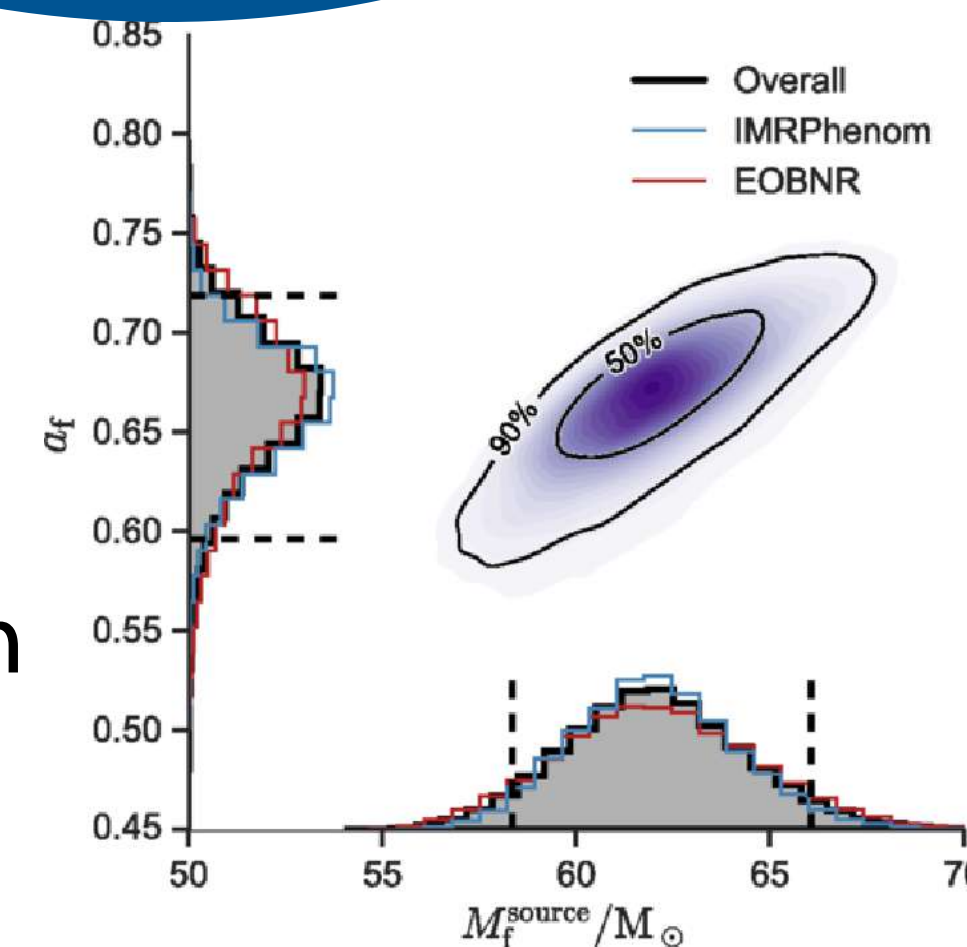


Glitch Classification



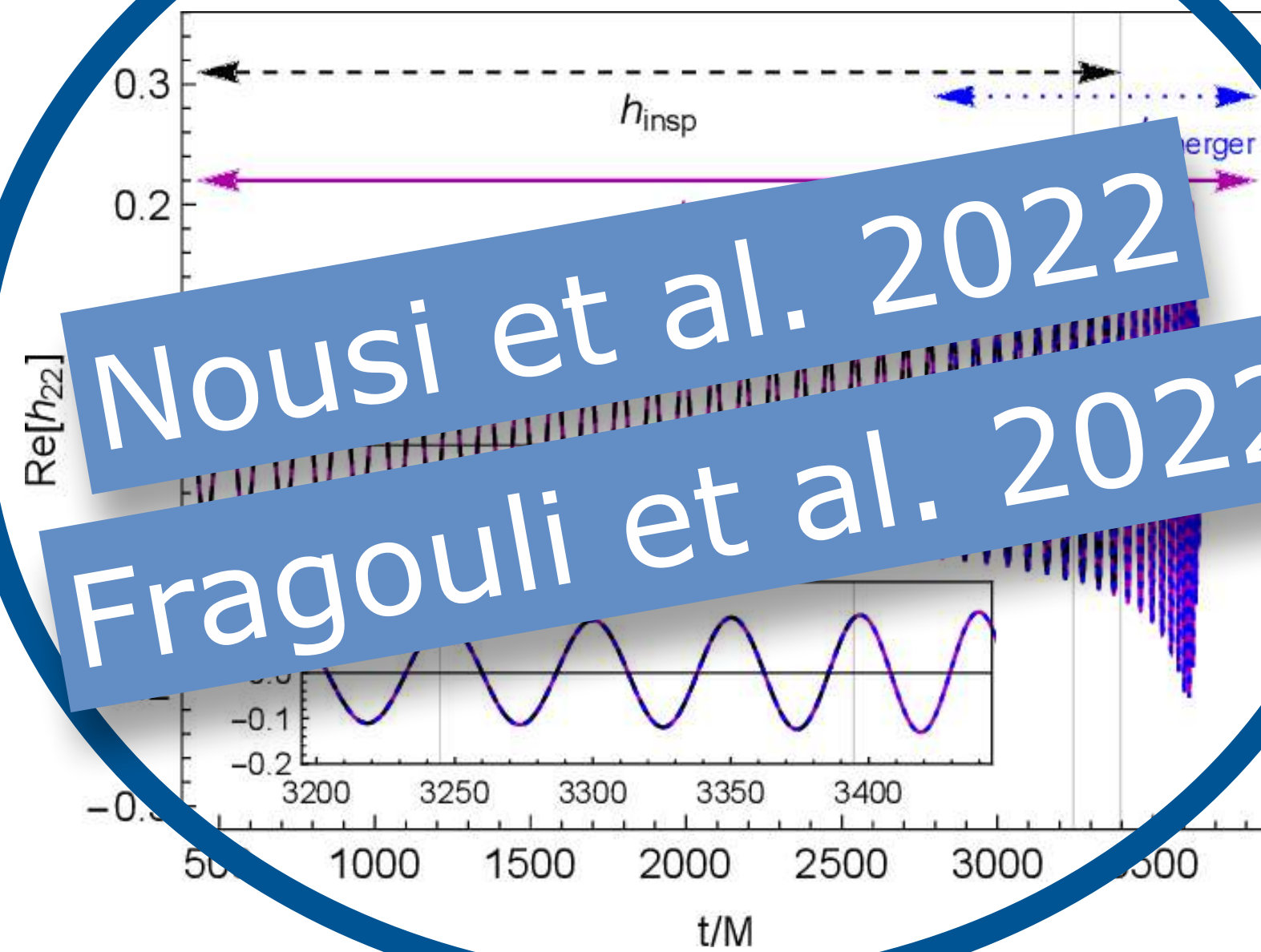
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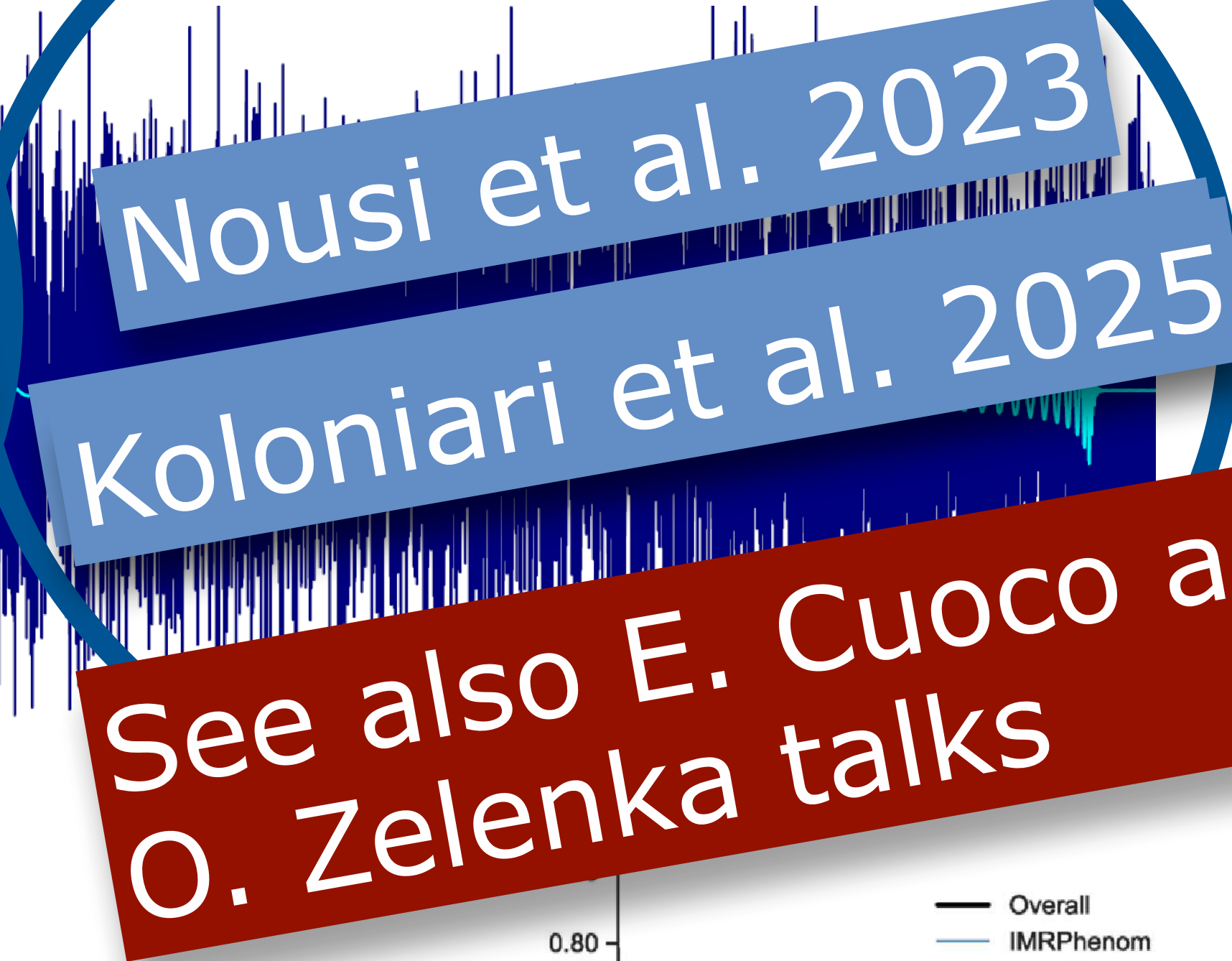


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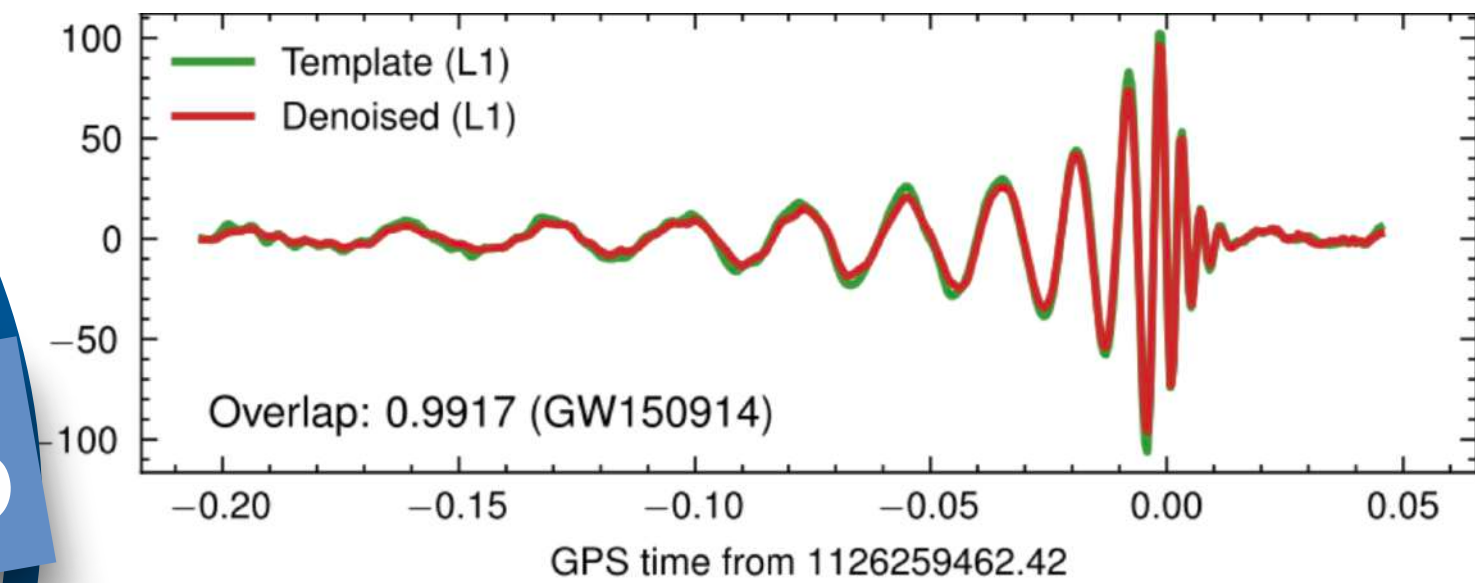
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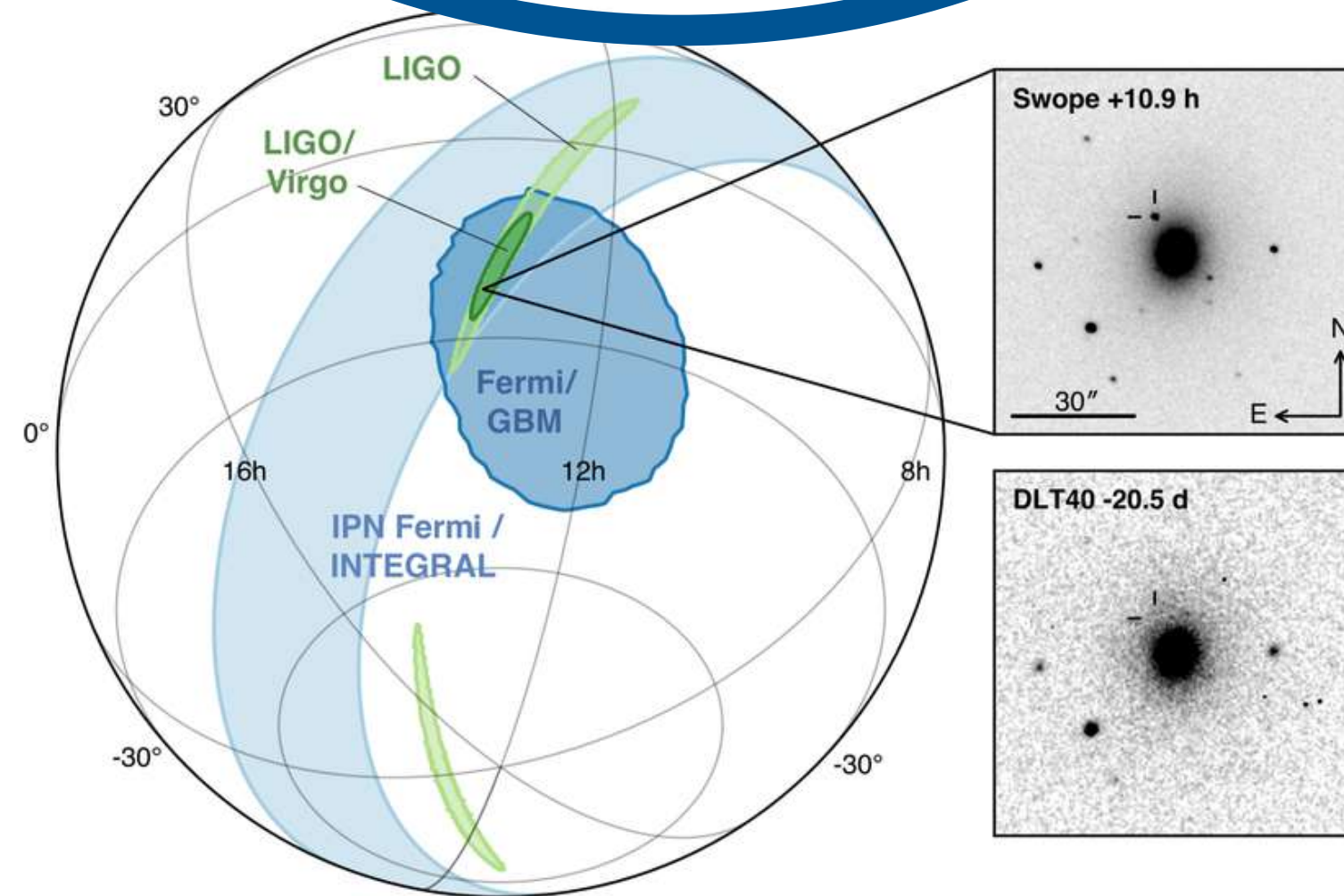
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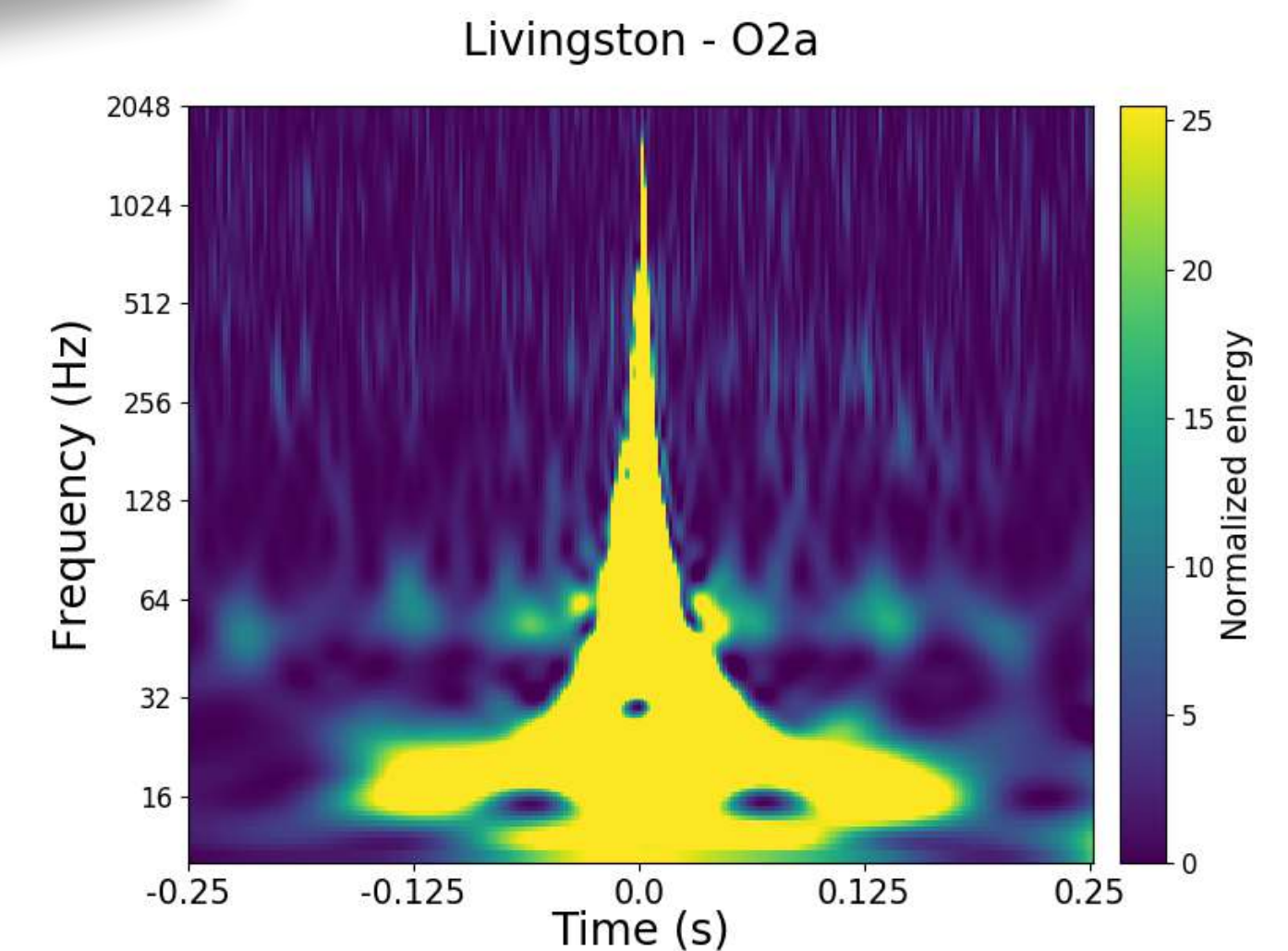
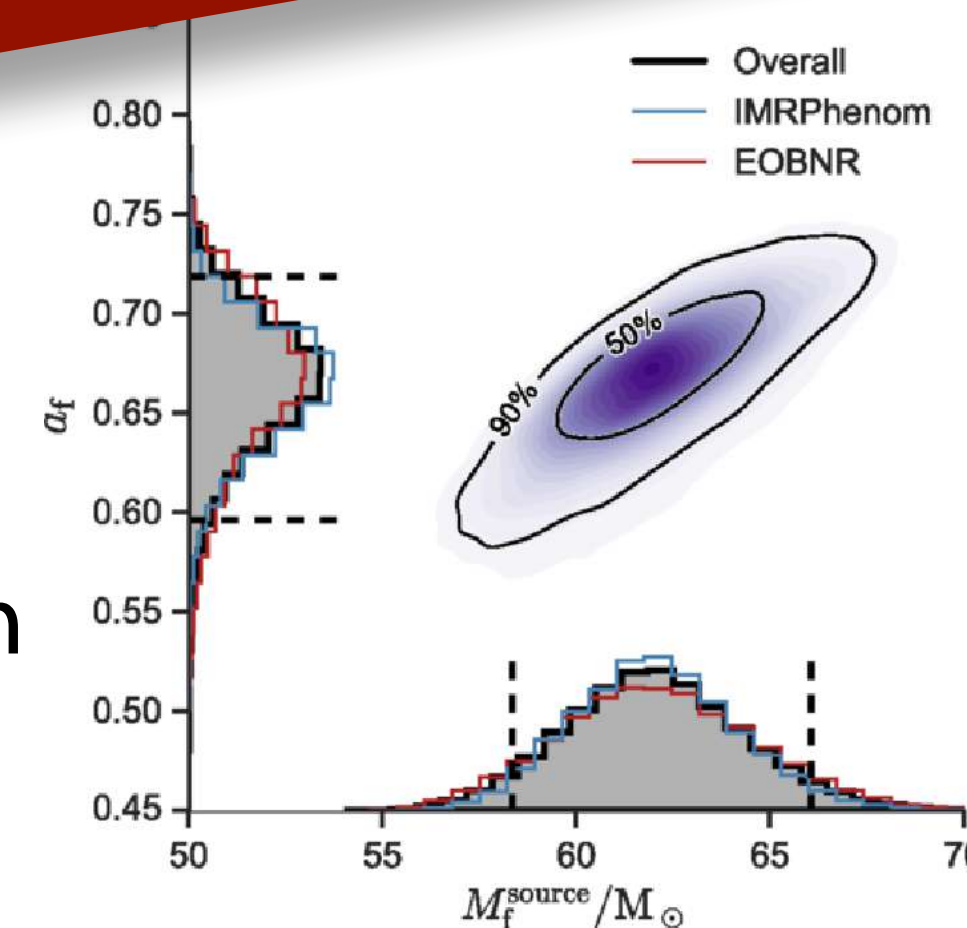


Glitch Classification



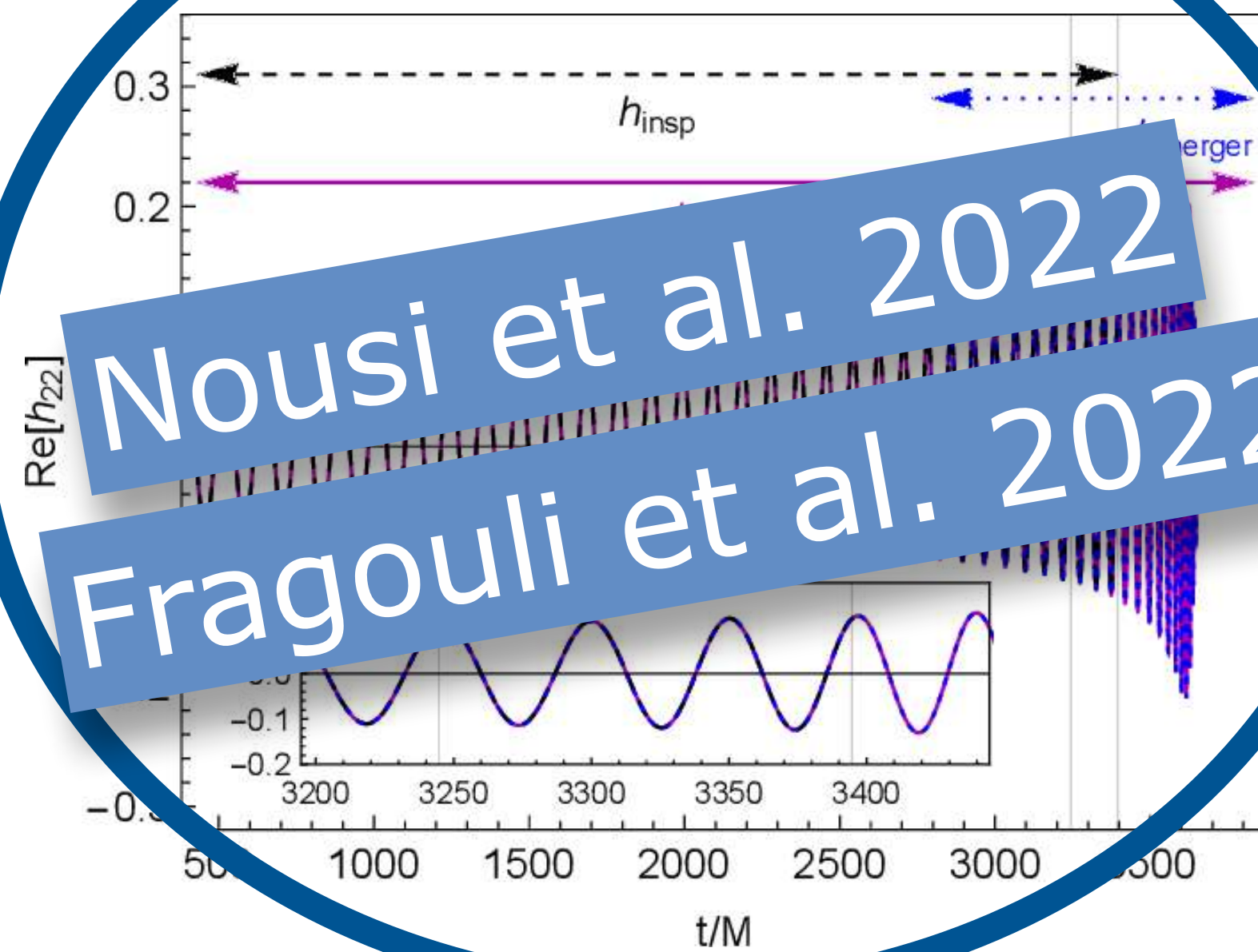
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MACHINE LEARNING IN GRAVITATIONAL WAVE ASTRONOMY

Waveform Modeling



Nousi et al. 2022

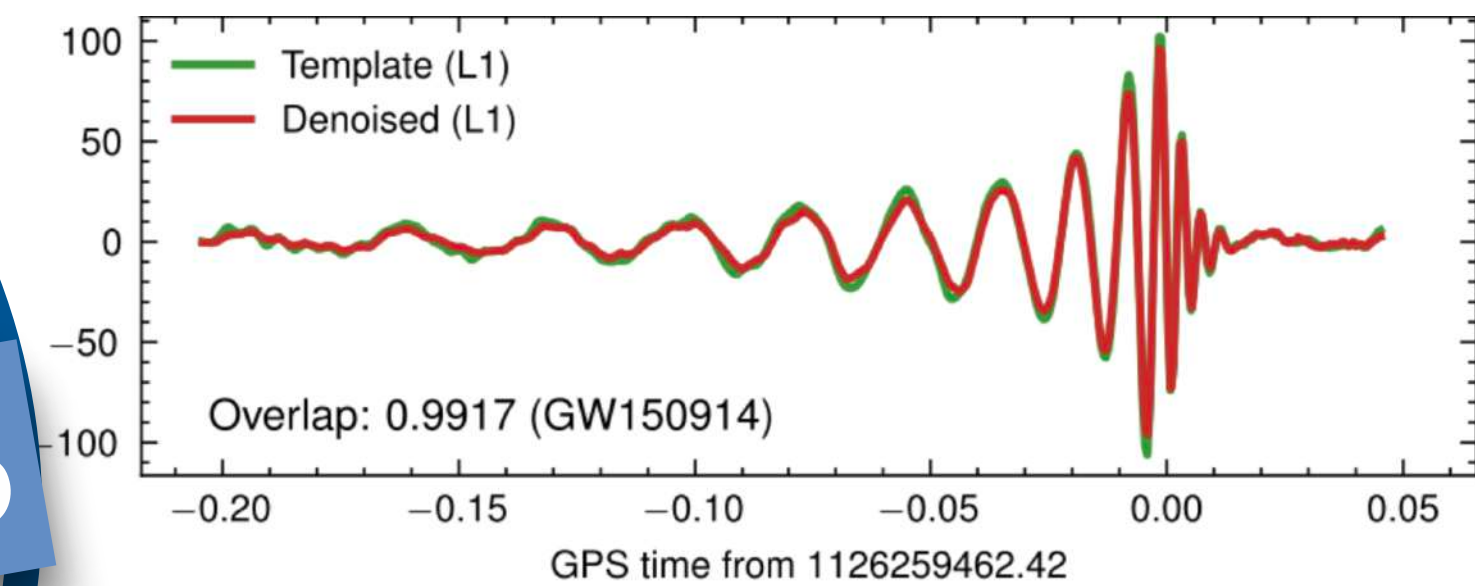
Fragouli et al. 2022

Detection

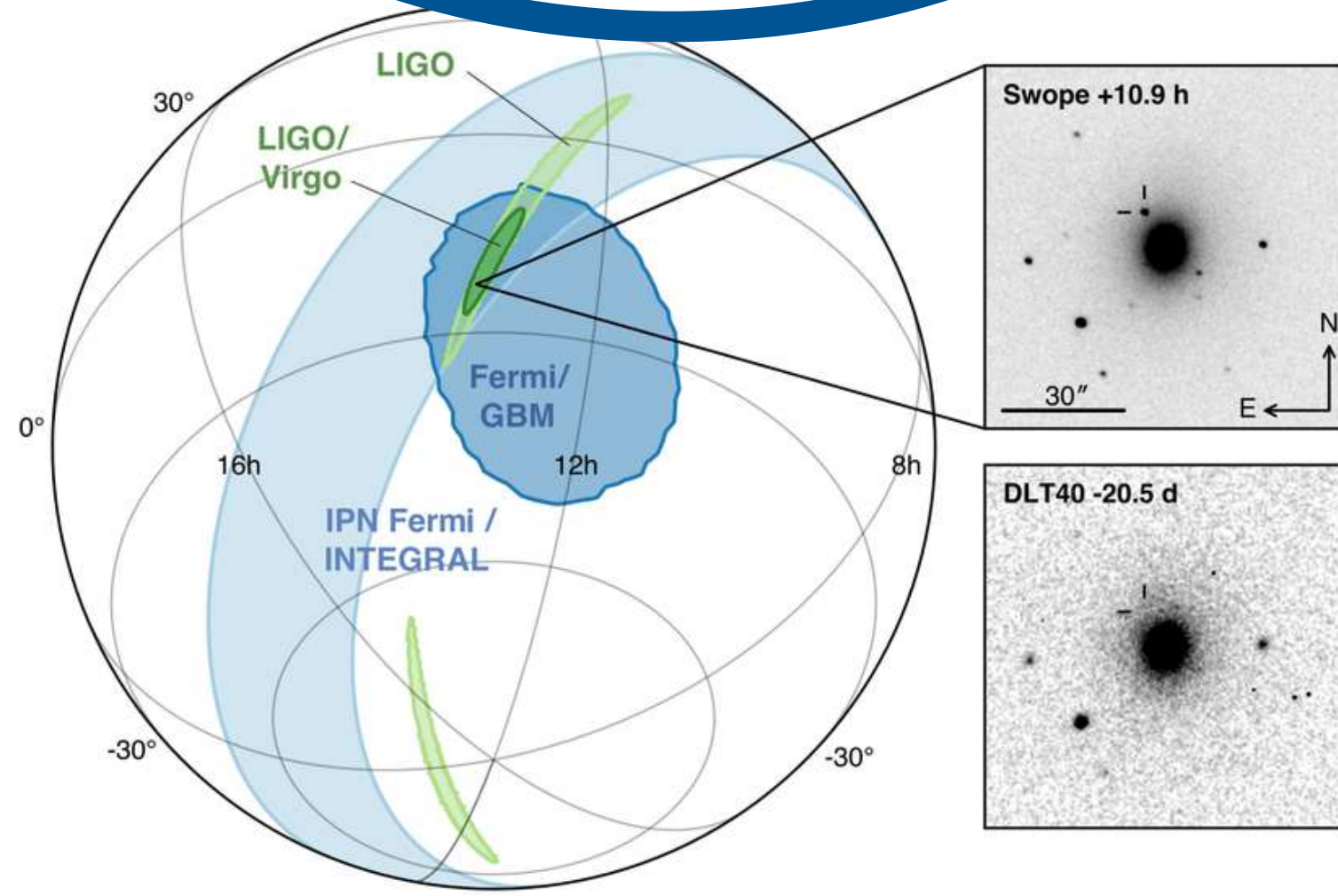


See also E. Cuoco and O. Zelenka talks

Denoising



Glitch Classification



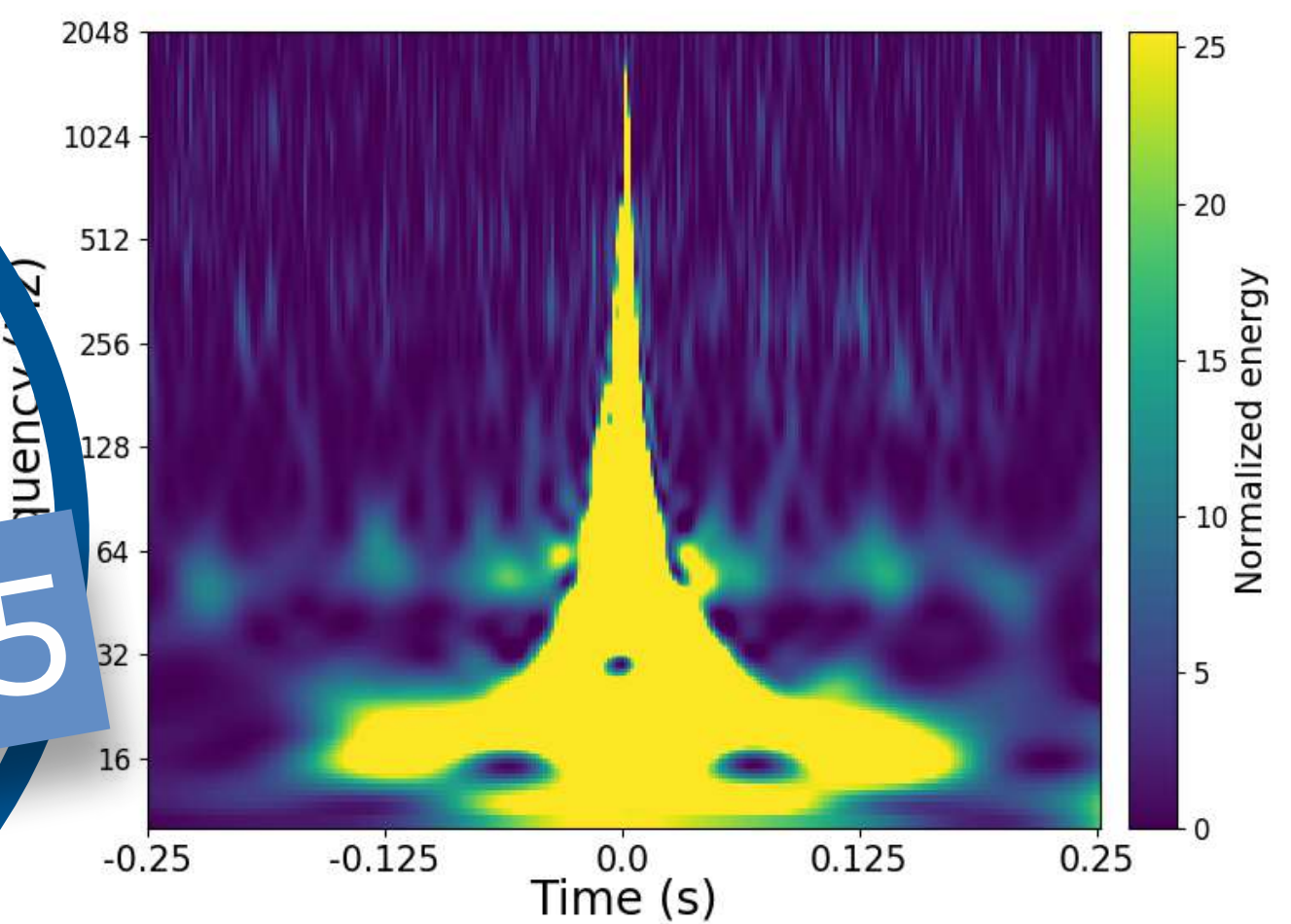
Parameter Estimation

Sky Localization



Vretinarris et al. 2025

Livingston - O2a



PHYSICAL REVIEW D **108**, 024022 (2023)

Deep residual networks for gravitational wave detection

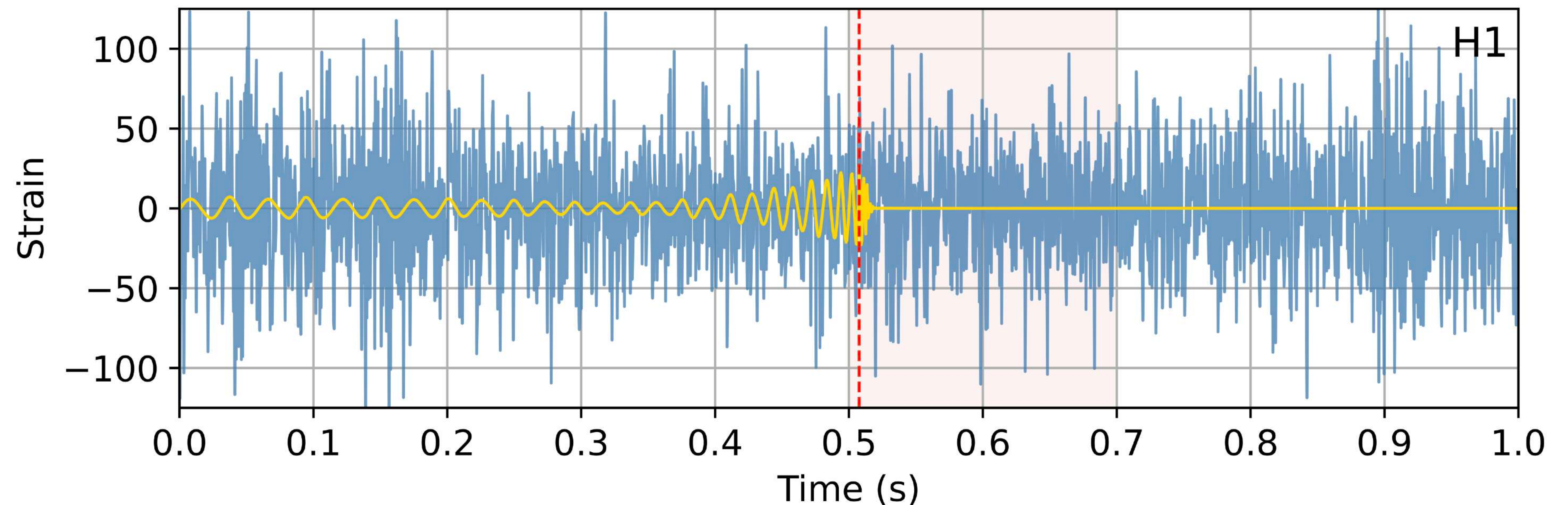
Paraskevi Nousi¹, Alexandra E. Koloniari², Nikolaos Passalis¹, Panagiotis Iosif²,
Nikolaos Stergioulas² and Anastasios Tefas¹

¹*Department of Informatics, Aristotle University of Thessaloniki, 54124 Thessaloniki, Greece*

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Architecture:

- 54-layer Resnet-1D
- Deep Adaptive Input Normalization
- SNR-based Curriculum Learning
- 30x faster than PyCBC (using a single GPU card)



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Mass range: $7M_{\odot} \leq M \leq 50M_{\odot}$

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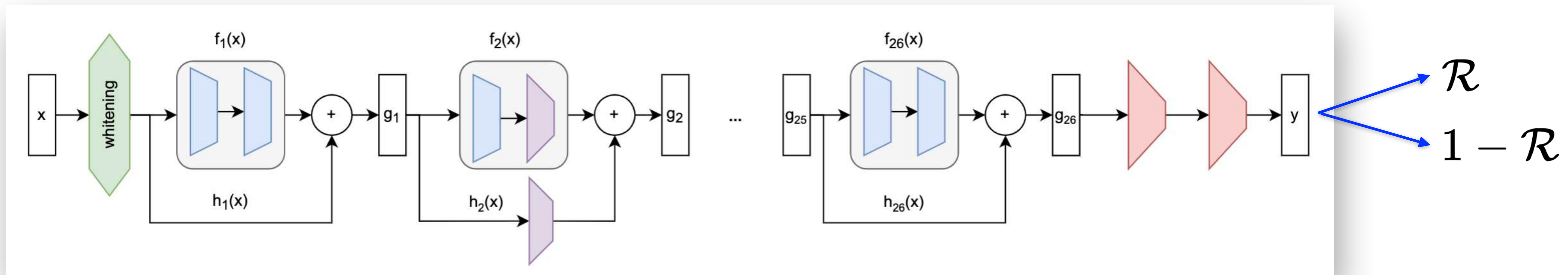
Mass range: $7M_{\odot} \leq M \leq 50M_{\odot}$

Leading algorithm (Virgo-AUTH) in the **1st ML GW search challenge** in the most demanding dataset.

<https://github.com/gwastro/ml-mock-data-challenge-1>

NETWORK ARCHITECTURE OF ARES-GW

1-D ResNet-54 (27 residual blocks with 2 convolutional layers each and skip connections)!

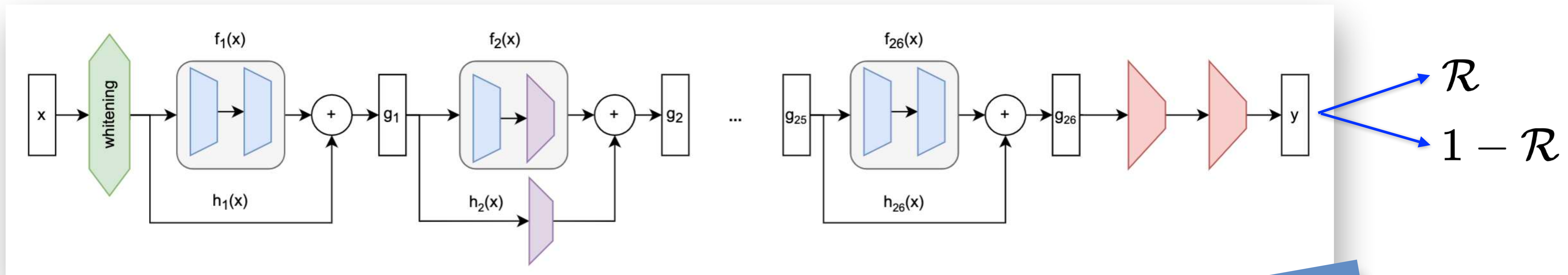


- Residual blocks with skip connections: $g(\mathbf{x}) = f(\mathbf{x}) + h(\mathbf{x})$
- $h(\mathbf{x}) = \mathbf{x}$ or a strided convolutional layer
- After each convolutional layer: batch normalization + ReLU activation
- Mini-batch size of 400 segments
- Adam optimizer for back propagation
- Objective function = regularized binary cross entropy

Residual blocks	Filters	Strided	Input D
4	8		2×2048
1	16	✓	8×2048
2	16		16×1024
1	32	✓	16×1024
2	32		32×512
1	64	✓	32×512
2	64		64×256
1	64	✓	64×256
2	64		64×128
1	64	✓	64×128
2	64		64×64
5	32		64×64
3	16		32×64

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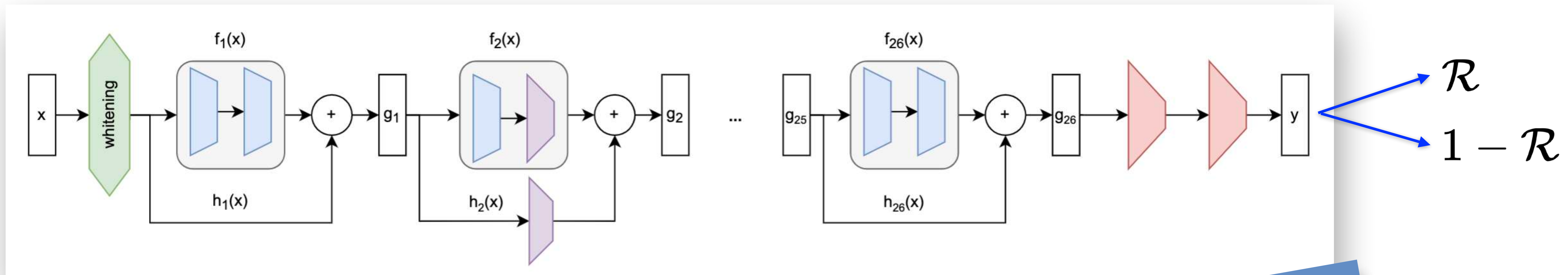
- Residual blocks with skip connections: $g(x) = f(x) + x$
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Gradient problem solved!
-> much deeper networks

			Input D
			2×2048
		✓	8×2048
	16		16×1024
	32	✓	16×1024
1	32		32×512
2	64	✓	32×512
1	64	✓	64×256
2	64		64×256
1	64	✓	64×128
2	64		64×128
5	32		64×64
3	16		32×64

NETWORK ARCHITECTURE OF ARES-GW

1-D ResNet-54 (27 residual blocks with 2 convolutional layers each and skip connections)!



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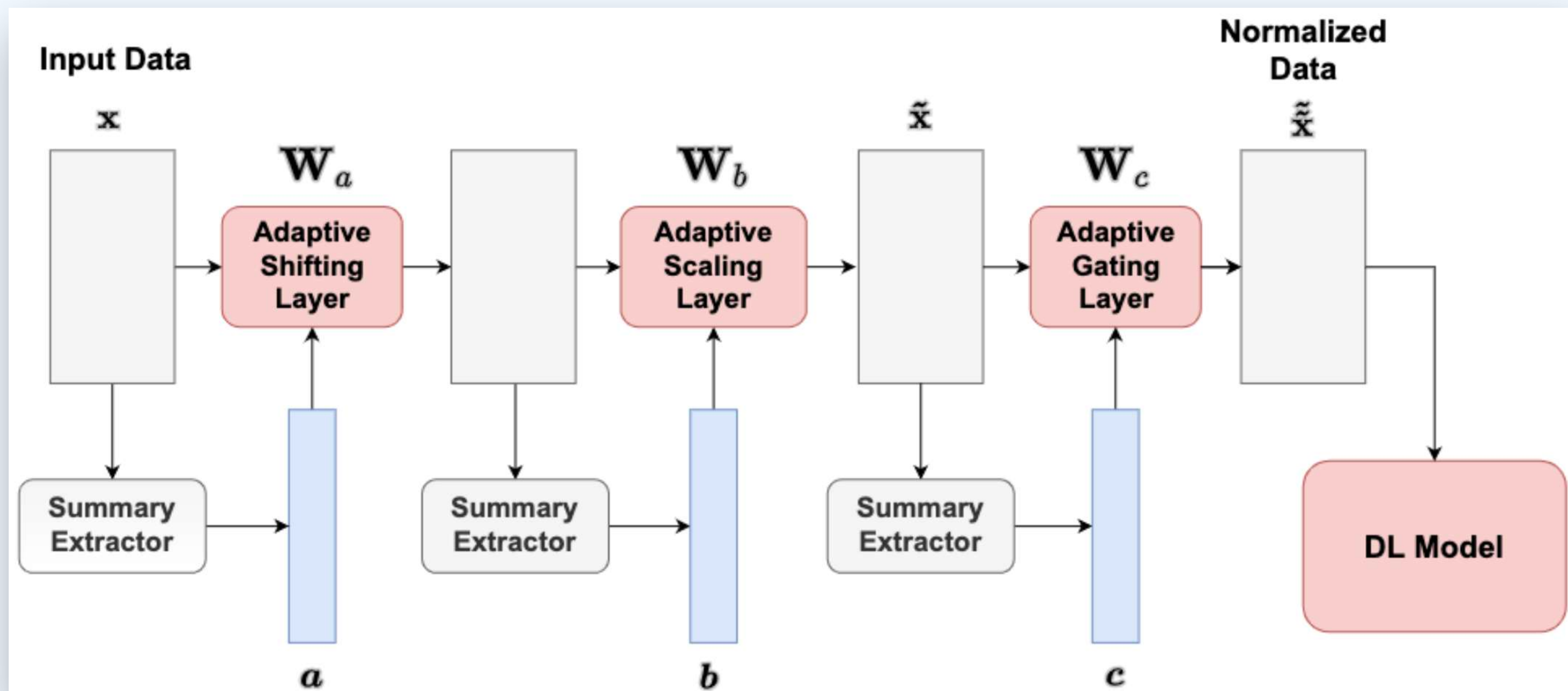
1-D ResNet-54 now used by most
ML GW detection codes

		Input D
		2×2048
		8×2048
1	16	✓
2	32	
3	64	
4	64	✓
5	32	
6	16	
		64×256
		64×128
		64×128
		64×64
		64×64
		32×64

ADAPTIVE INPUT NORMALIZATION

Deep Adaptive Input Normalization (DAIN) (Passalis et al. 2019)

Is applied during training - weights $\mathbf{W}_a$, $\mathbf{W}_b$, $\mathbf{W}_c$ are learnable and adapt to input data!



ARESGW ON GITHUB

<https://github.com/vivinousi/gw-detection-deep-learning>

The screenshot displays the GitHub repository page for `vivinousi/gw-detection-deep-learning`. The repository is public and has 22 stars, 2 forks, and 7 watchers. The repository description is "Gravitational wave detection in real noise timeseries using deep residual neural networks".

The repository structure is as follows:

File/Folder	Commit Message	Commit Time
doc	readme update	2 years ago
modules	training code initial commit	2 years ago
trained_models	training code initial commit	2 years ago
utils	training code initial commit	2 years ago
LICENSE	Initial commit	2 years ago
README.md	readme update	2 years ago
run_on_test.sh	training code initial commit	2 years ago
test.py	training code initial commit	2 years ago
test_challenge_model.py	training code initial commit	2 years ago
train.py	readme update	2 years ago

The repository details section includes the following information:

- About:** Gravitational wave detection in real noise timeseries using deep residual neural networks. Includes a Readme, Apache-2.0 license, and 22 stars.
- Releases:** No releases published.
- Packages:** No packages published.
- Languages:** Python 98.4%, Shell 1.6%.

The README section is titled "AResGW: Augmentation and RESidual networks for Gravitational Wave detection". It describes the project as "Gravitational wave detection in real noise timeseries using deep residual neural networks." and mentions that the repository contains the method submitted by the team, Virgo-AUTH, to the [MLGWSC](#) competition. The method contains the following components:



PAPER

New gravitational wave discoveries enabled by machine learning

OPEN ACCESS

Alexandra E Koloniari^{1,*} , Evdokia C Koursoumpa¹ , Paraskevi Nousi² , Paraskevas Lampropoulos¹ , Nikolaos Passalis³ , Anastasios Tefas⁴  and Nikolaos Stergioulas¹ 

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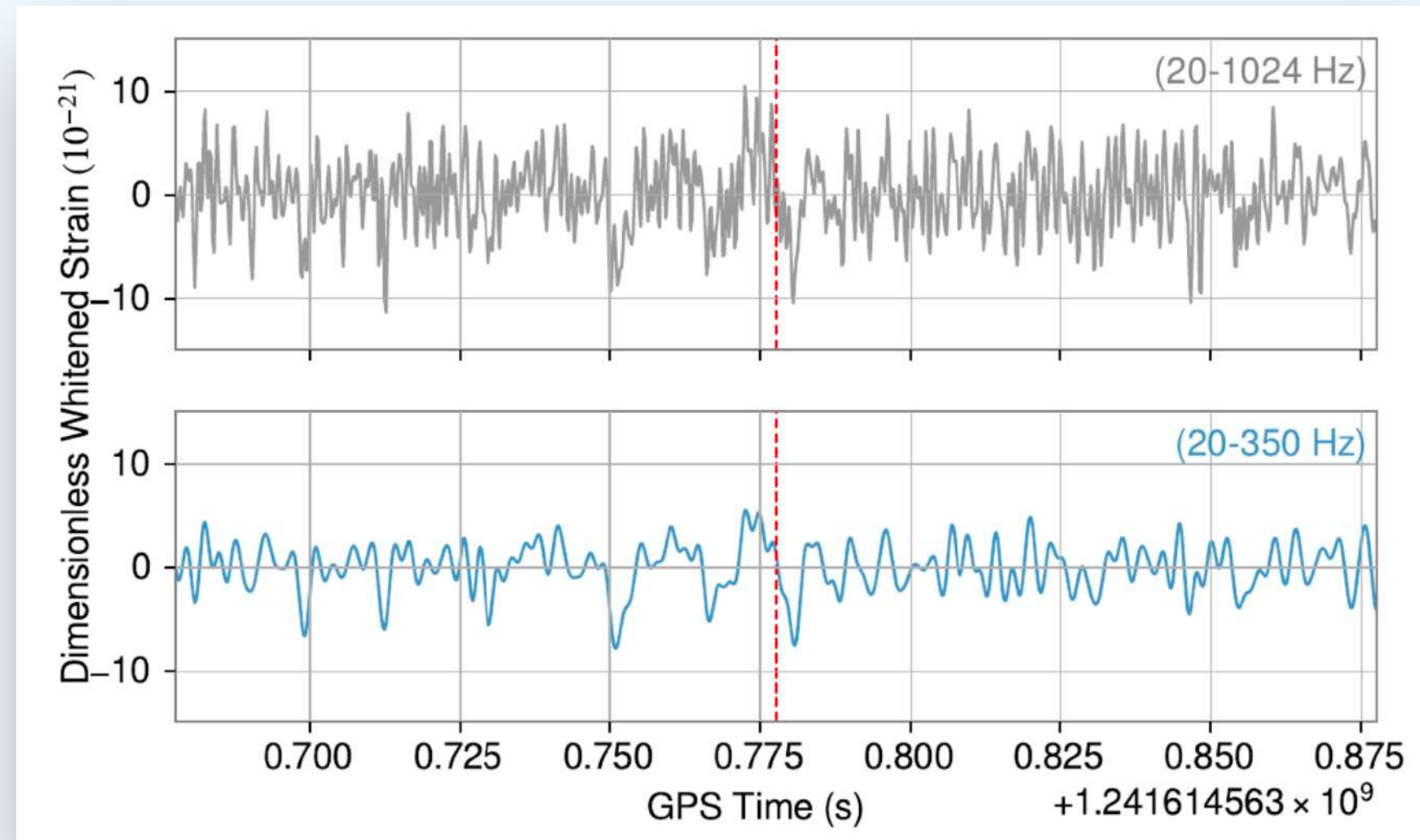
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E-mail: akolonia@auth.gr

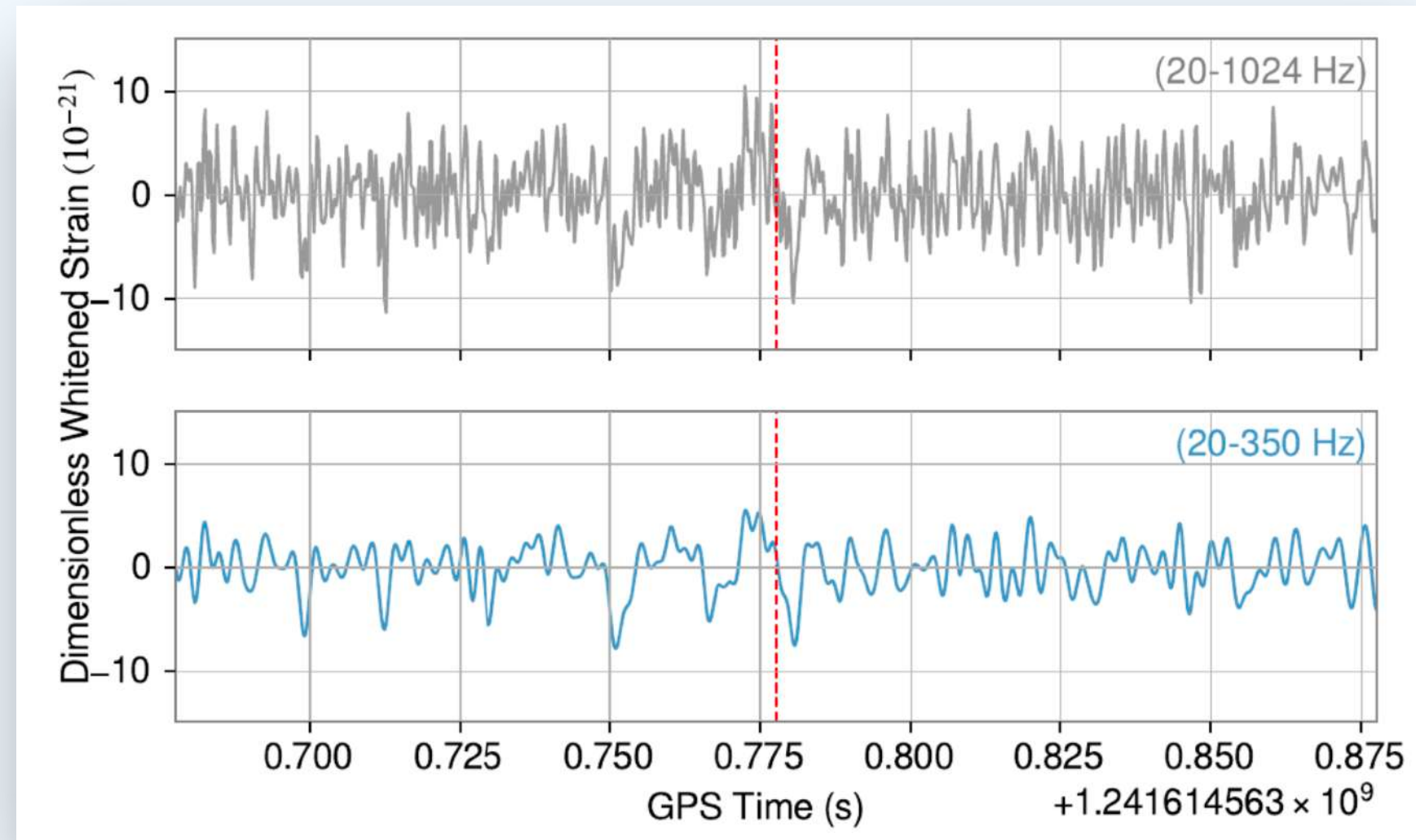
MAIN ENHANCEMENTS:

1) Training on low-pass filtered data

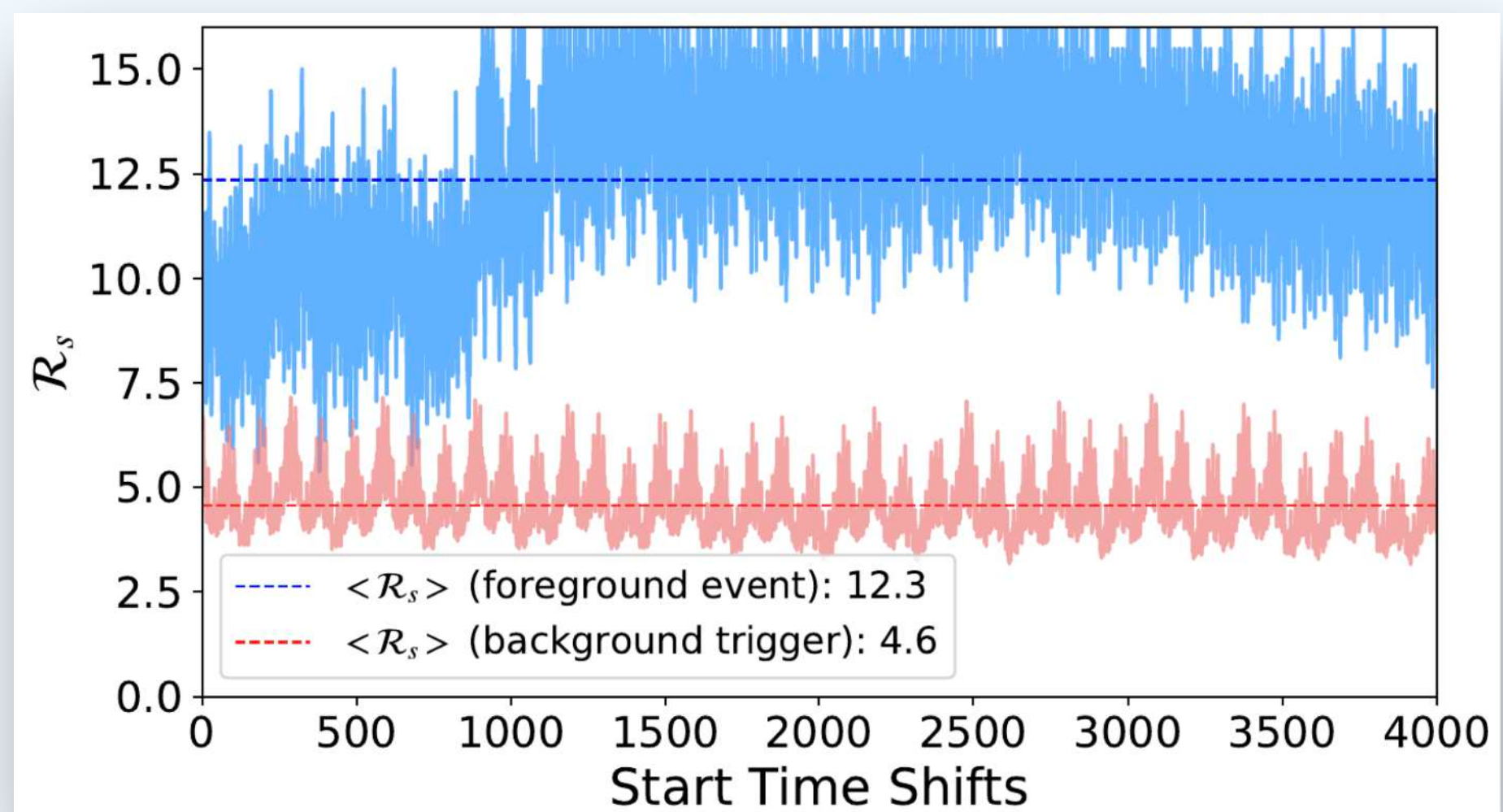


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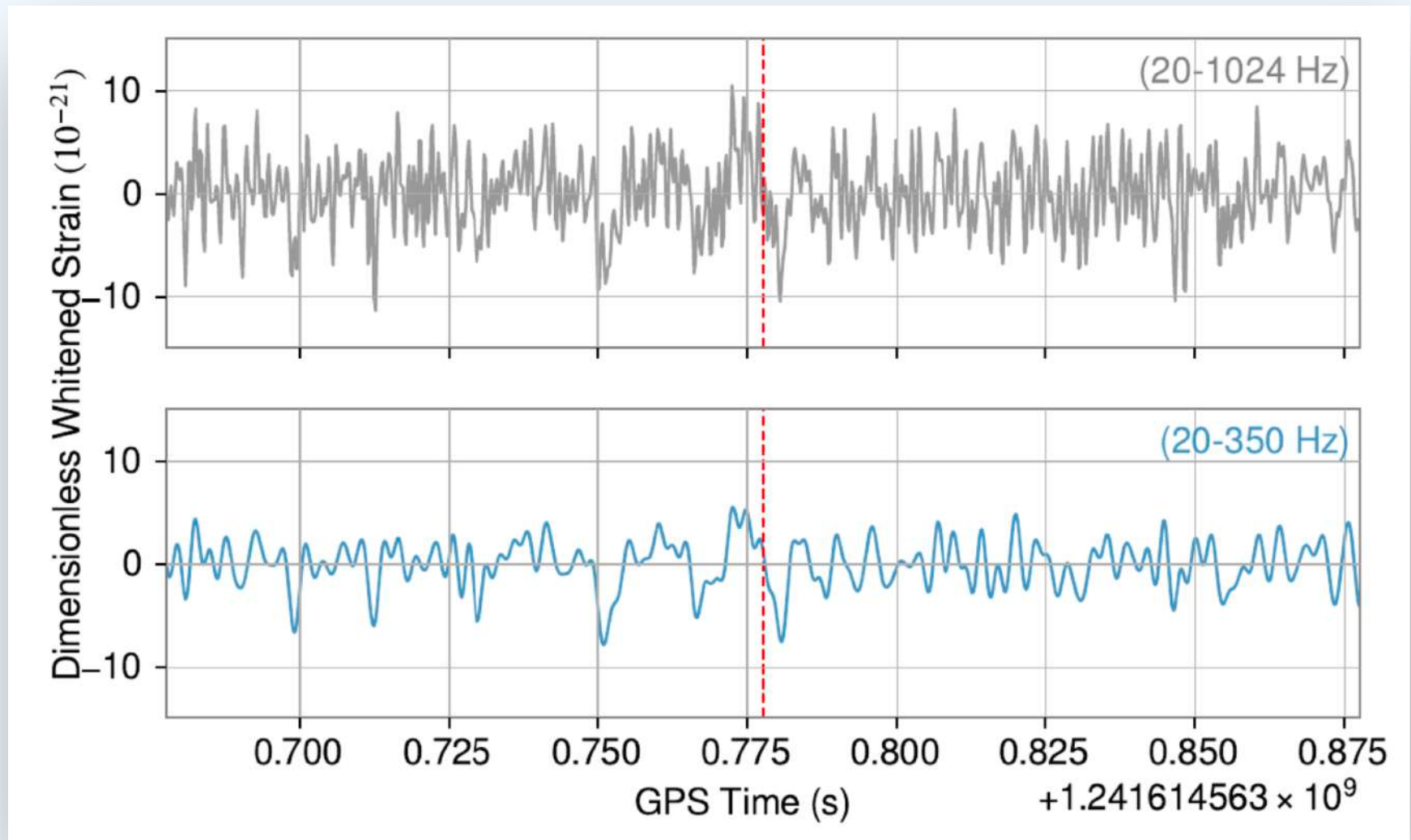


2) Ensemble-averaged ranking statistic

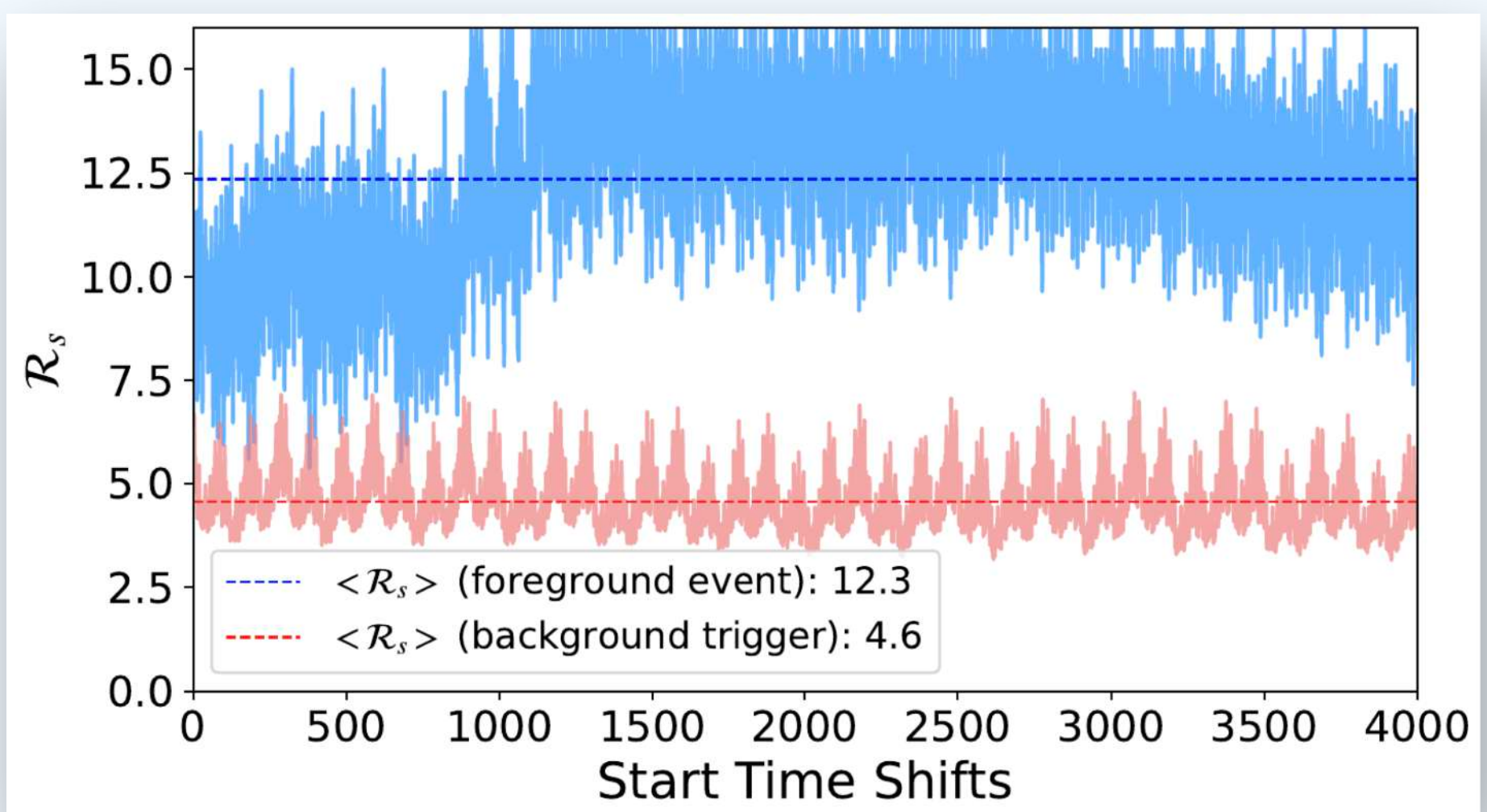


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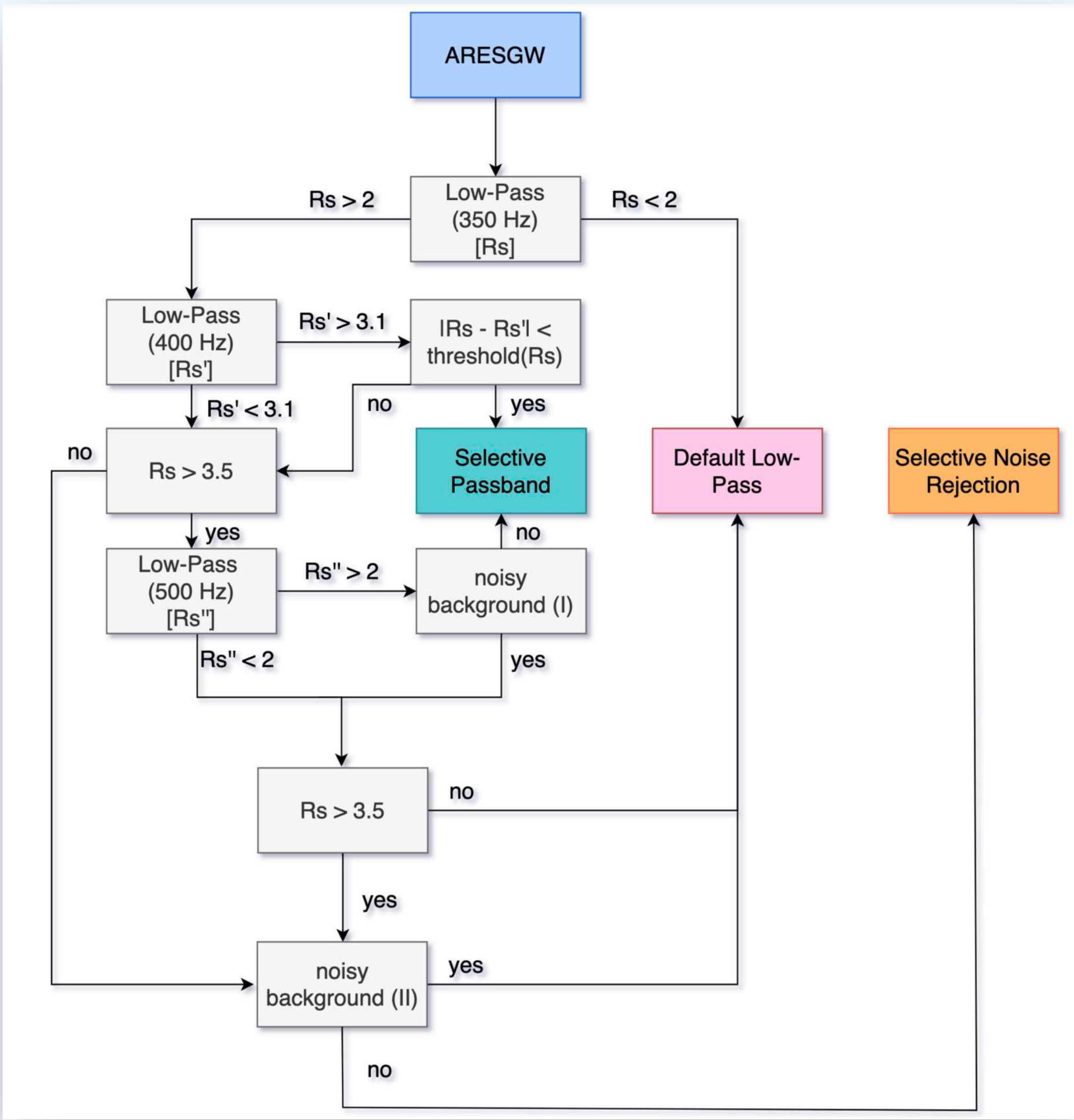
1) Training on low-pass filtered data



2) Ensemble-averaged ranking statistic



3) Application of noise filters to reduce background FAR.



ASTROPHYSICAL PROBABILITY

p_astro is calculated as

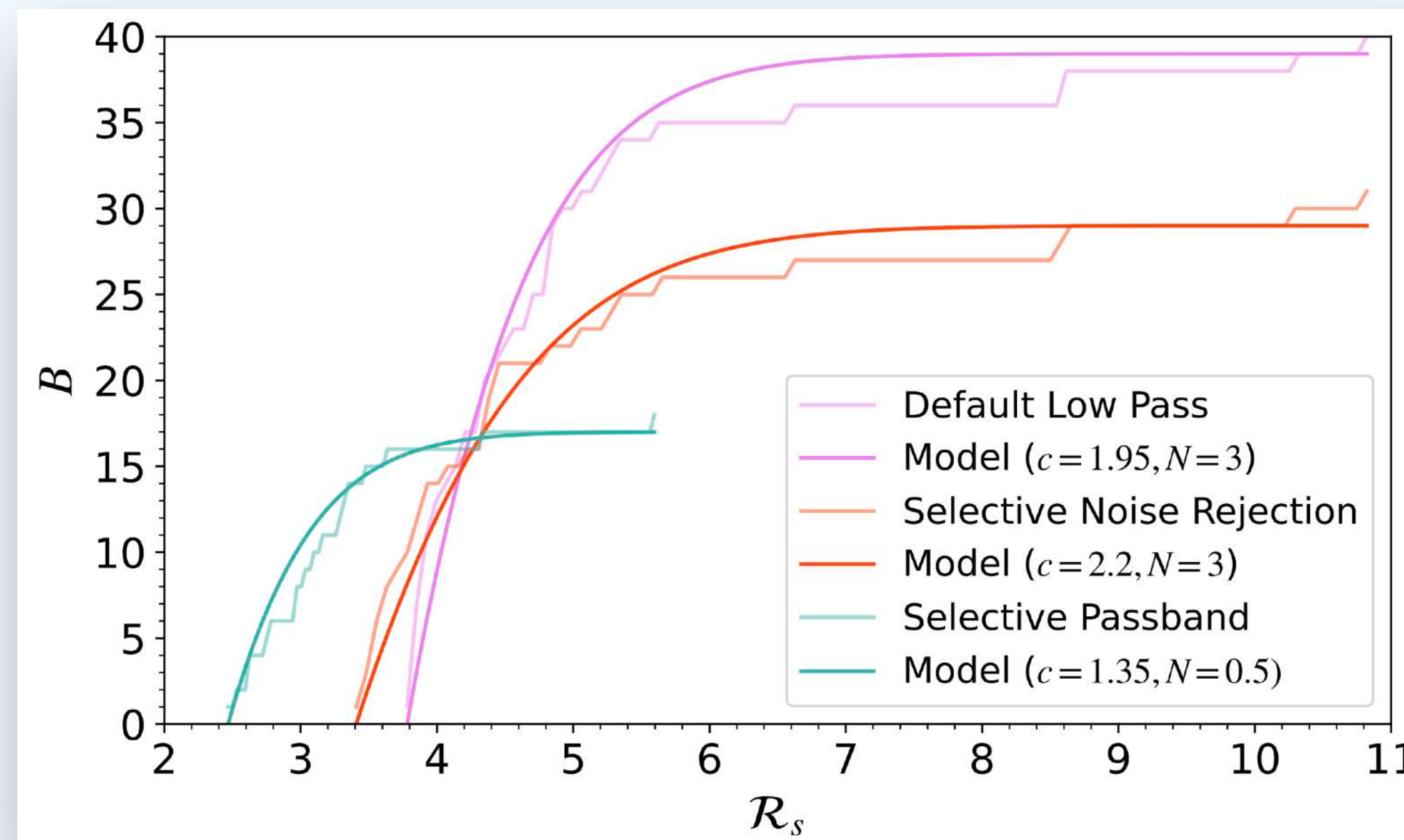
$$p_{\text{astro}} = \frac{f(\mathcal{R}_s)}{b(\mathcal{R}_s) + f(\mathcal{R}_s)}$$

where the **background** and **foreground differential rates** are

$$b(\mathcal{R}_s) = \frac{dB}{d\mathcal{R}_s} \quad f(\mathcal{R}_s) = \frac{dF}{d\mathcal{R}_s}$$

The cumulative distribution of the **O3 background** is modeled **analytically** as

$$\hat{B}(x) = \frac{\left(1 + \operatorname{erf}\left(\frac{x}{\sqrt{2}}\right)\right)^N - \left(1 + \operatorname{erf}\left(\frac{x_{\min}}{\sqrt{2}}\right)\right)^N}{2^N - \left(1 + \operatorname{erf}\left(\frac{x_{\min}}{\sqrt{2}}\right)\right)^N}$$

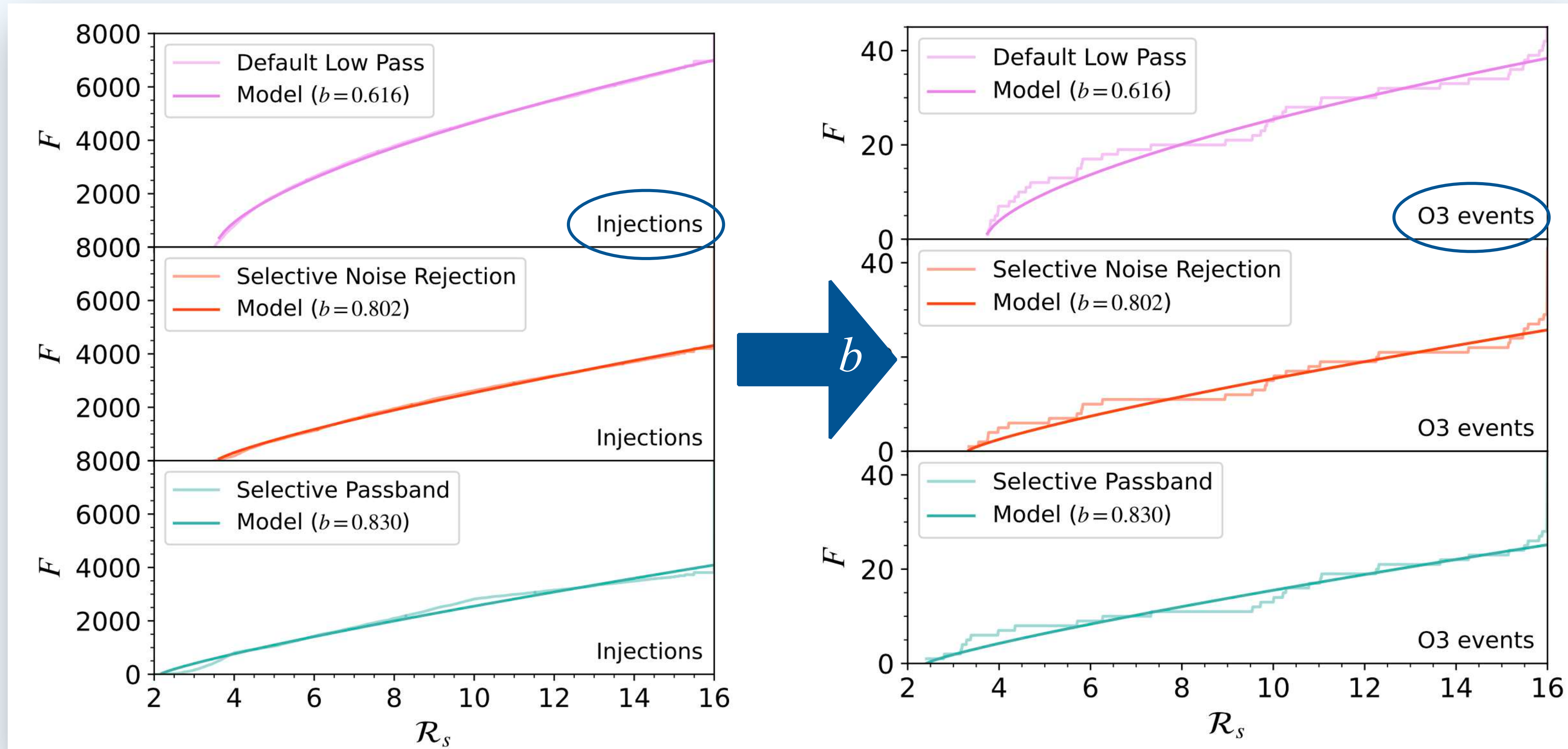


ASTROPHYSICAL PROBABILITY

Analytic model of **cumulative foreground** distribution:

$$F(x) = a(x - x_{\min})^b$$

Coefficient **b** determined through **injections** in O3 noise:



NEW GW DETECTIONS WITH AresGW IN O3 DATA

AresGW detects **42 out of 51** known O3 events (*most sensitive pipeline in this mass range*)

We found **8 new gravitational wave candidates** with $p_{\text{astro}} > 50\%$ (3 $p_{\text{astro}} > 99\%$).

TABLE VII: New candidate events identified by AresGW.

#	Event Name	GPS Time (s)	p_{astro}	FAR (1/yr)	$\langle \mathcal{R}_s \rangle$	Time delay (s)	χ_L^2	χ_H^2	Class
1	GW190511_125545	1241614563.77	1.00	0.27	9.54	0.0027	1.16	1.46	Selective Passband
2	GW190614_134749	1244555287.93	0.99	4.6	5.80	0.0012	0.65	0.80	Selective Passband
3	GW190607_083827	1243931925.99	0.99	6.5	8.95	0.0056	0.90	0.48	Selective Noise Rejection
4	GW190904_104631	1251629209.01	0.72	14	4.35	0.0002	0.38	0.71	Selective Passband
5	GW190523_085933	1242637191.44	0.68	20	6.60	0.0054	0.75	1.39	Selective Noise Rejection
6	GW200208_211609	1265231787.68	0.55	18	4.0	0.0063	0.69	0.98	Selective Passband
7	GW190705_164632	1246380410.88	0.51	49	5.82	0.0103	1.05	0.98	Default Low-Pass*
8	GW190426_082124	1240302101.93	0.50	20	3.91	0.0007	1.48	0.53	Selective Passband

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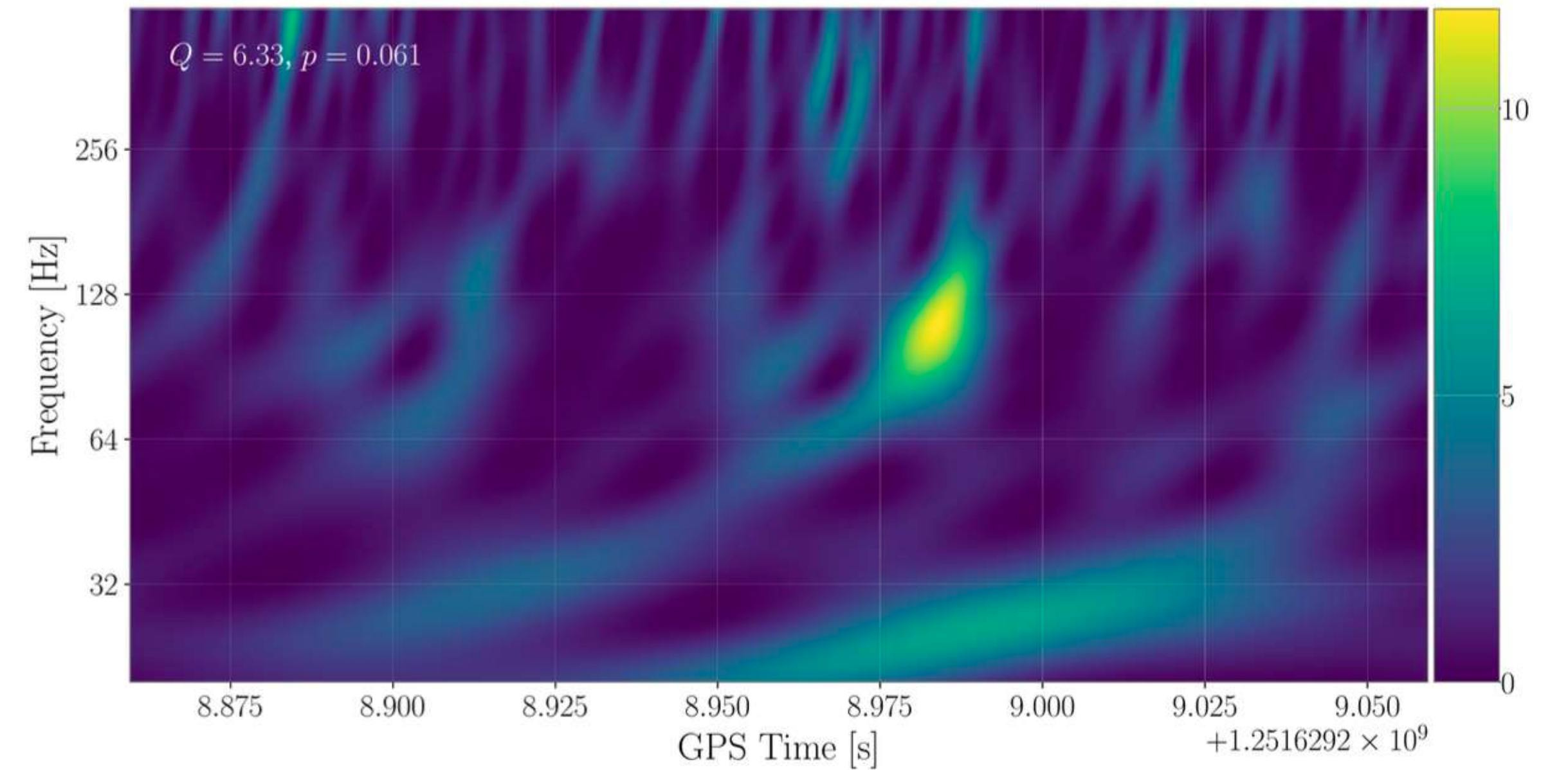
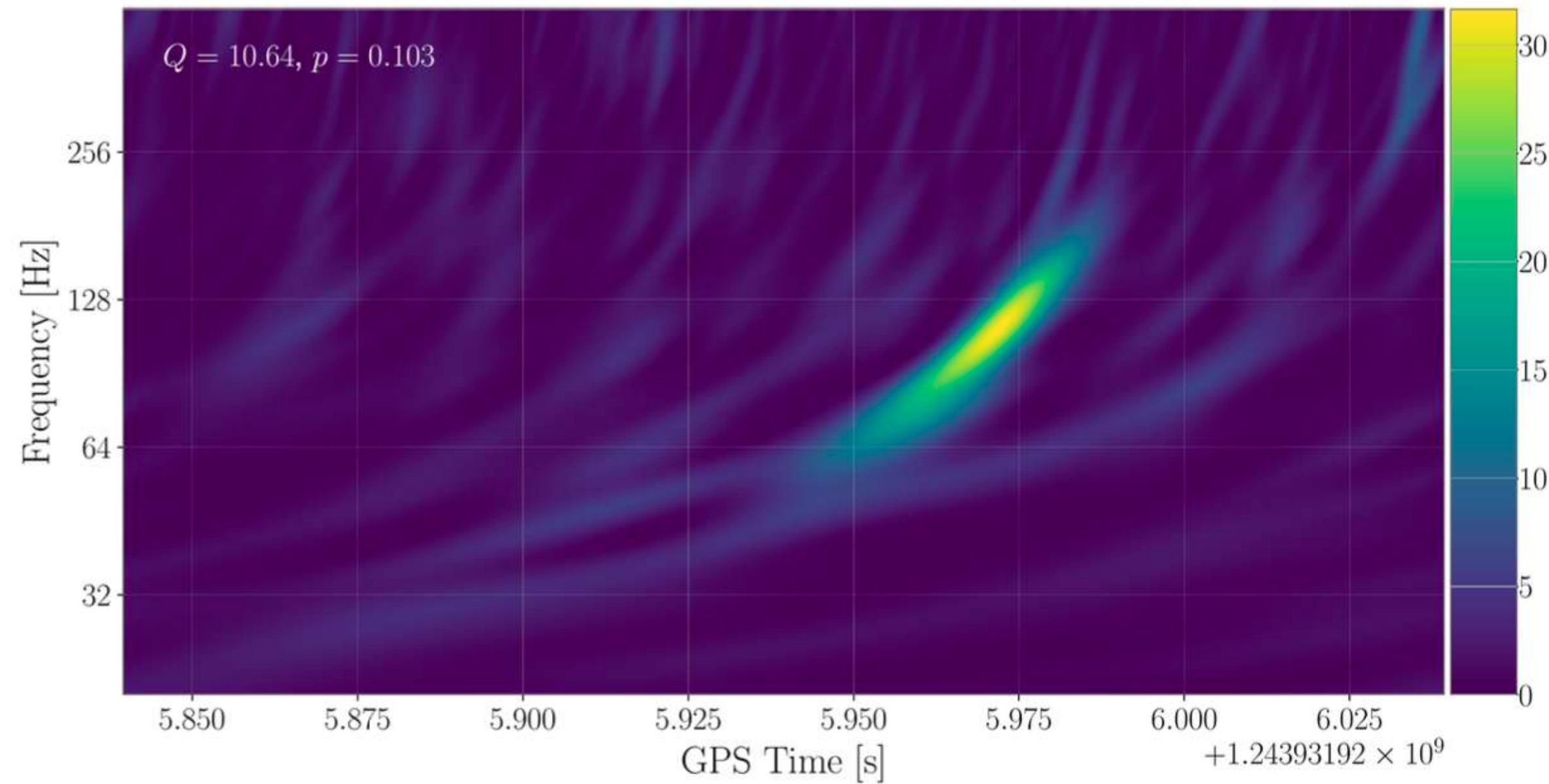
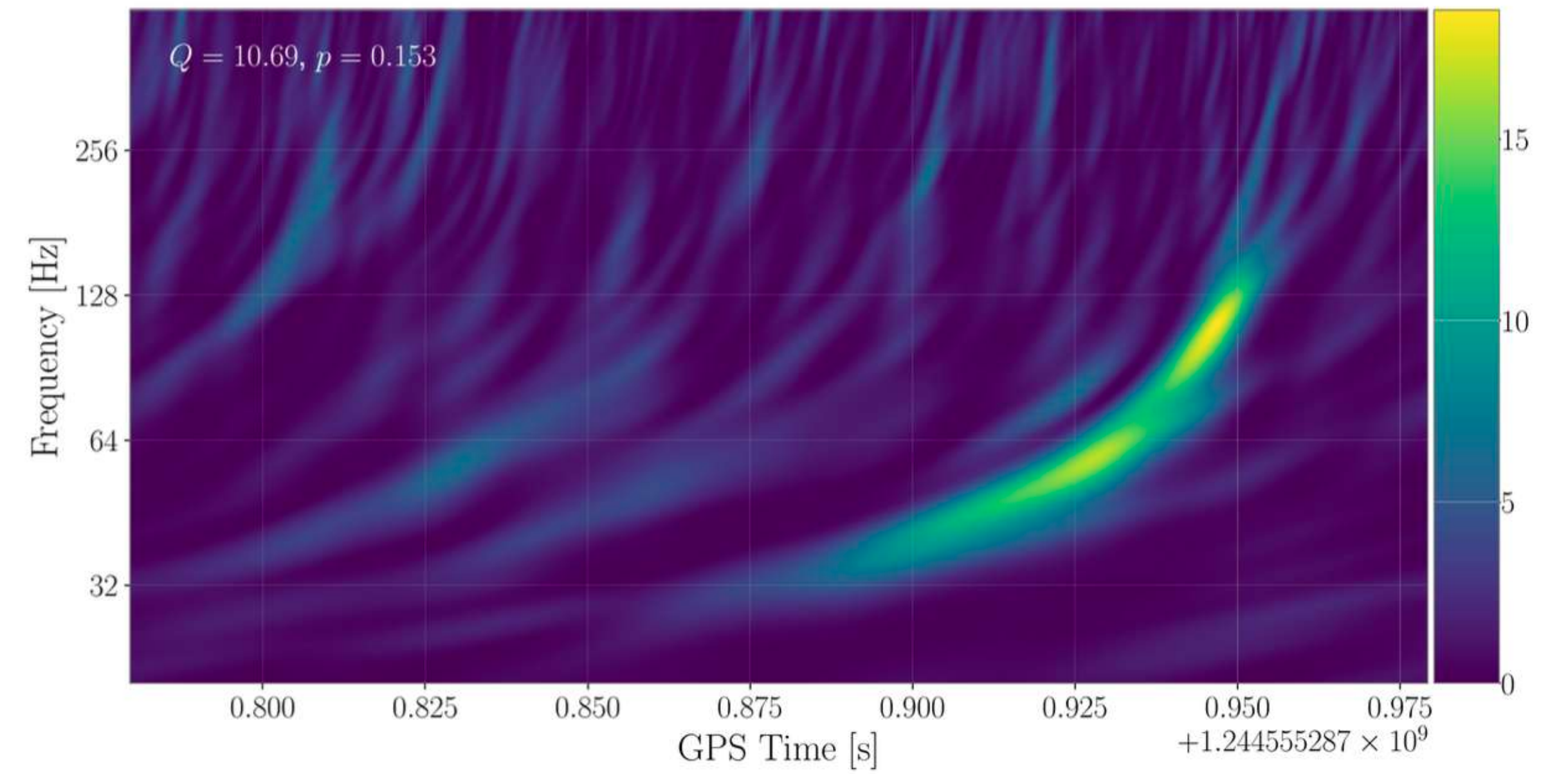
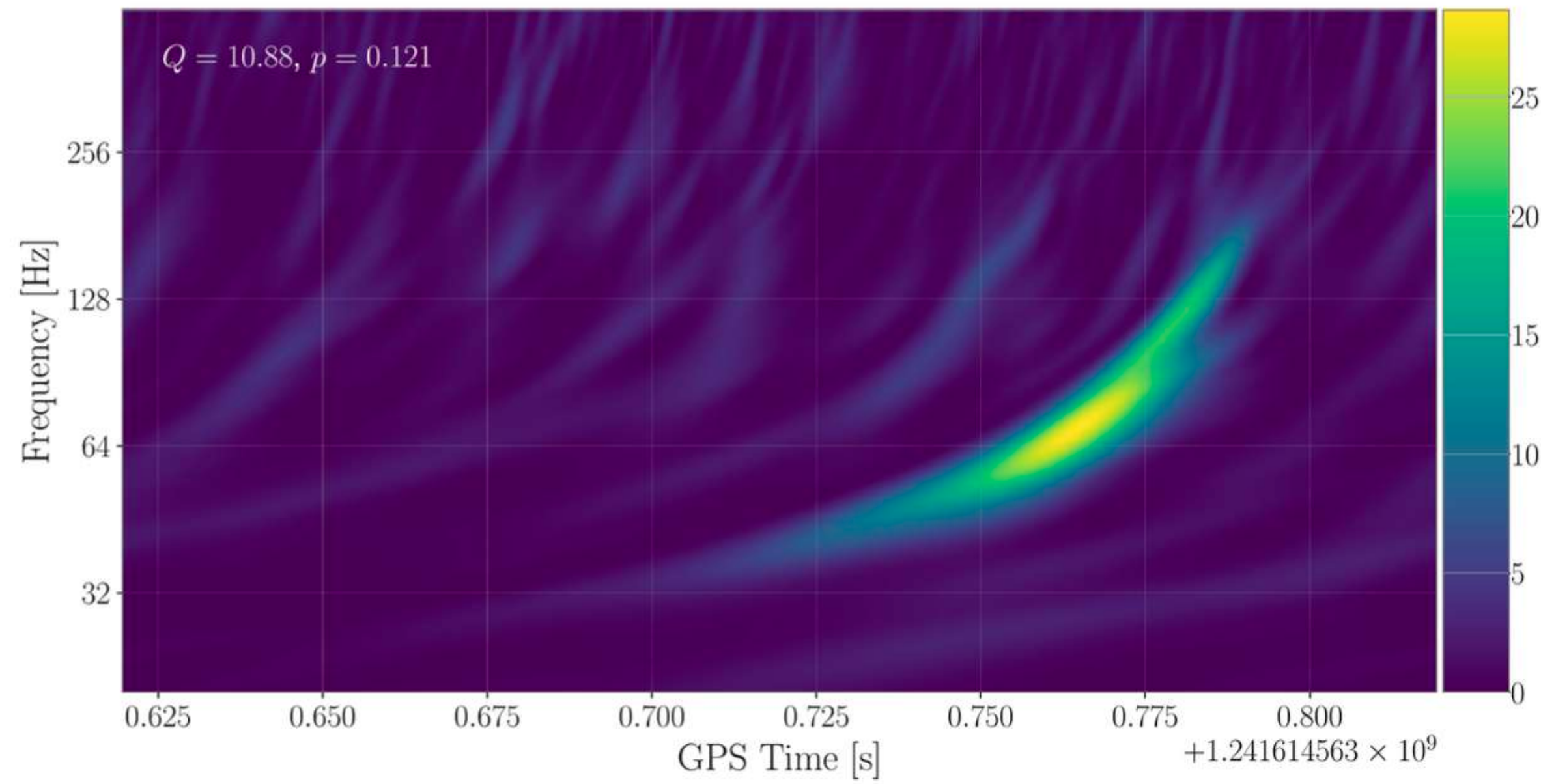
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TABLE VII: New candidate events identified by AresGW.

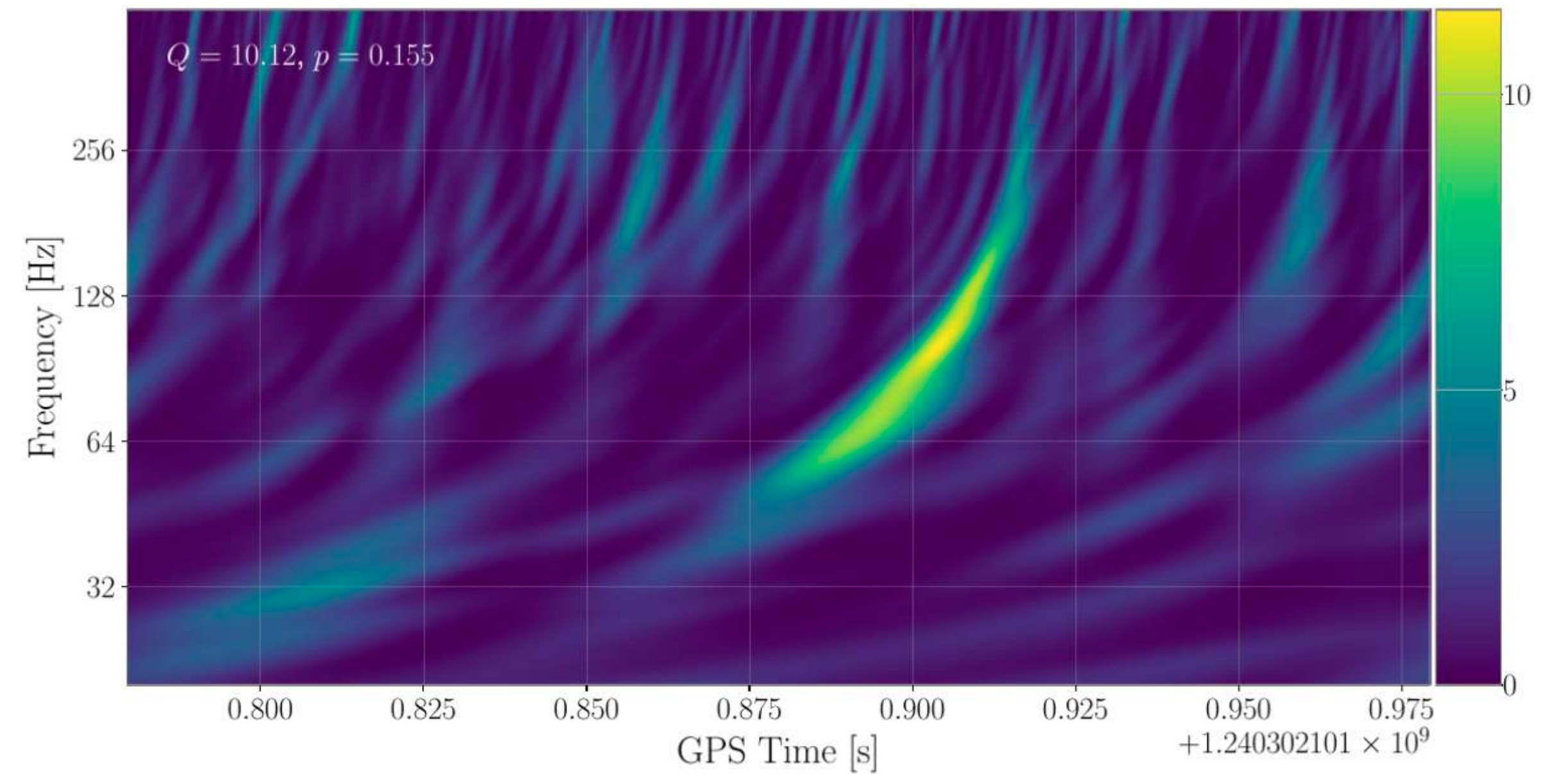
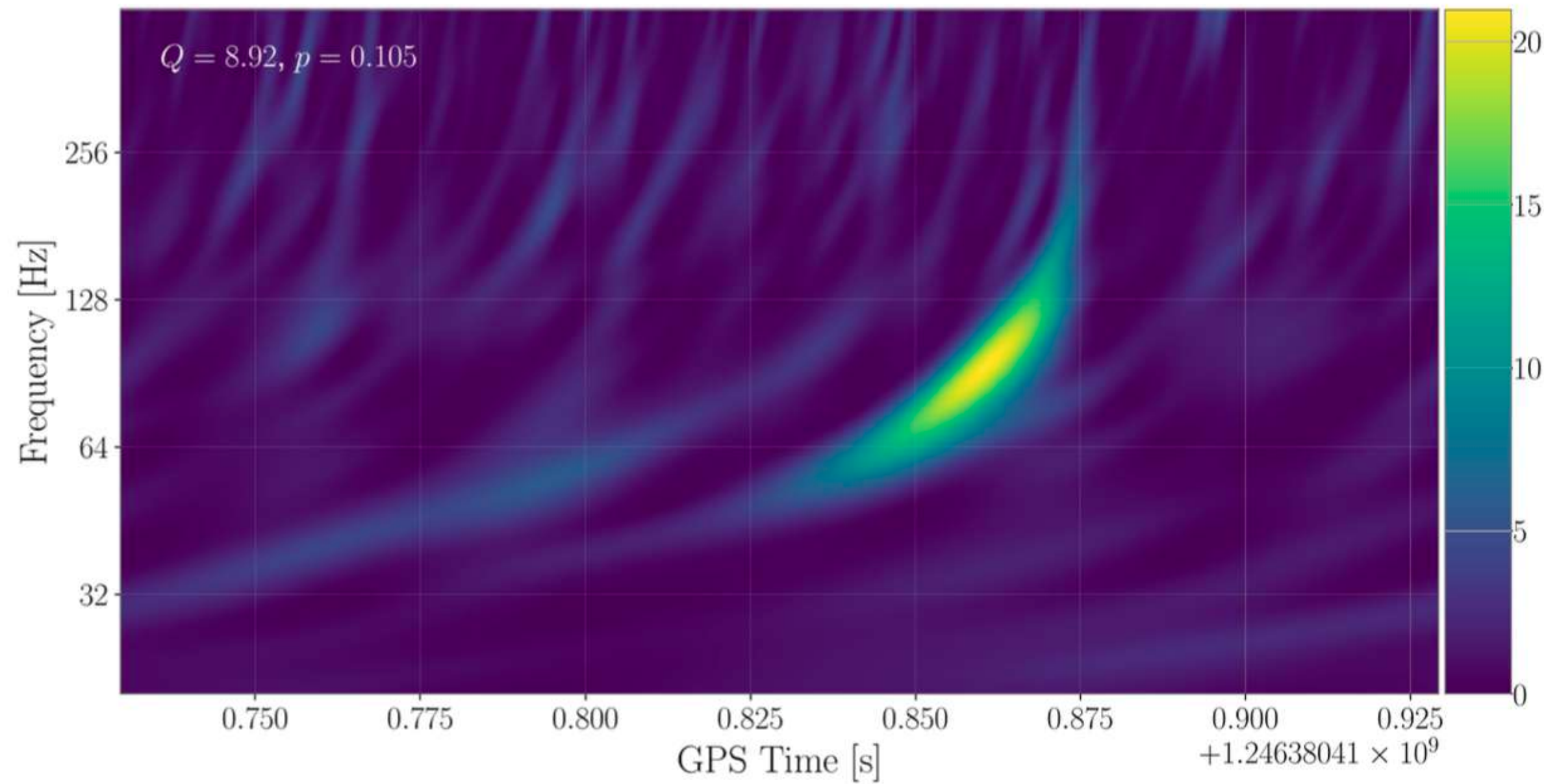
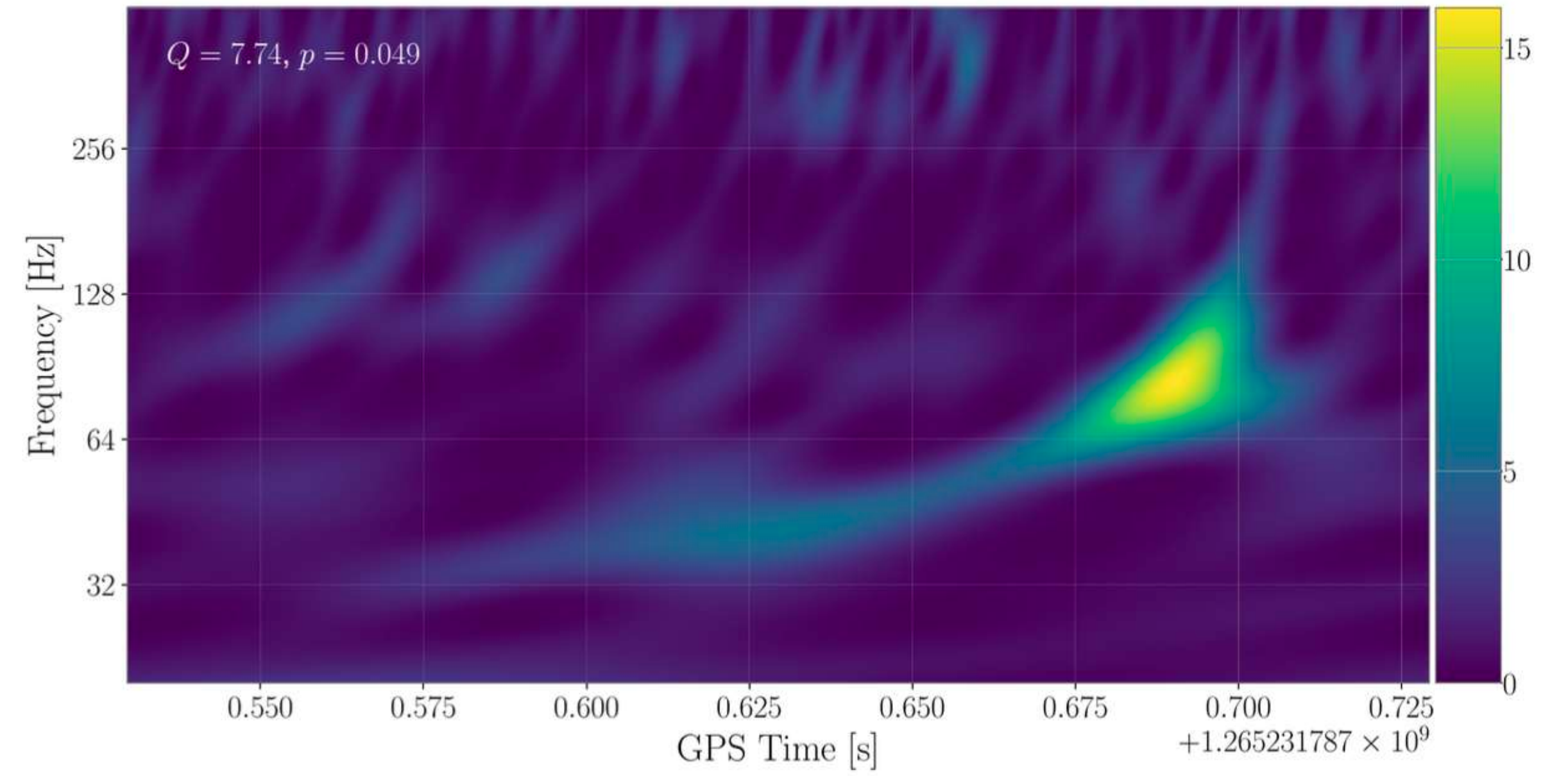
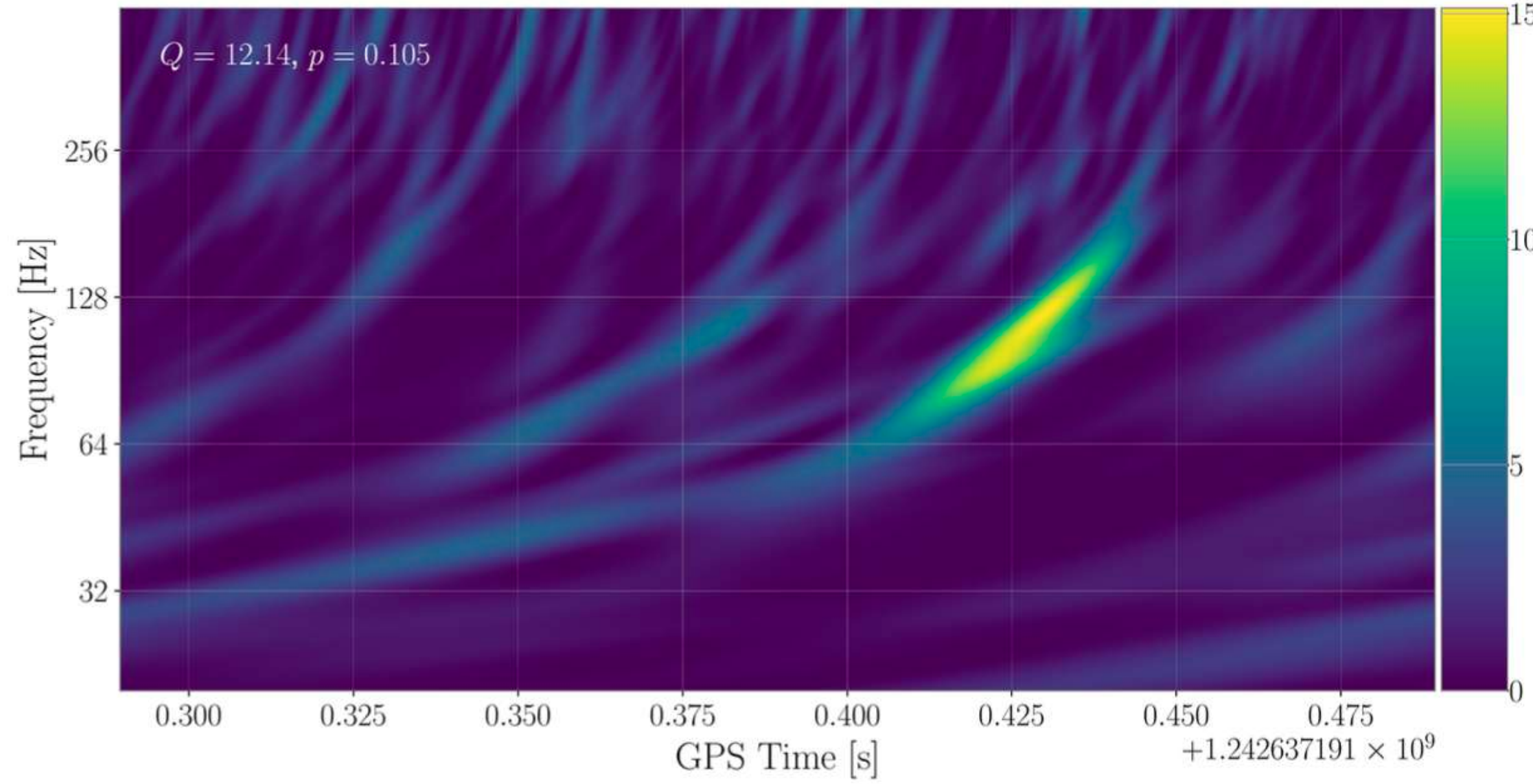
#	Event Name	GPS Time (s)	p_{astro}	FAR (1/yr)	$\langle \mathcal{R}_s \rangle$	Time delay	χ^2_{red}	ρ	Class
1	GW190511_125545	1241614563.77	1.00	1	3.95	0.0000	0.90	0.80	Selective Passband
2	GW190614_134740	1242637191.44	0.72	14	4.35	0.0002	0.38	0.71	Selective Passband
3	GW190607_085538	1242637191.44	0.68	20	6.60	0.0054	0.75	1.39	Selective Noise Rejection
4	GW190904_105351	1265231787.68	0.55	18	4.0	0.0063	0.69	0.98	Selective Passband
5	GW190523_085353	1242637191.44	0.68	20	6.60	0.0054	0.75	1.39	Selective Noise Rejection
6	GW200208_211609	1265231787.68	0.55	18	4.0	0.0063	0.69	0.98	Selective Passband
7	GW190705_164632	1246380410.88	0.51	49	5.82	0.0103	1.05	0.98	Default Low-Pass*
8	GW190426_082124	1240302101.93	0.50	20	3.91	0.0007	1.48	0.53	Selective Passband

First coincident GW events identified using a machine-learning algorithm

ARESGW NEW CANDIDATE EVENTS



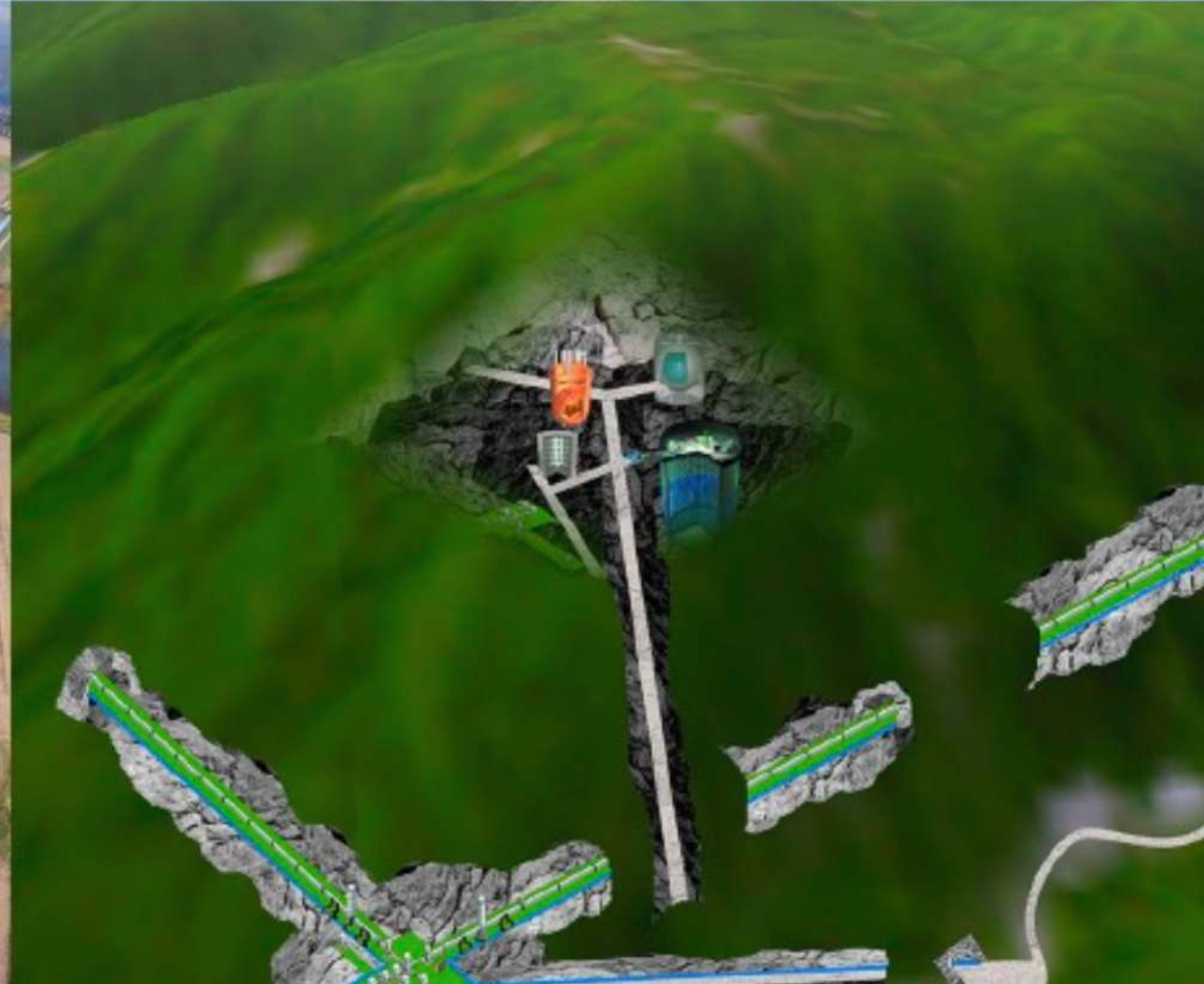
ARESGW NEW CANDIDATE EVENTS



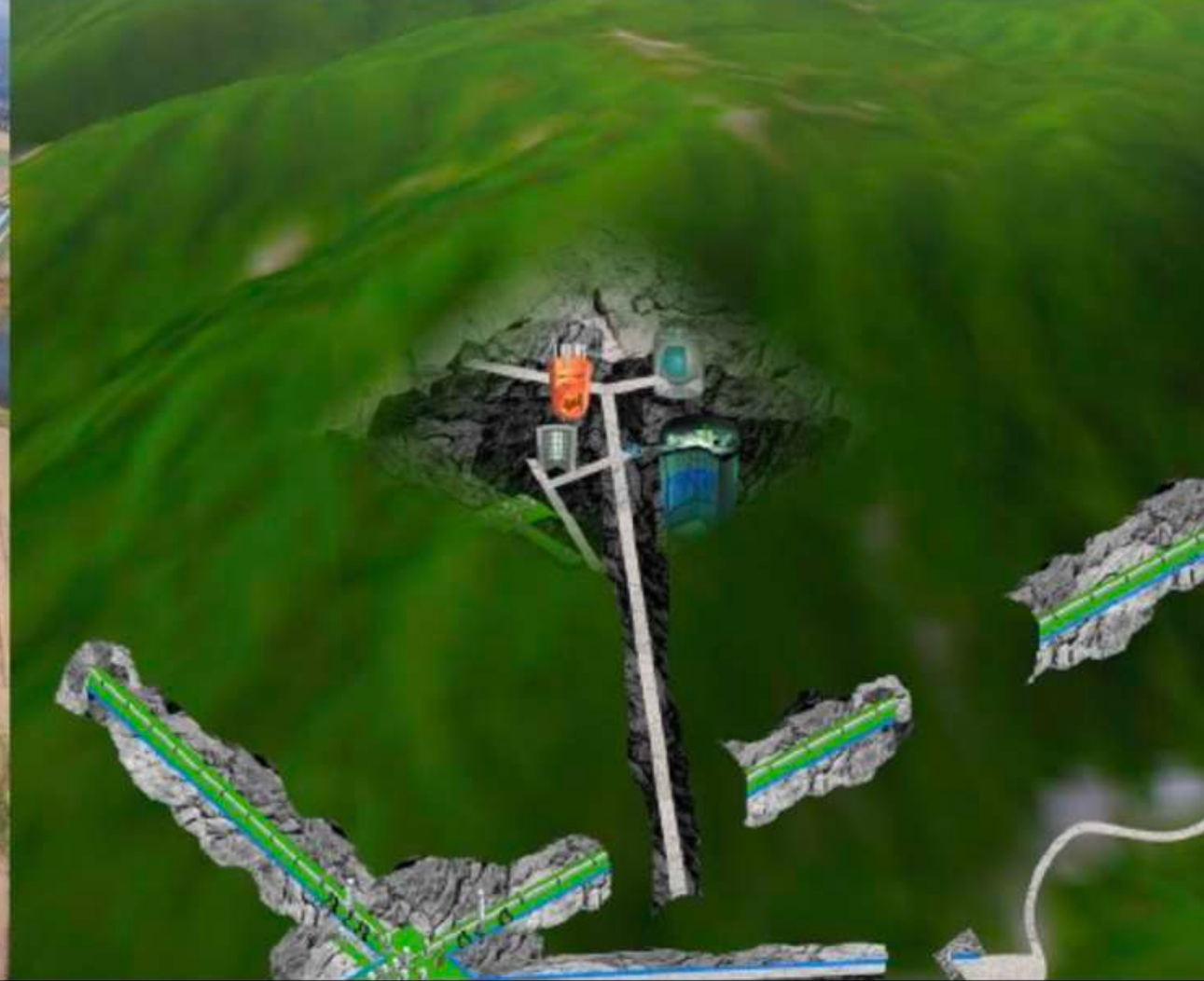
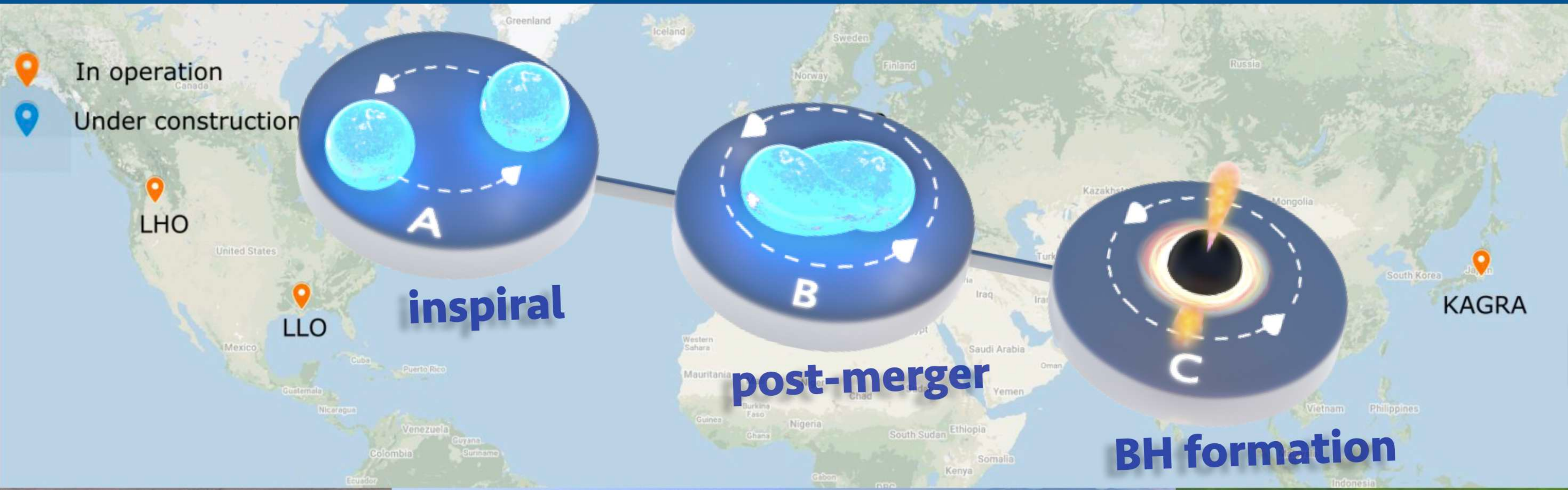
PART B.

BINARY NEUTRON STAR POST-MERGER PHASE

INTERNATIONAL GRAVITATIONAL-WAVE OBSERVATORY NETWORK (IGWN)

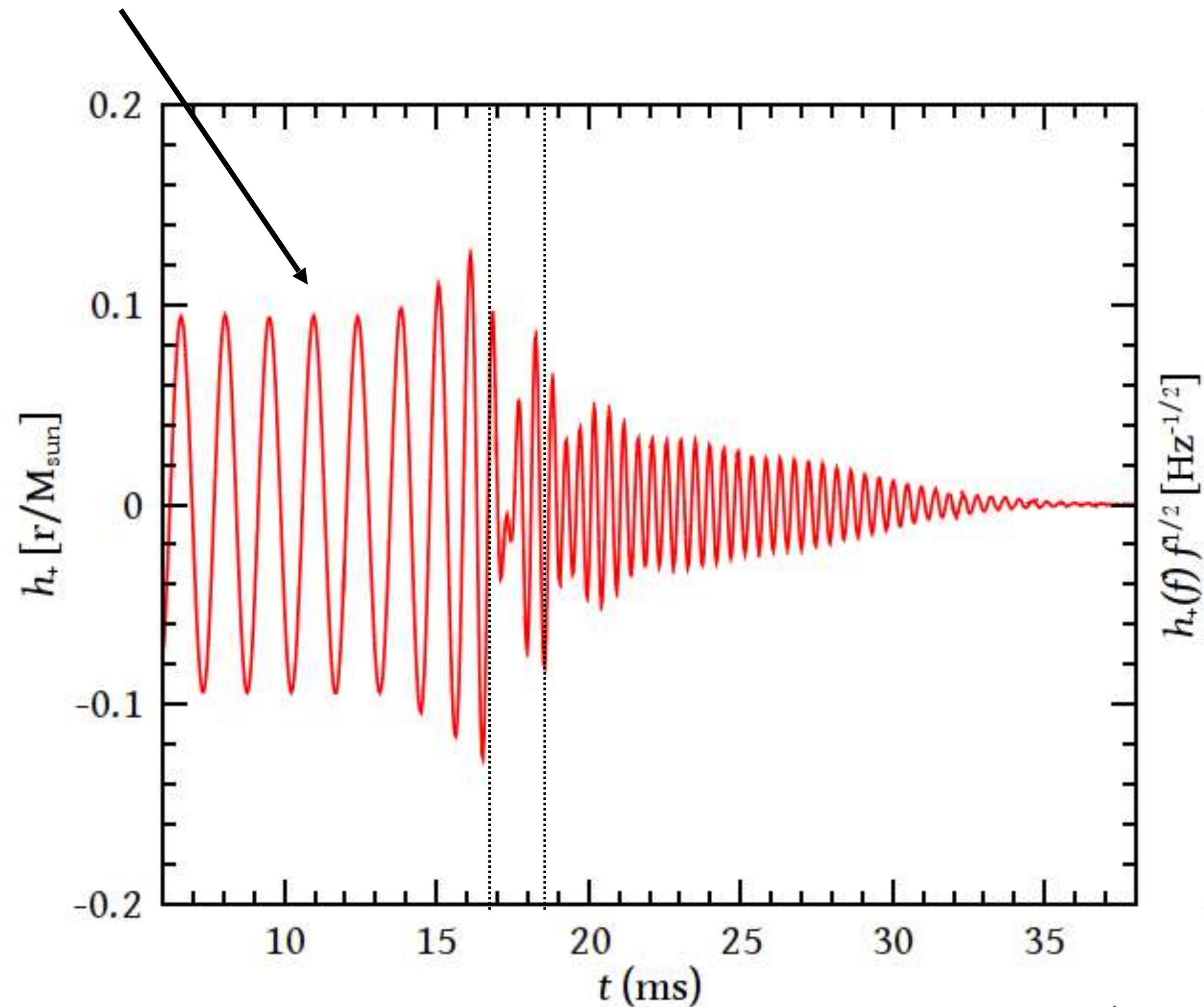


INTERNATIONAL GRAVITATIONAL-WAVE OBSERVATORY NETWORK (IGWN)



POST-MERGER PHASE IN BNS MERGERS

Time domain: three distinct phases of the GW signal:
inspiral, *merger* and *post-merger oscillations*.

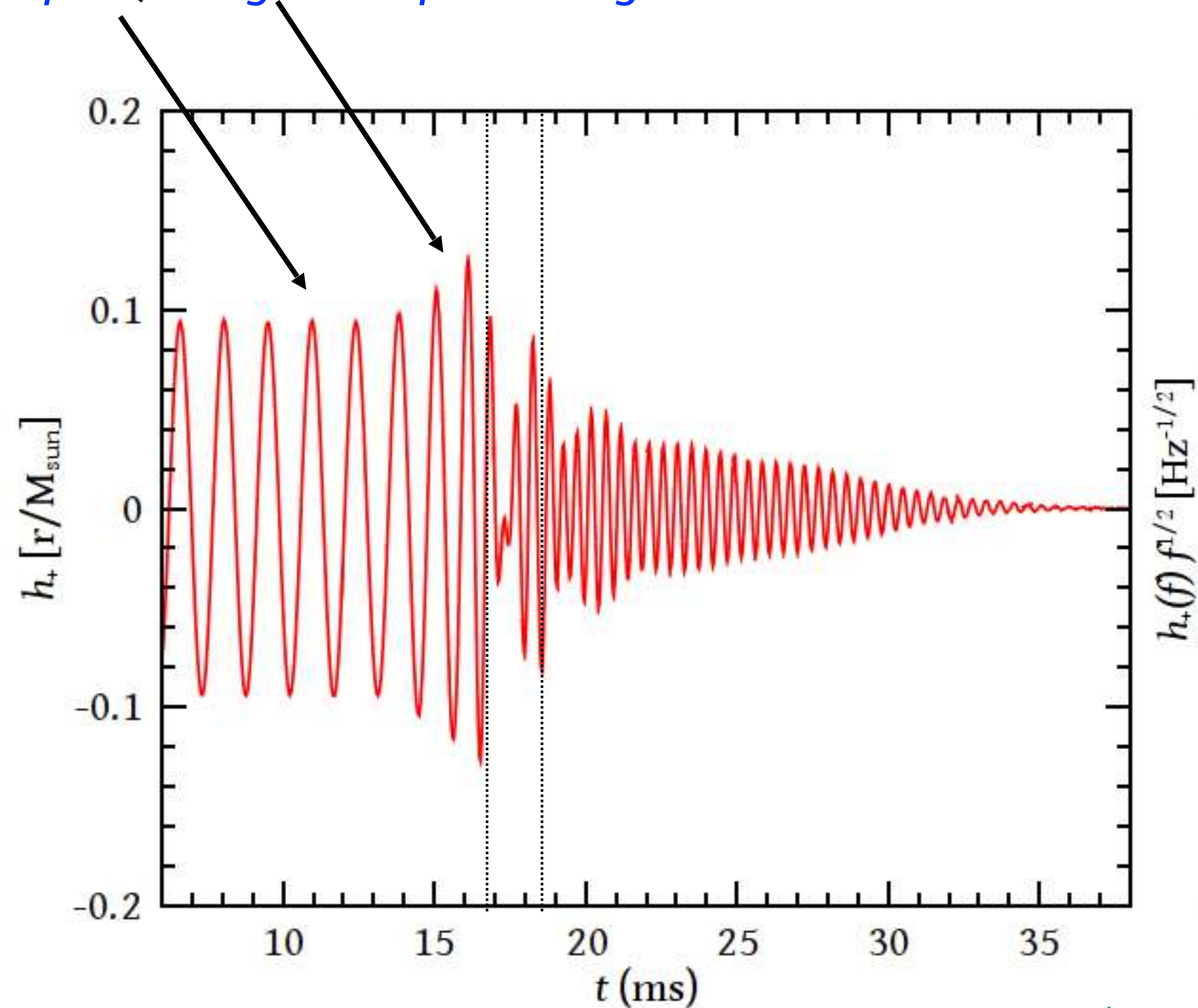


Stergioulas et al. (2011)

POST-MERGER PHASE IN BNS MERGERS

Time domain: three distinct phases of the GW signal:

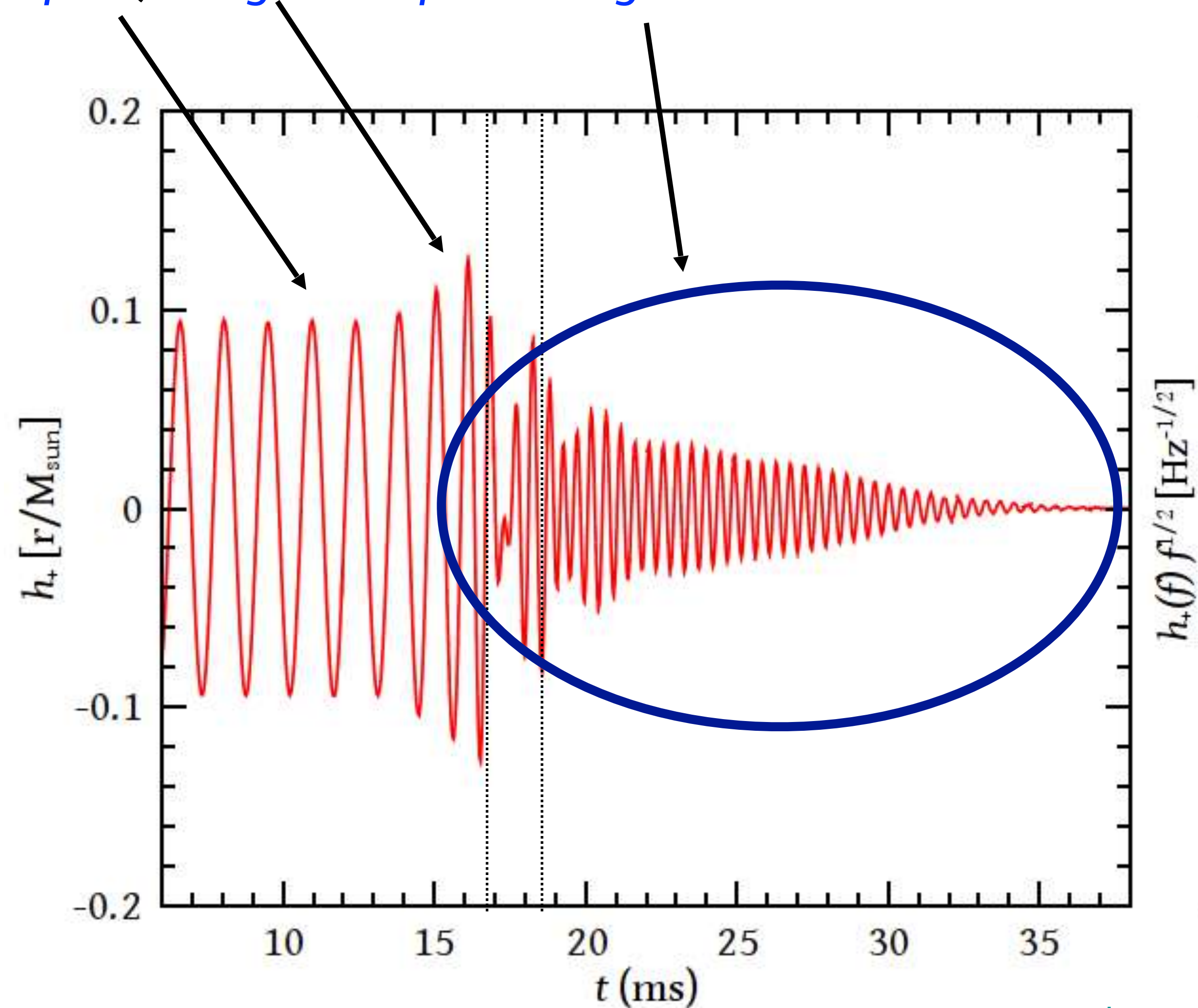
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Stergioulas et al. (2011)

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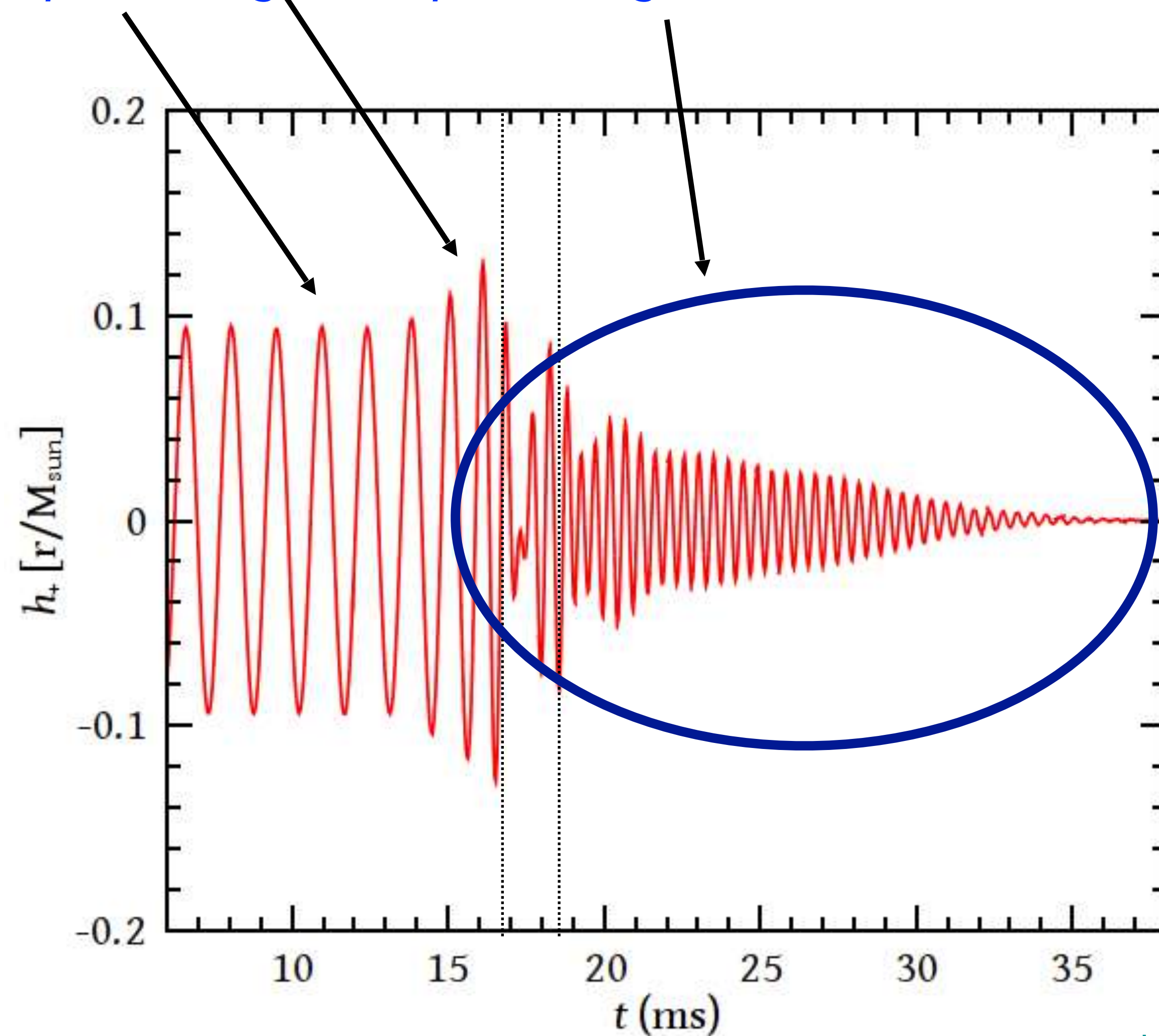


Stergioulas et al. (2011)

POST-MERGER PHASE IN BNS MERGERS

Time domain: three distinct phases of the GW signal:

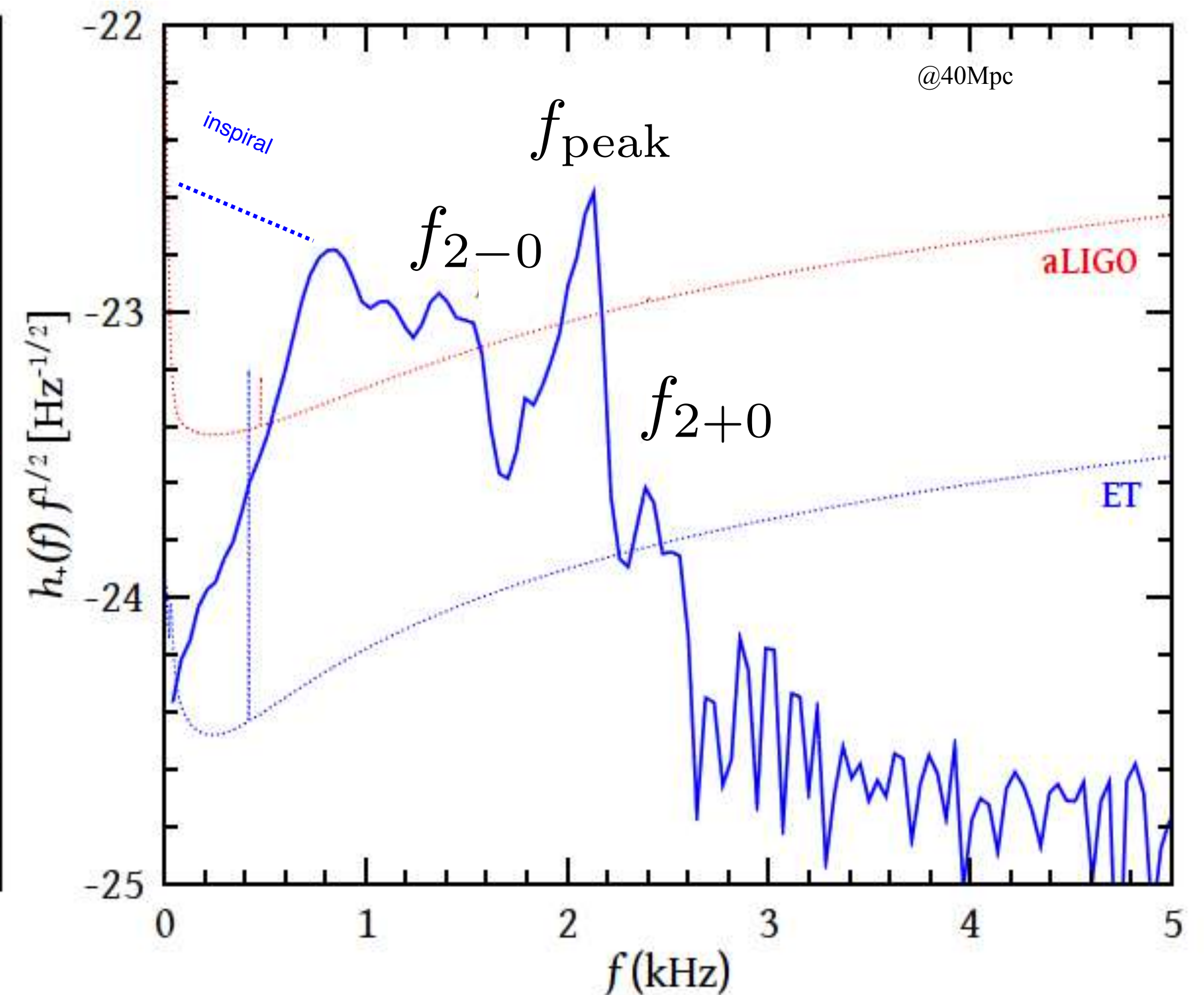
inspiral, *merger* and *post-merger oscillations*.



Frequency domain:

f_{peak} : $l=m=2$ fundamental mode.

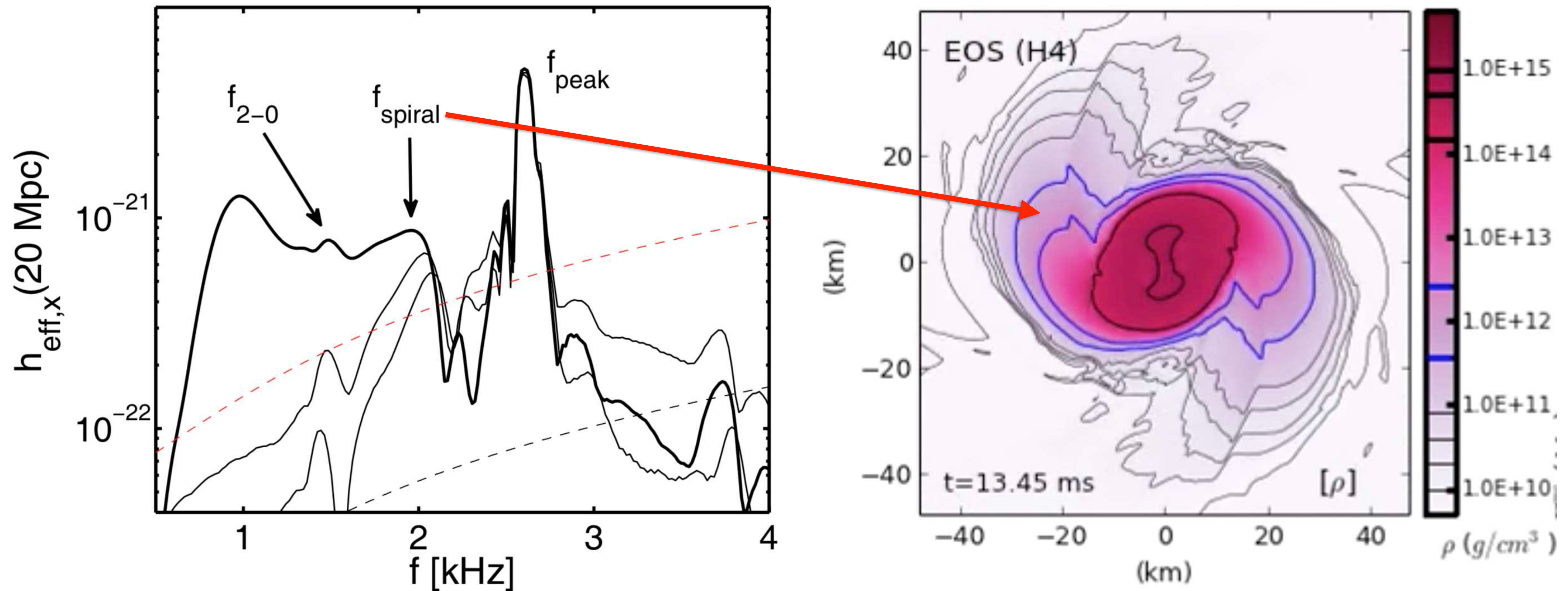
f_{2-0}, f_{2+0} : *nonlinear combination tones*



Stergioulas et al. (2011)

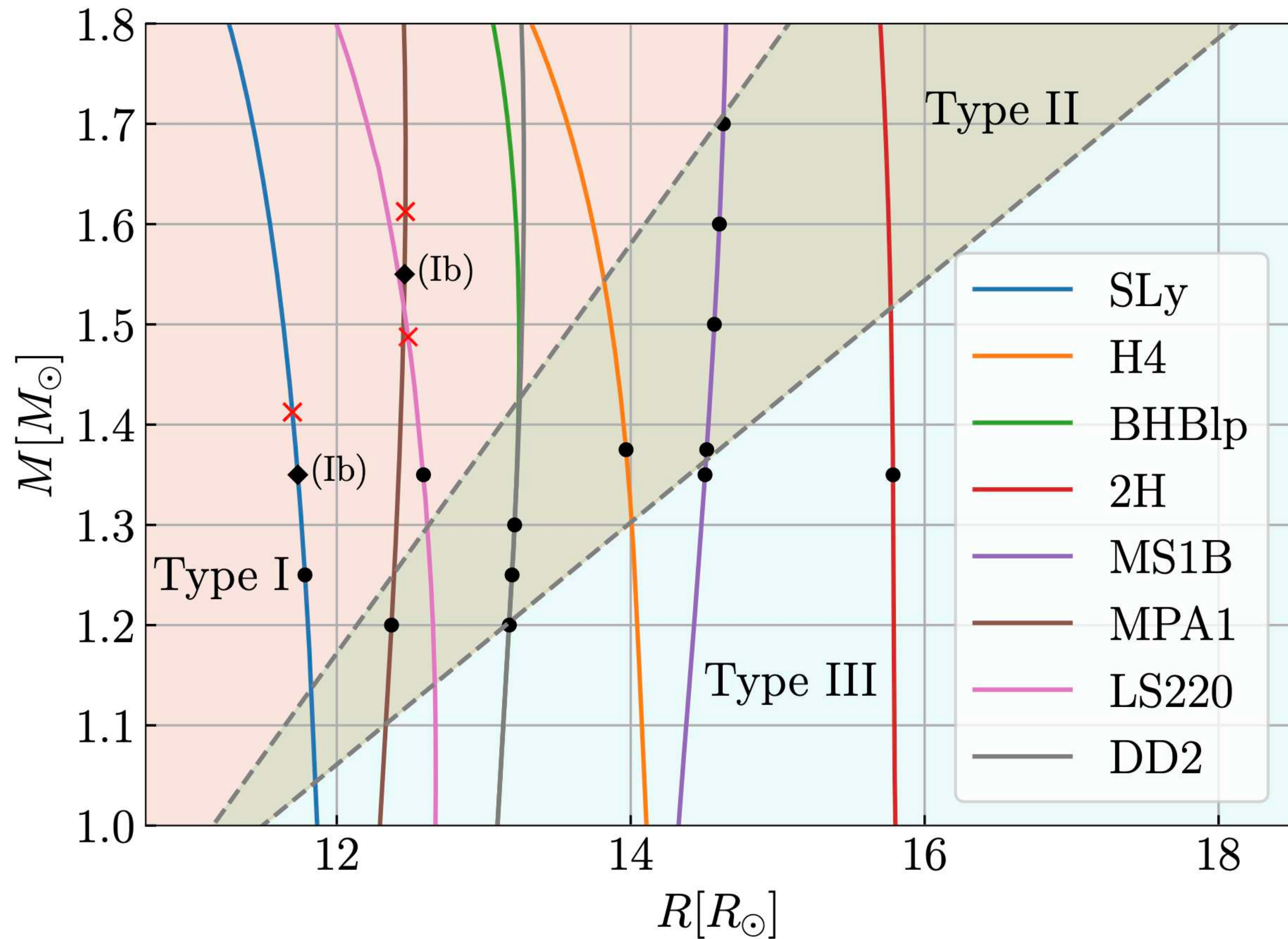
POST-MERGER PHASE IN BNS MERGERS

Orbiting spiral arms also lead to a distinct frequency f_{spiral}



Bauswein & Stergioulas (2015)

CLASSIFICATION OF POST-MERGER WAVEFORMS



Bauswein & Stergioulas (2015)

Vretinaris, Bauswein & Stergioulas (2020)

Type I:

f_{2-0} stronger than f_{spiral}

Type II:

f_{2-0} comparable to f_{spiral}

Type III:

f_{spiral} stronger than f_{2-0}

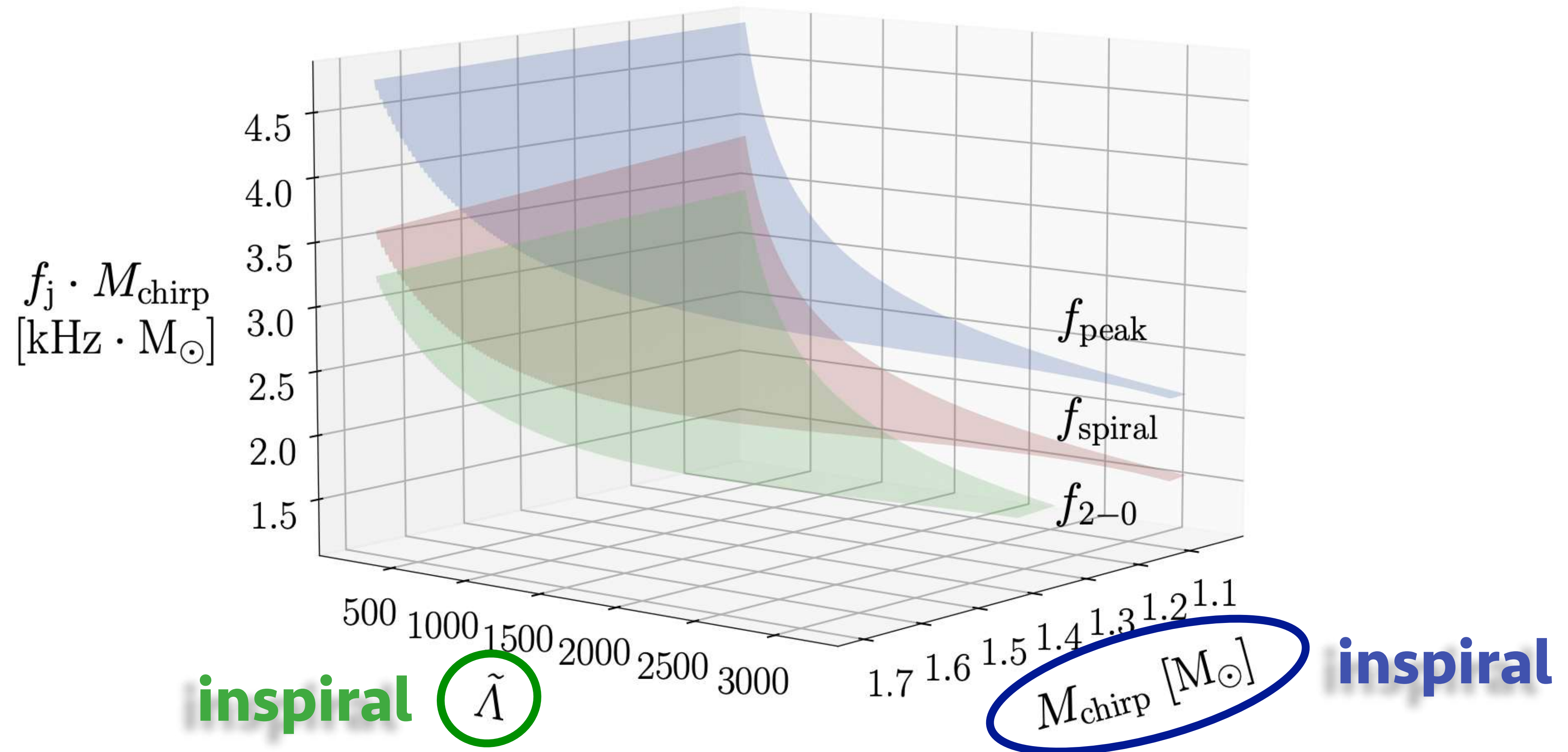
Type Ib:

(close to M_{thres})

Vretinaris et al. (2025)

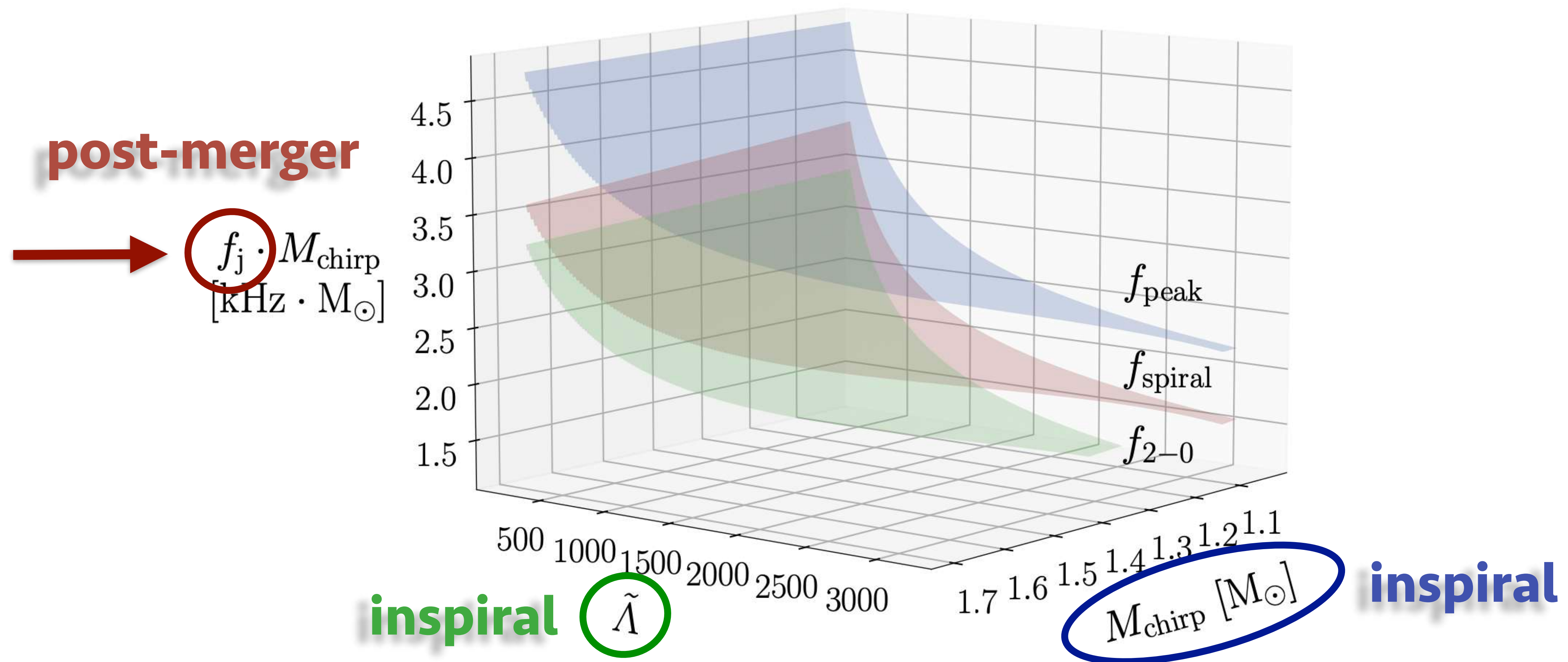
EMPIRICAL RELATIONS OF POST-MERGER FREQUENCIES

$$\begin{aligned} f_{\text{peak}} M_{\text{chirp}} &= 1.392 - 0.108 M_{\text{chirp}} + 51.70 \tilde{\Lambda}^{-1/2} && \text{Vretinaris, Bauswein \& Stergioulas (2020)} \\ f_{2-0} M_{\text{chirp}} &= 0.558 - 0.406 M_{\text{chirp}} + 48.696 \tilde{\Lambda}^{-1/2} && \text{Vretinaris et al. (2025)} \\ f_{\text{spiral}} M_{\text{chirp}} &= 1.2 - 0.442 M_{\text{chirp}} + 45.819 \tilde{\Lambda}^{-1/2} && \text{Vretinaris et al. (2025)} \end{aligned}$$



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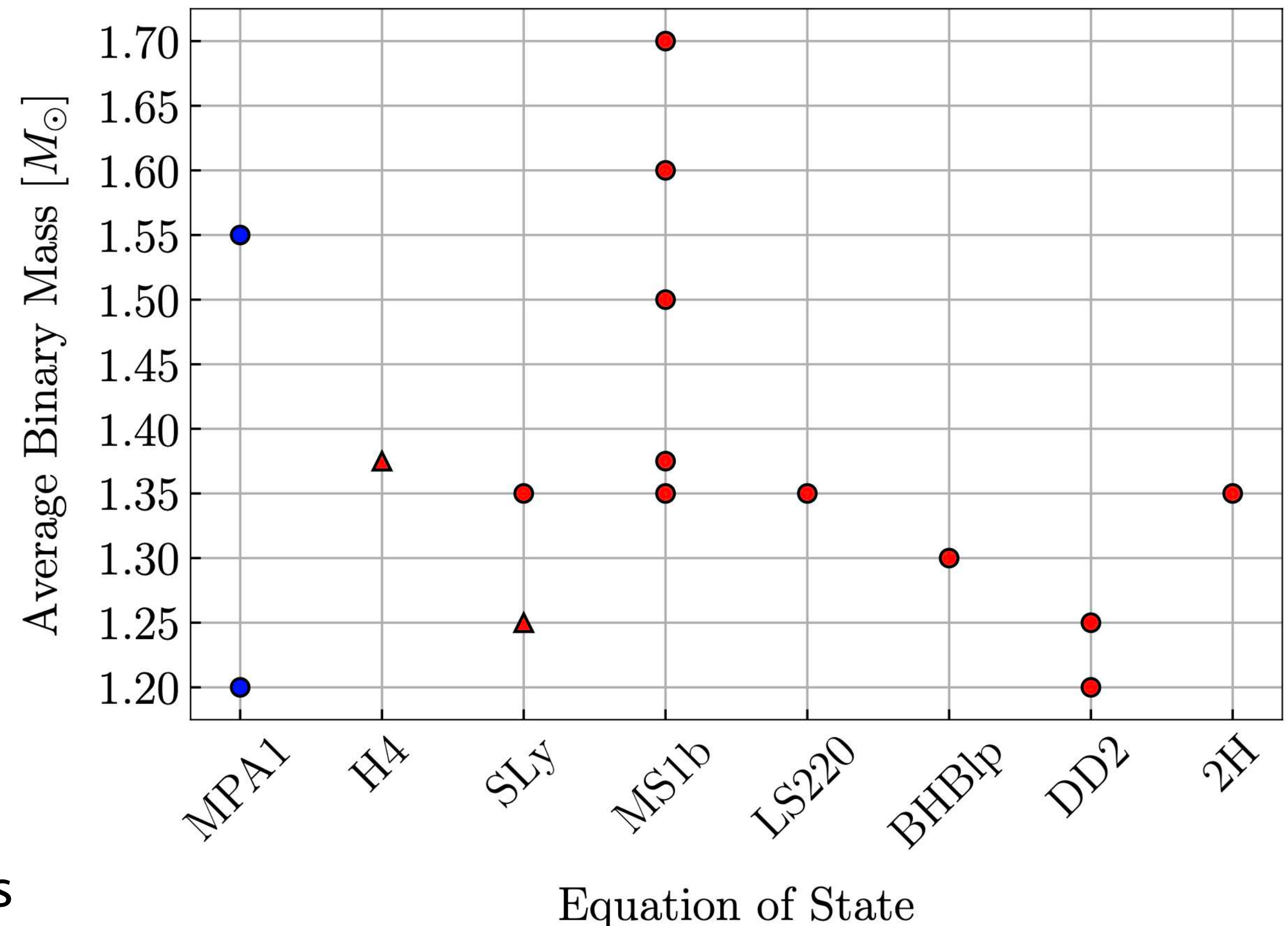
ACCELERATION OF POST-MERGER INFERENCE

13 numerical waveforms from the CoRe database (Gonzalez et al. 2022)

+2 numerical waveforms from Souldanis, Bauswein & Stergioulas (2022)

Label	EOS	q	(Average) Mass	References
THC:0036:R03	SLy	1.0	1.350	[47]
THC:0019:R05	LS220	1.0	1.350	[101, 102]
BAM:0088:R01	MS1b	1.0	1.500	[99, 100]
THC:0002:R01	BHBlp	1.0	1.300	[101, 102]
THC:0011:R01	DD2	1.0	1.250	[101, 102]
BAM:0070:R01	MS1b	1.0	1.375	[103]
BAM:0065:R03	MS1b	1.0	1.350	[104]
THC:0010:R01	DD2	1.0	1.200	[101, 102]
BAM:0002:R02	2H	1.0	1.350	[104]
BAM:0053:R01	H4	1.5	1.375	[105]
BAM:0124:R01	SLy	1.5	1.250	[103]
BAM:0090:R02	MS1b	1.0	1.600	[99, 100]
BAM:0092:R02	MS1b	1.0	1.700	[99, 100]
Souldanis et al.	MPA1	1.0	1.200	[67]
Souldanis et al.	MPA1	1.0	1.550	[67]

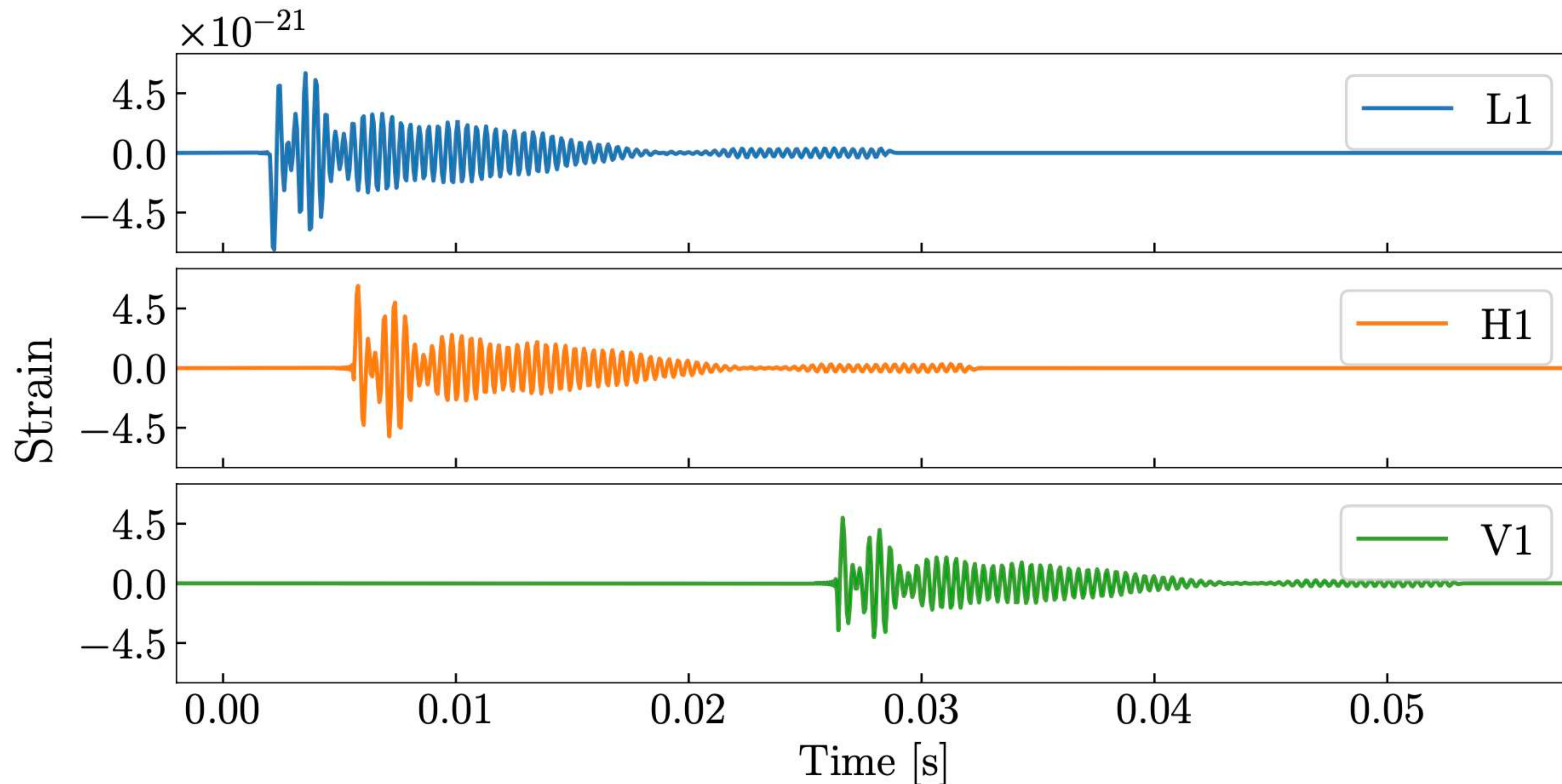
Extension of the set of 9 waveforms used in previous work by Easter et al. (2020)



INJECTIONS IN 3-DETECTOR NETWORK

Waveforms are injected in 3-detector HLV network at design sensitivity, using BILBY (Ashton et al. 2019)

We choose post-merger SNR of 8, 16 and 50, to simulate detection by 3G network (ET/CE) at distances as close as 200Mpc.



Several analytic models exist in the time- and frequency-domains.

Here, we extend the analytic model of Easter et al. (2020) as follows:

$$\begin{aligned} h(\boldsymbol{\theta}, t) &= h_+(\boldsymbol{\theta}, t) - ih_\times(\boldsymbol{\theta}, t) \\ &= \sum_{j=1}^4 [h_{j,+}(\boldsymbol{\theta}, t) - ih_{j,\times}(\boldsymbol{\theta}, t)] \\ h_{j,+}(\boldsymbol{\theta}, t) &= A_j \exp \left[-\frac{t}{T_j} \right] \cos [2\pi f_j t (1 + a_j t) + \psi_j] \end{aligned}$$

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Intrinsic parameters

$$\boldsymbol{\theta} = \{A_j, T_j, f_j, a_j, \psi_j\} \quad \text{for } j \in [1, 4]$$

$h_{j,\times}(\boldsymbol{\theta}, t)$ is obtained by applying a $\pi/2$ phase shift to $h_{j,+}(\boldsymbol{\theta}, t)$

- We have added a 4th oscillator at high frequencies $> f_{\text{peak}}$ (e.g. f_{2+0})
- Amplitudes A_j are free parameters

INFORMED PRIORS

In Easter et al. (2020) flat priors in a wide frequency range of 1-5 kHz for every oscillator were used.

- Here, we take advantage of the [empirical relations](#) to set [Gaussian priors](#) in a [narrow frequency range](#) around each expected frequency.
- In addition, the priors [differ](#), according to the [type of the post-merger](#) waveform:
 - Type I: Gaussian priors, $\mathcal{N}(f_{2-0}, \sigma^2)$ for f_{2-0} and uniform priors $\mathcal{U}(1, 5)$ [kHz] for f_{spiral} .
 - Type II: Gaussian priors, $\mathcal{N}(f_{2-0}, \sigma^2)$ for f_{2-0} and $\mathcal{N}(f_{\text{spiral}}, \sigma^2)$ for f_{spiral} .
 - Type III: Gaussian priors, $\mathcal{N}(f_{\text{spiral}}, \sigma^2)$ for f_{spiral} and uniform priors $\mathcal{U}(1, 5)$ [kHz] for f_{2-0} .

where $\sigma = 3 \times \text{max error of empirical relations}$. For f_{peak} : Gaussian ; for f_4 : flat in $[f_{\text{peak}} + 0.3\text{kHz}, 5\text{kHz}]$.

priors for A_j : uniform in $[-24, -19]$

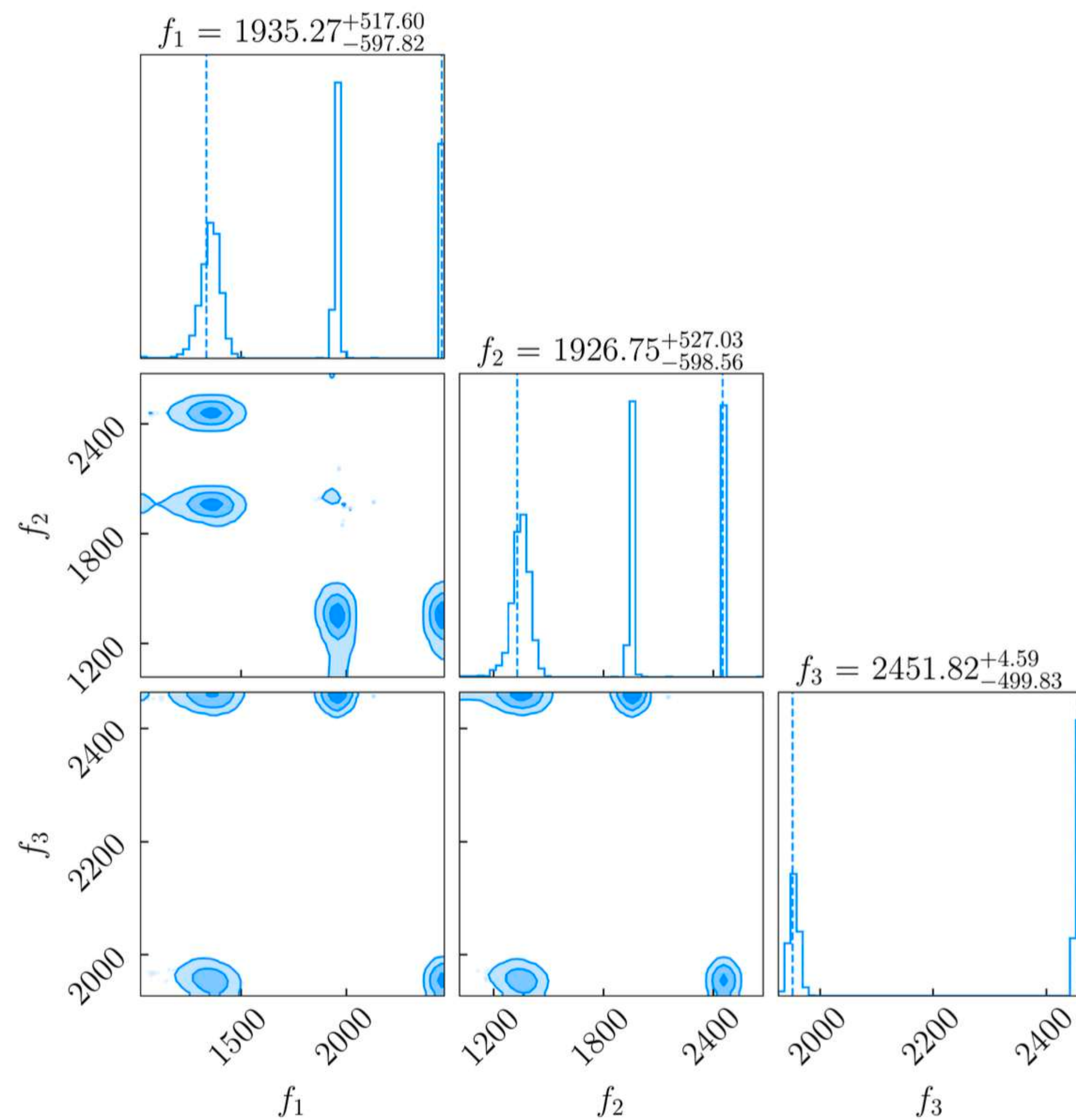
priors for a_j : uniform in $[-6.4, 6.4]$

priors for remaining parameters: as in Easter et al. (2020)

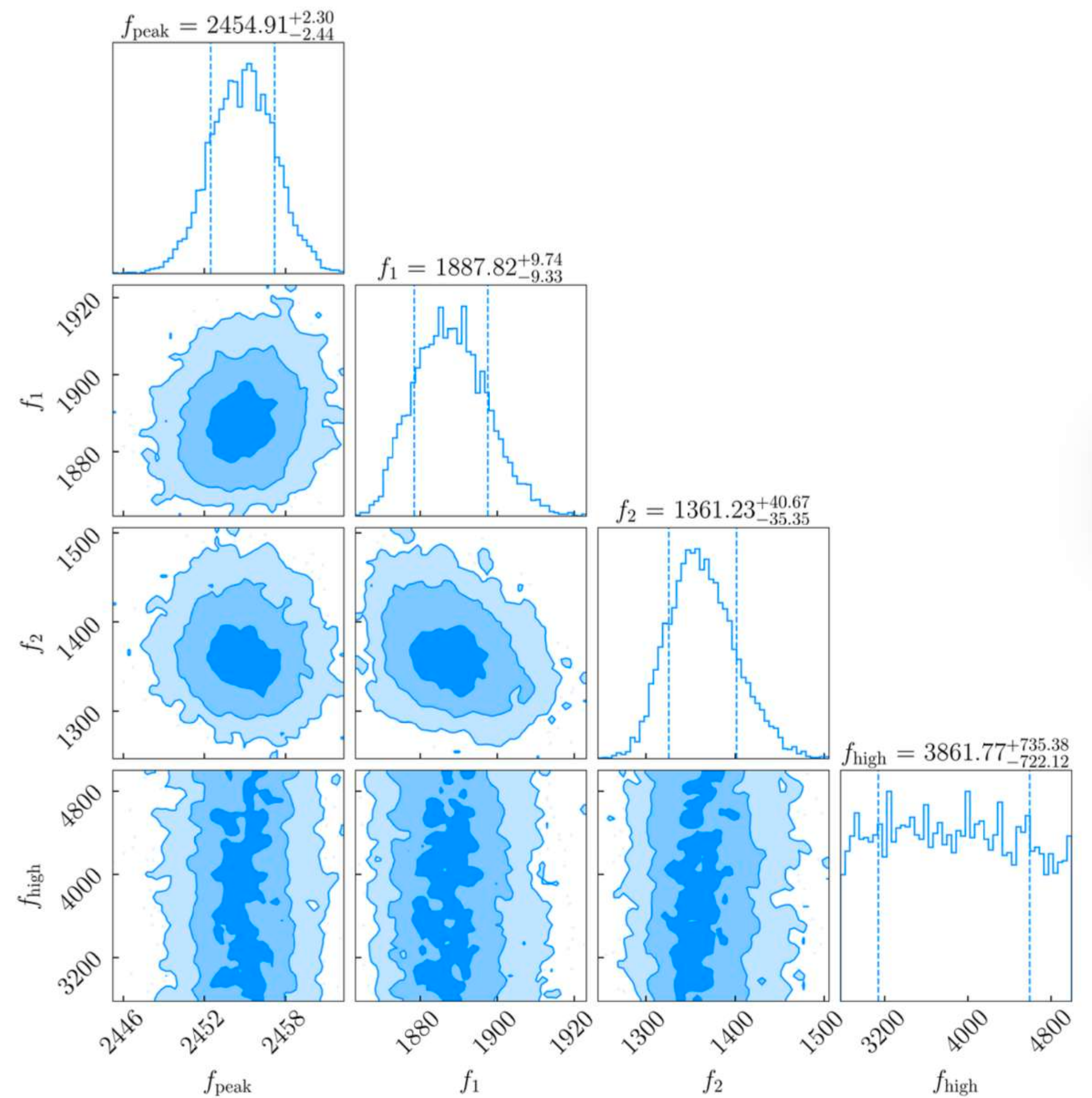
POSTERIOR DISTRIBUTIONS

EOS BHBlp 1.3+1.3, SNR = 50

using flat priors



using informed priors (through empirical relations)

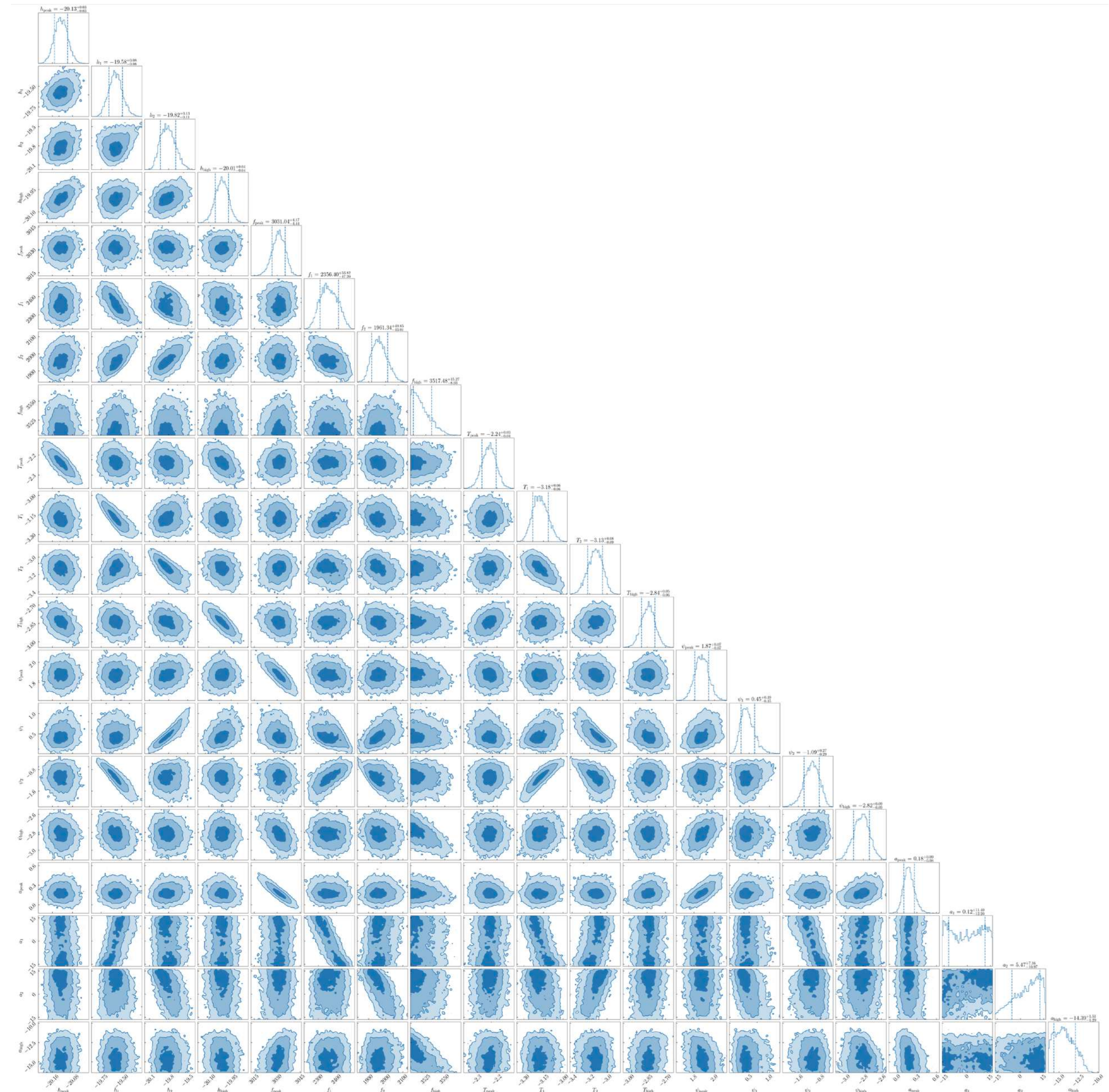


POSTERIOR DISTRIBUTIONS

EOS MPA 1.55+1.55, SNR = 50

using informed priors

all parameters



POCOMC: PRECONDITIONED MONTE CARLO SAMPLER

Sequential Monte Carlo + Normalizing Flow Preconditioning:

= **Preconditioned Monte Carlo Sampling** (Karamanis et al. 2022)

PMC targets an **annealed version of the posterior**, with density given by

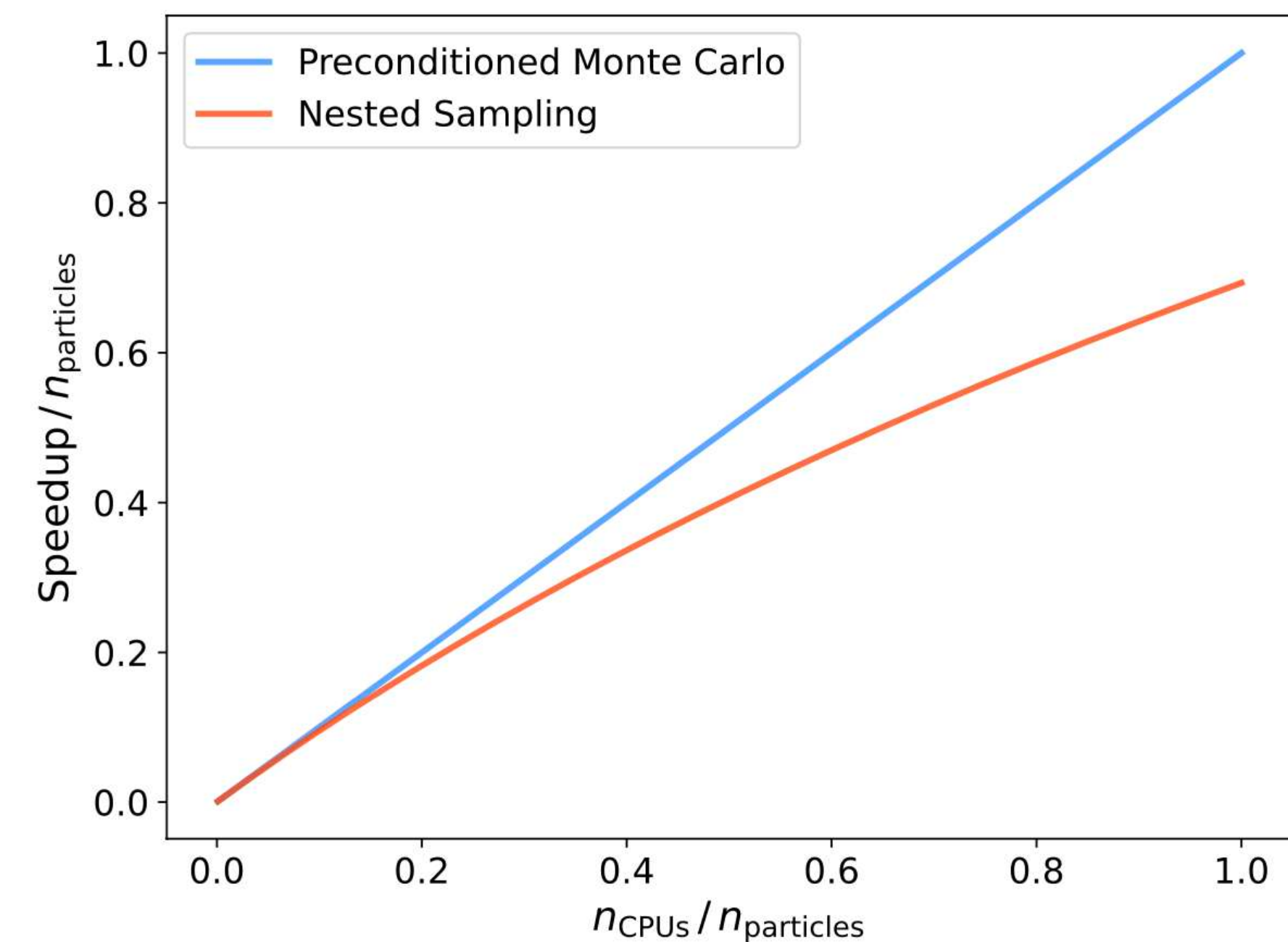
$$p_t(\boldsymbol{\theta} \mid d) \propto \mathcal{L}^{\beta_t}(\boldsymbol{\theta} \mid d)\pi(\boldsymbol{\theta})$$

where β_t a parameter (inverse temperature).

We use 2000 particles that **transition from the prior ($\beta_0 = 0$) to the posterior distribution ($\beta_T = 1$)**, through a sequence of reweighing, resampling and mutation steps.

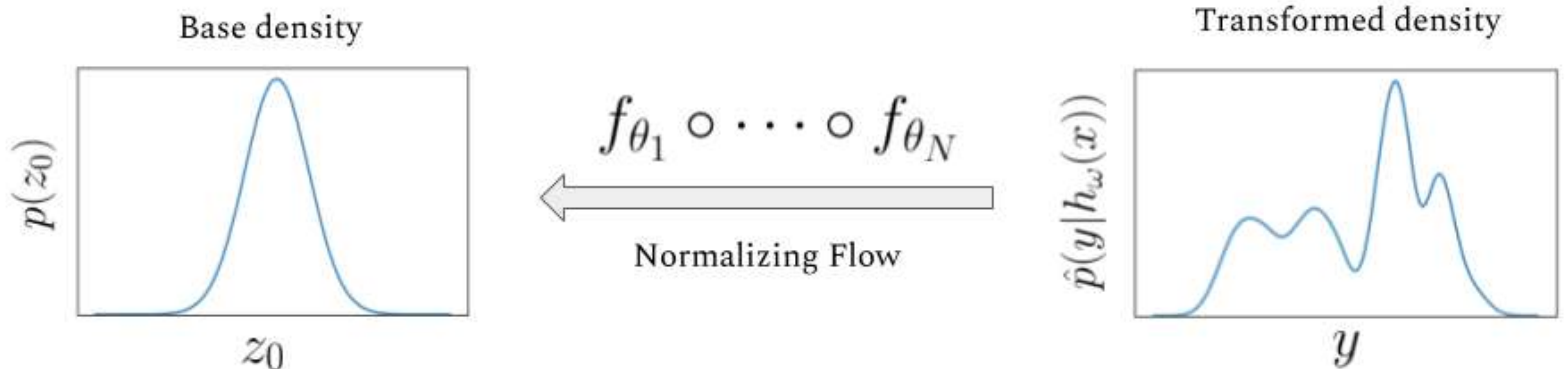
pocomc

<https://github.com/minaskar/pocomc>



PocoMC is highly parallelizable

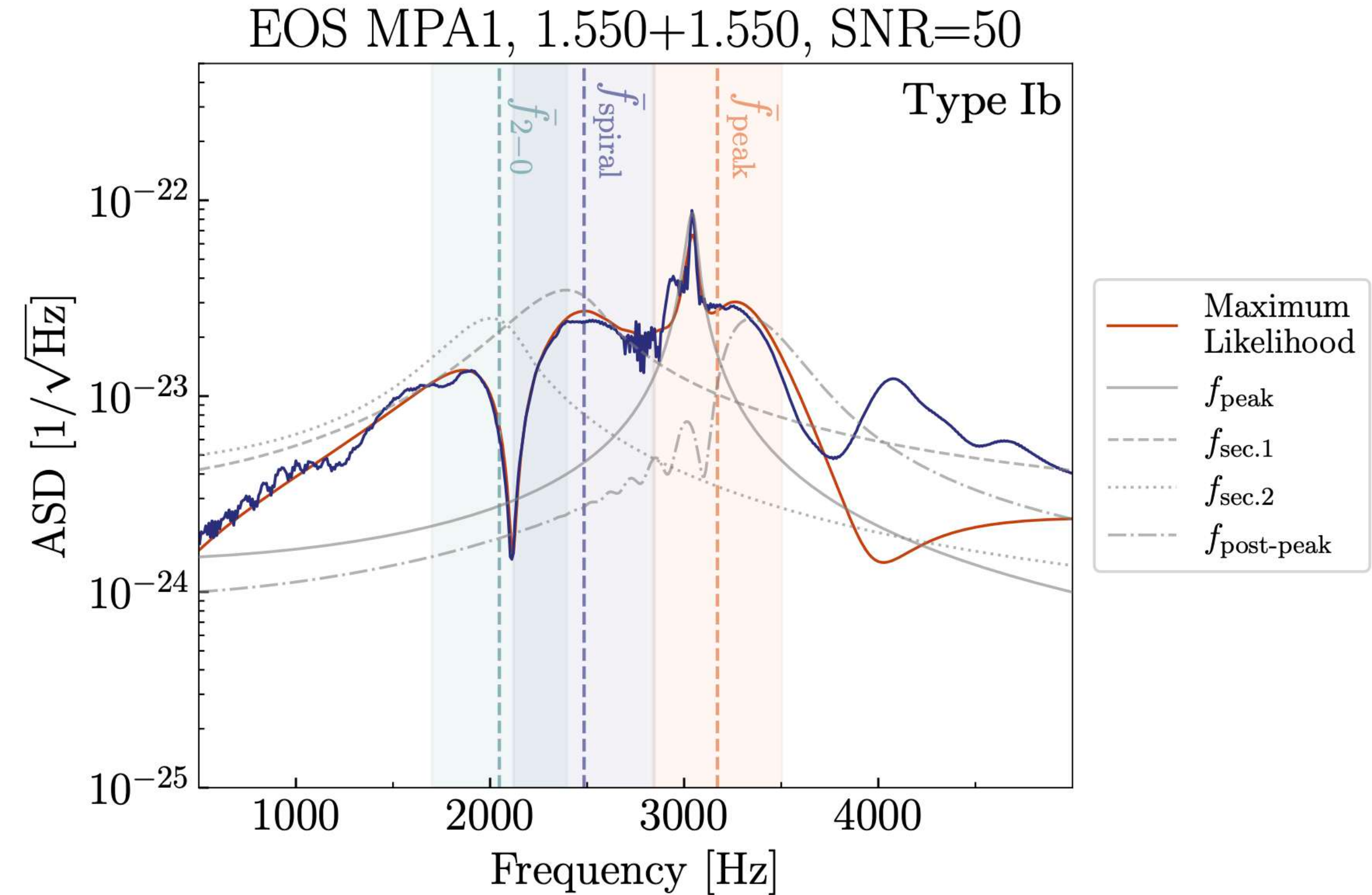
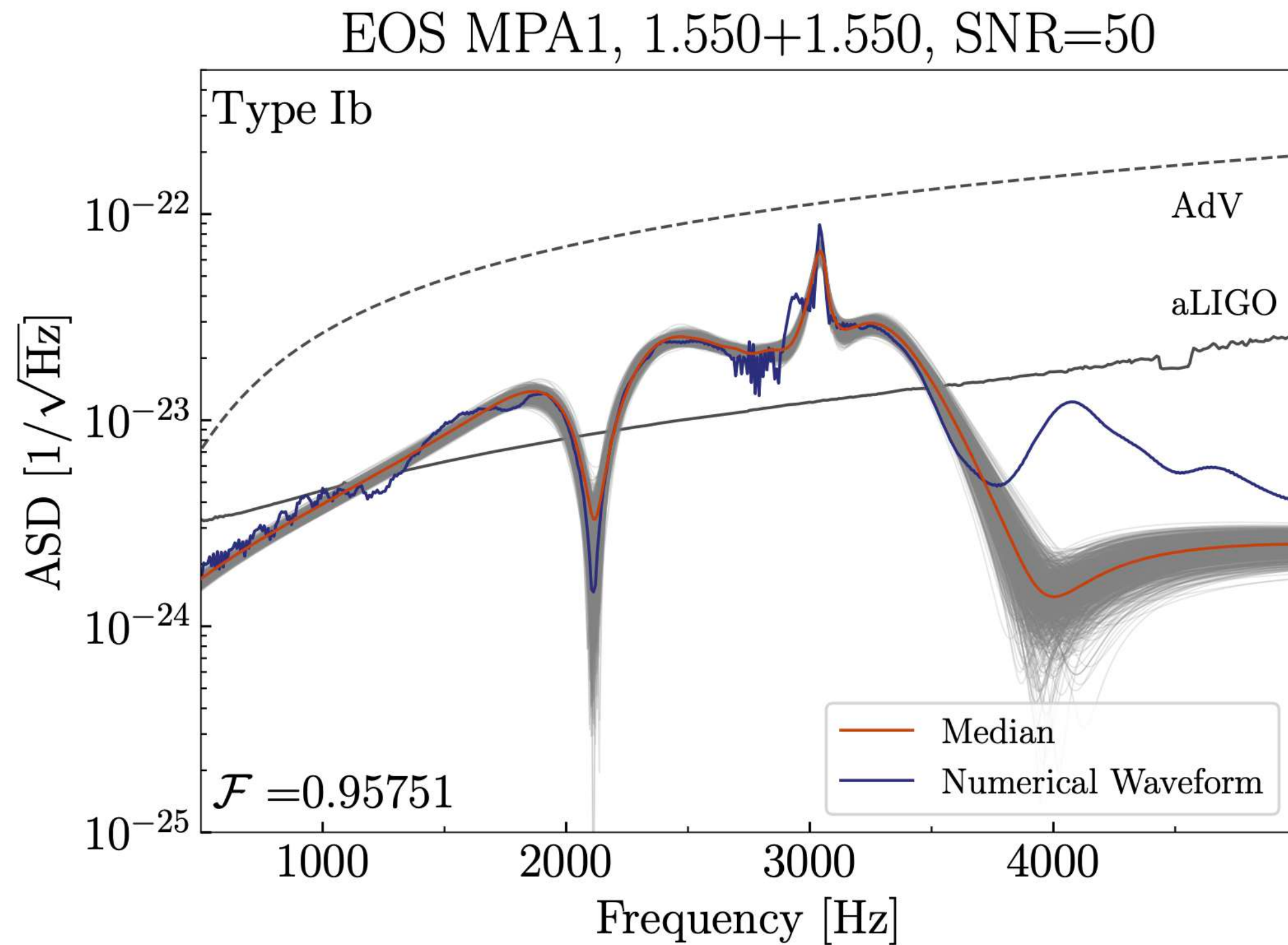
NORMALIZING FLOWS



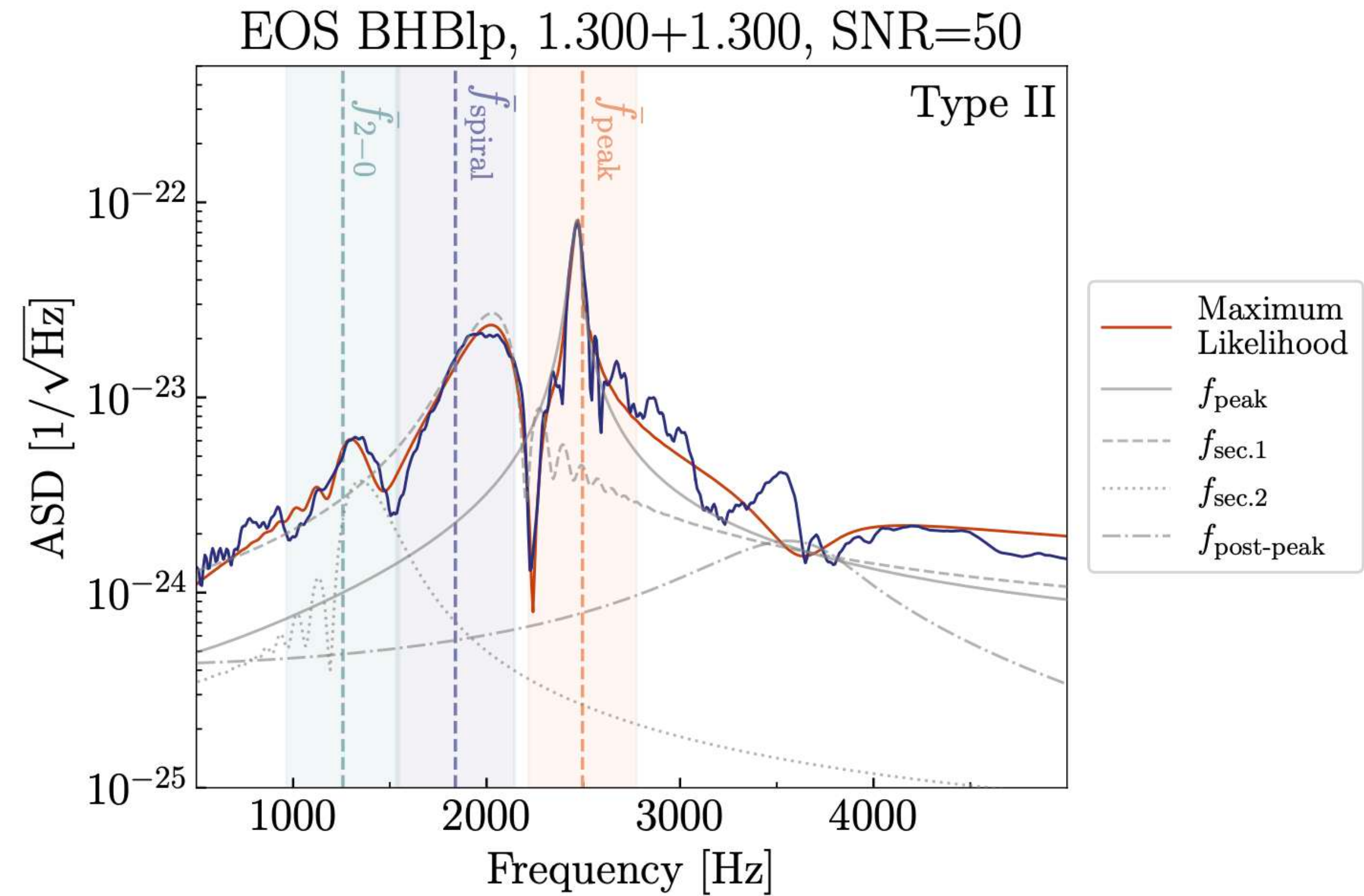
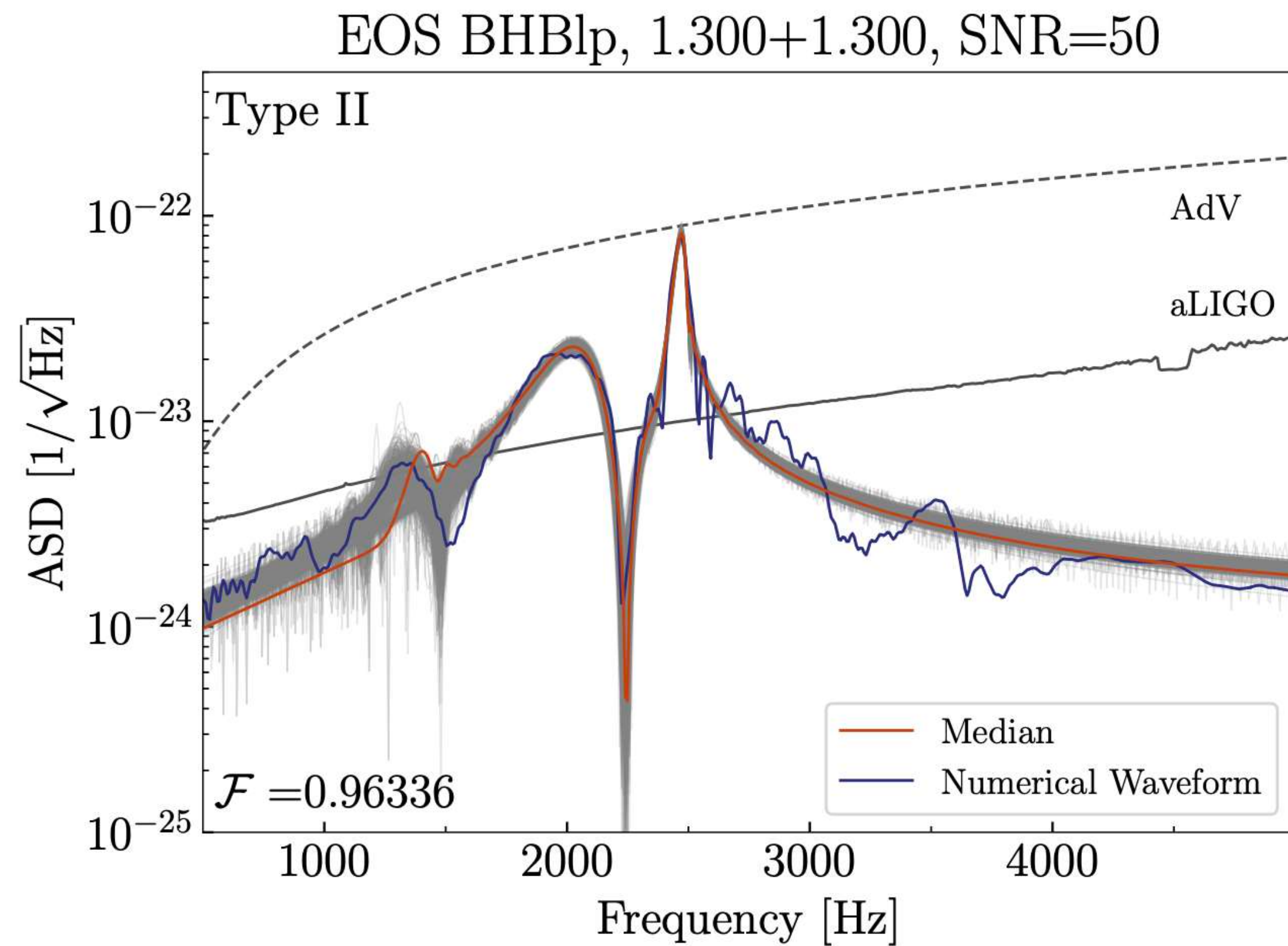
After each iteration, a **normalizing flow** transforms the distribution to a simpler one (almost Gaussian), decorrelating the parameters. This allows for a much faster sampling.

On same number of CPUs: **pocoMC** is **~10 times faster** than **dynesty** (which uses nested sampling).

RECONSTRUCTION IN THE FREQUENCY DOMAIN



RECONSTRUCTION IN THE FREQUENCY DOMAIN

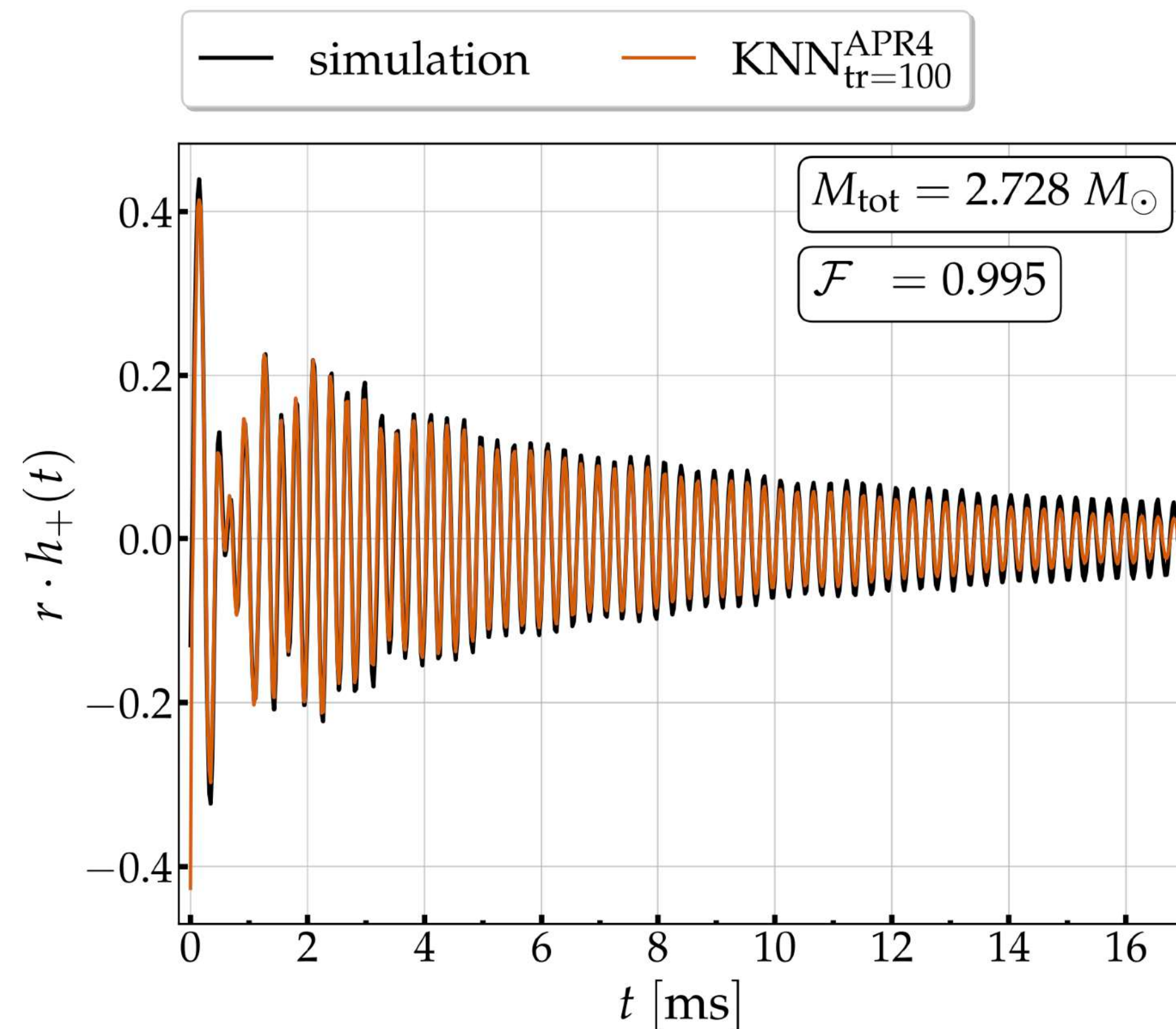


APPLICATION OF MACHINE LEARNING TO THE POST-MERGER PHASE

Problem: Only $O(200)$ substantially different numerical BNS simulations are currently available.

Solution: Construct surrogate model of post-merger GWs as function of e.g. M , q , $\text{EOS}(\Lambda)$

Time domain surrogate model using
K-Nearest Neighbor (KNN) regression:

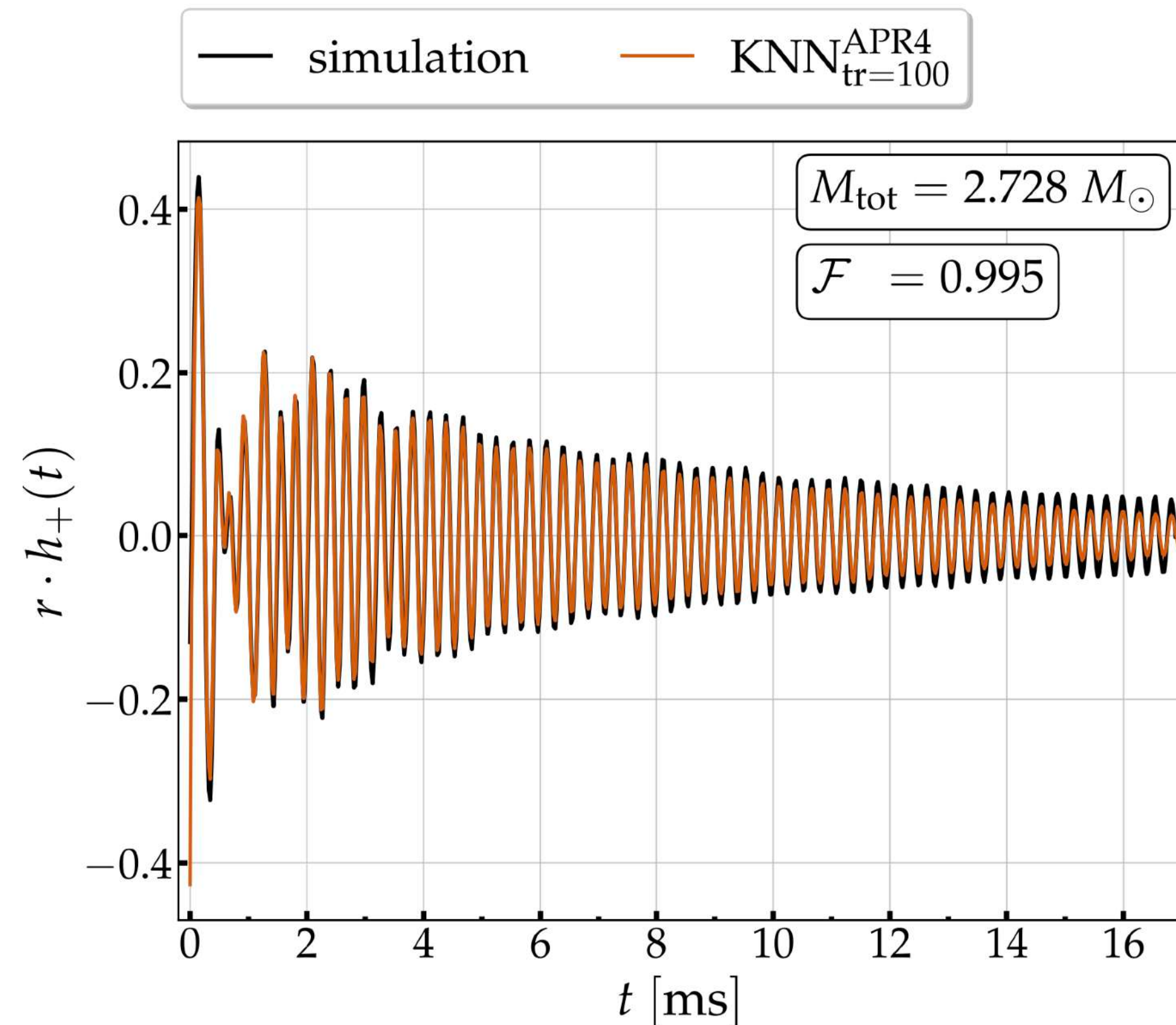


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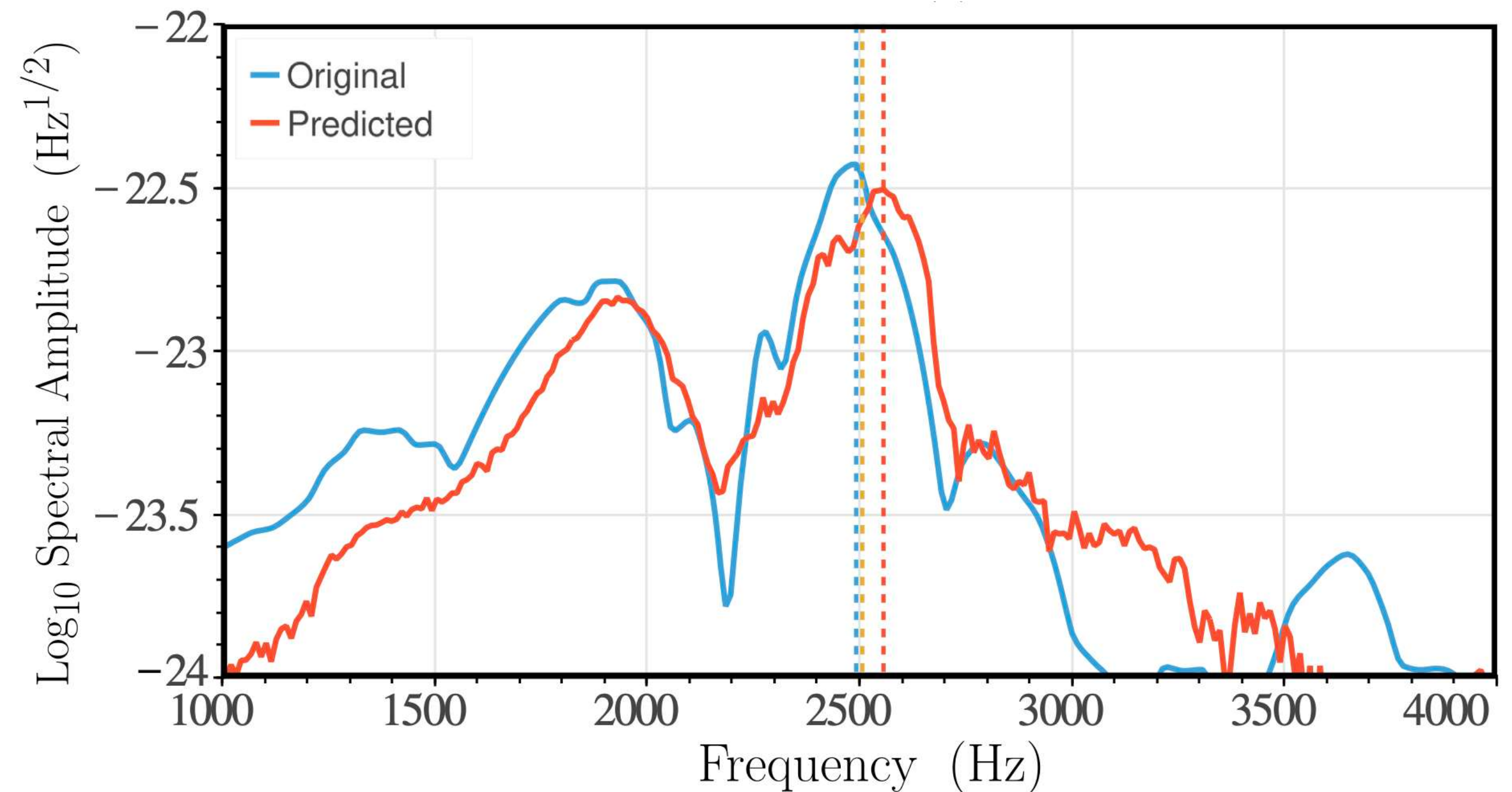
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Time domain surrogate model using
K-Nearest Neighbor (KNN) regression:



Soultanis et al. (2025)

Frequency domain surrogate model using
Artificial Neural Networks (ANN) regression:

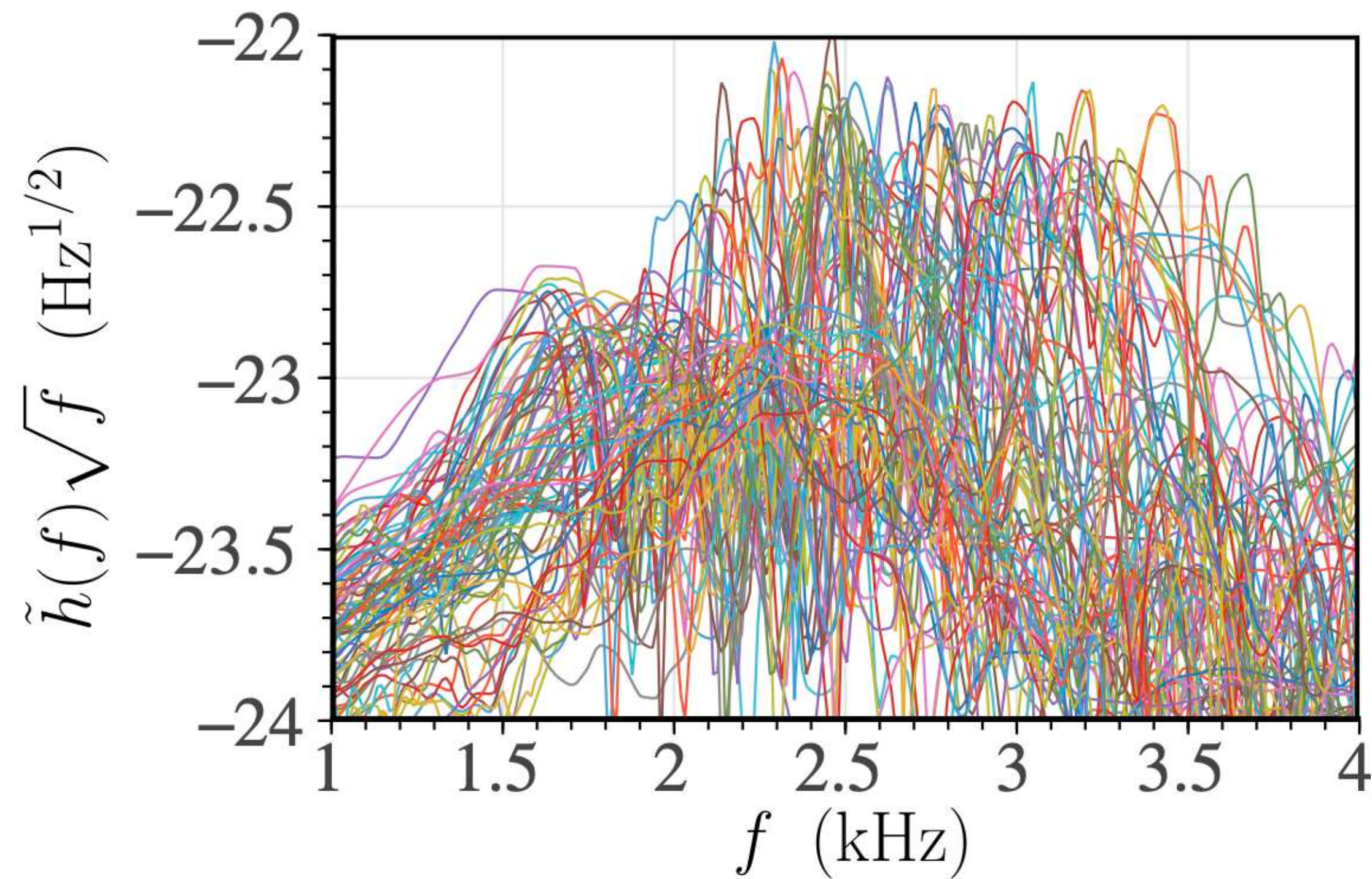


Pesios et al. (2024)

ANN REGRESSION IN THE FREQUENCY DOMAIN

Expanded training set: 87 equal-mass models using 14 different EOS

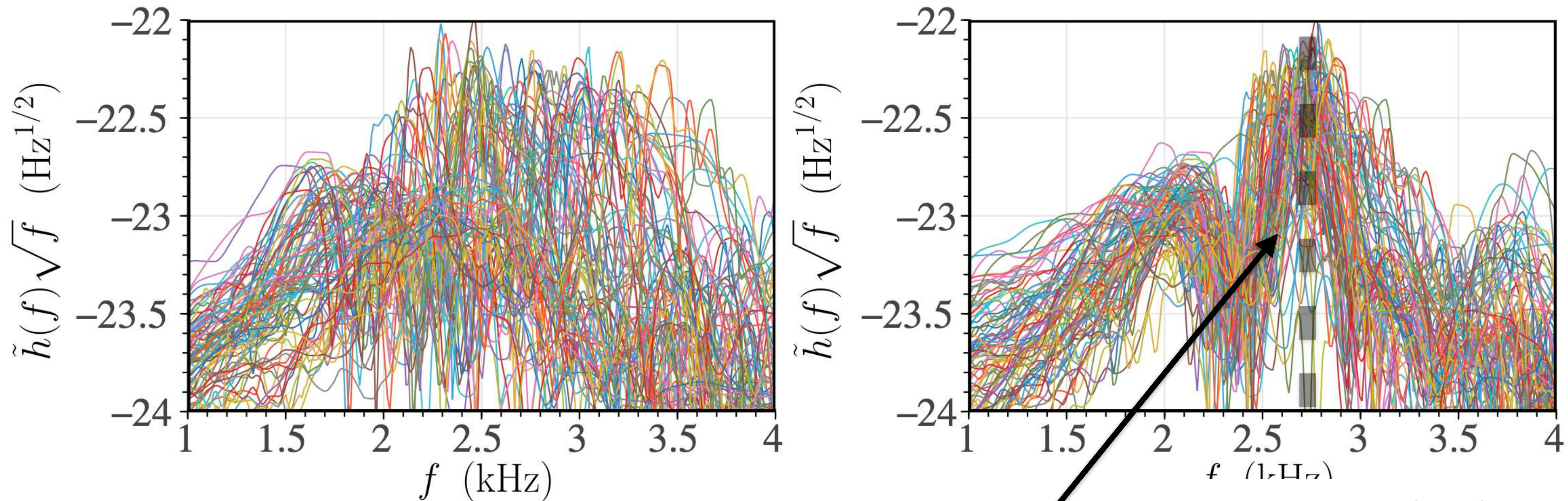
Surrogate model now depends on both mass and tidal deformability.



ANN REGRESSION IN THE FREQUENCY DOMAIN

Expanded training set: 87 equal-mass models using 14 different EOS

Surrogate model now depends on both mass and tidal deformability.



Partial alignment of spectra using empirical relation: $f_{\text{peak}}(\kappa_2^\tau, M) = 4 \frac{\beta_1}{M} \ln \left(\frac{\beta_0}{8\kappa_2^\tau} \right)$

Pesios, Koutalios, Kugiumtzis, Stergioulas (2024)

ANN SURROGATE IN THE FREQUENCY DOMAIN

Input features:

1) Mass, 2) tidal coupling constant, 3) dR/dM

Prediction:

Magnitude of GW spectrum (1-4 kHz).

ANN SURROGATE IN THE FREQUENCY DOMAIN

Input features:

1) *Mass*, 2) *tidal coupling constant*, 3) *dR/dM*

Prediction:

Magnitude of GW spectrum (1-4 kHz).

4-layer feed-forward ANN

Added Gaussian noise and dropout layers

Adam optimizer

Layer	Type	Shape	Activation	Params
1	Gaussian noise (0.1)	(None, 3)	...	0
2	Dense	(None, 200)	Linear	800
3	Gaussian noise (0.05)	(None, 200)	...	0
4	Dropout (0.15)	(None, 200)	...	0
5	Dense	(None, 400)	Sigmoid	80400
6	Gaussian noise (0.1)	(None, 400)	...	0
7	Dropout (0.15)	(None, 400)	...	0
8	Dense	(None, 400)	Sigmoid	160400
9	Gaussian noise (0.1)	(None, 400)	...	0
10	Dropout (0.05)	(None, 400)	...	0
11	Dense	(None, 370)	Linear	148370

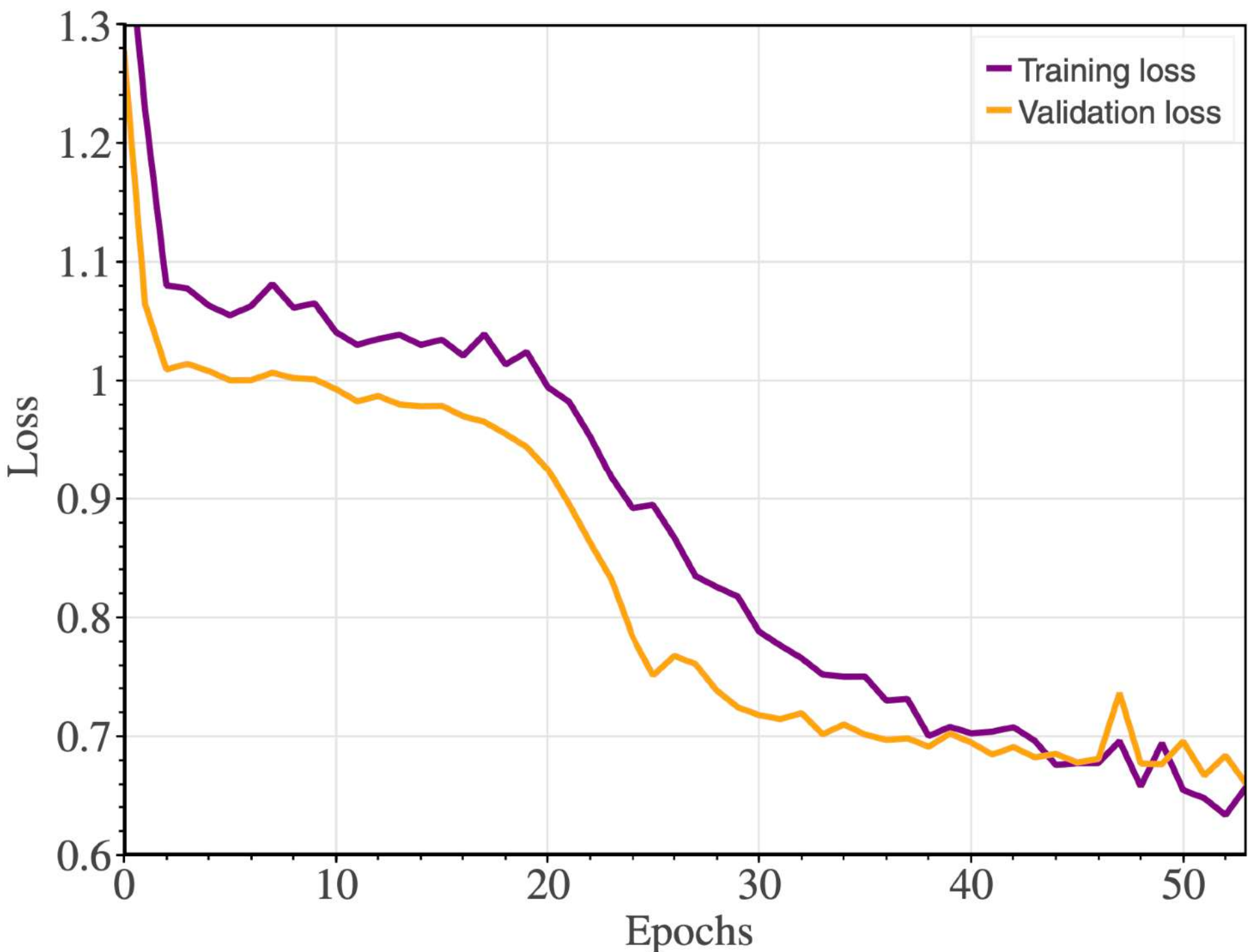
ANN SURROGATE IN THE FREQUENCY DOMAIN

Input features:

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Prediction:

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6	Gaussian noise (0.1)	(None, 400)	...	0
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9	Gaussian noise (0.1)	(None, 400)	...	0
10	Dropout (0.05)	(None, 400)	...	0
11	Dense	(None, 370)	Linear	148370

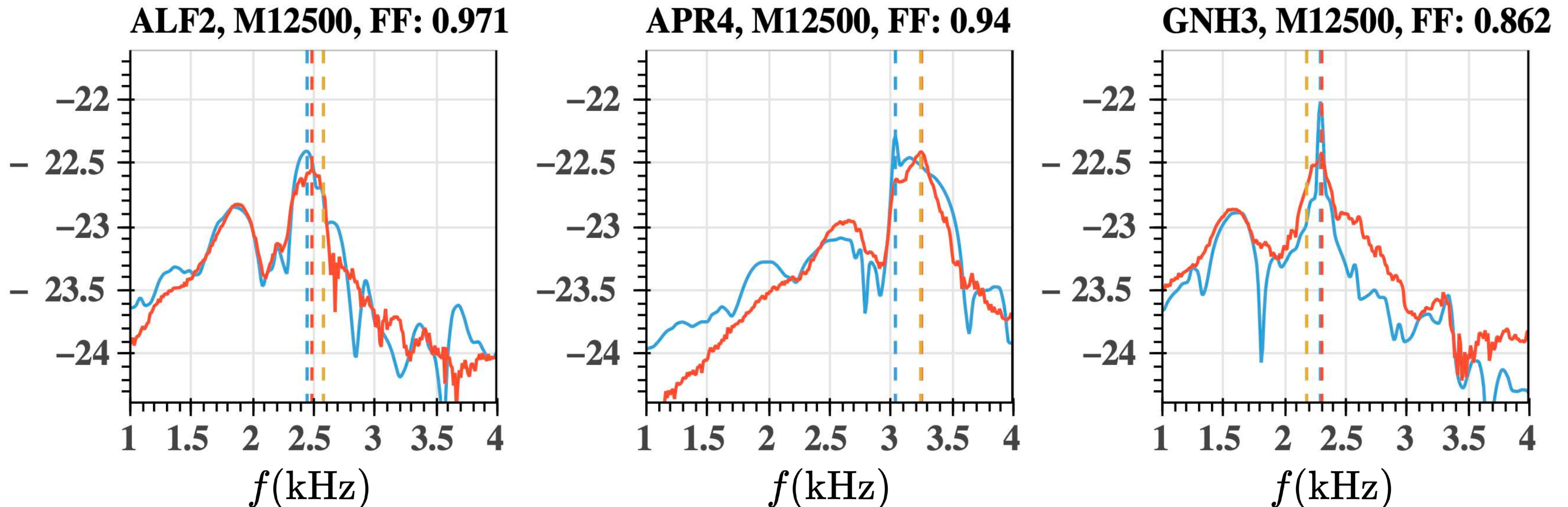
ANN SURROGATE IN THE FREQUENCY DOMAIN

Typical examples of predicted magnitudes of GW spectra

FF = 0 = overlap

Impact of uncertainty in empirical relation offset by re-calibration of spectra.

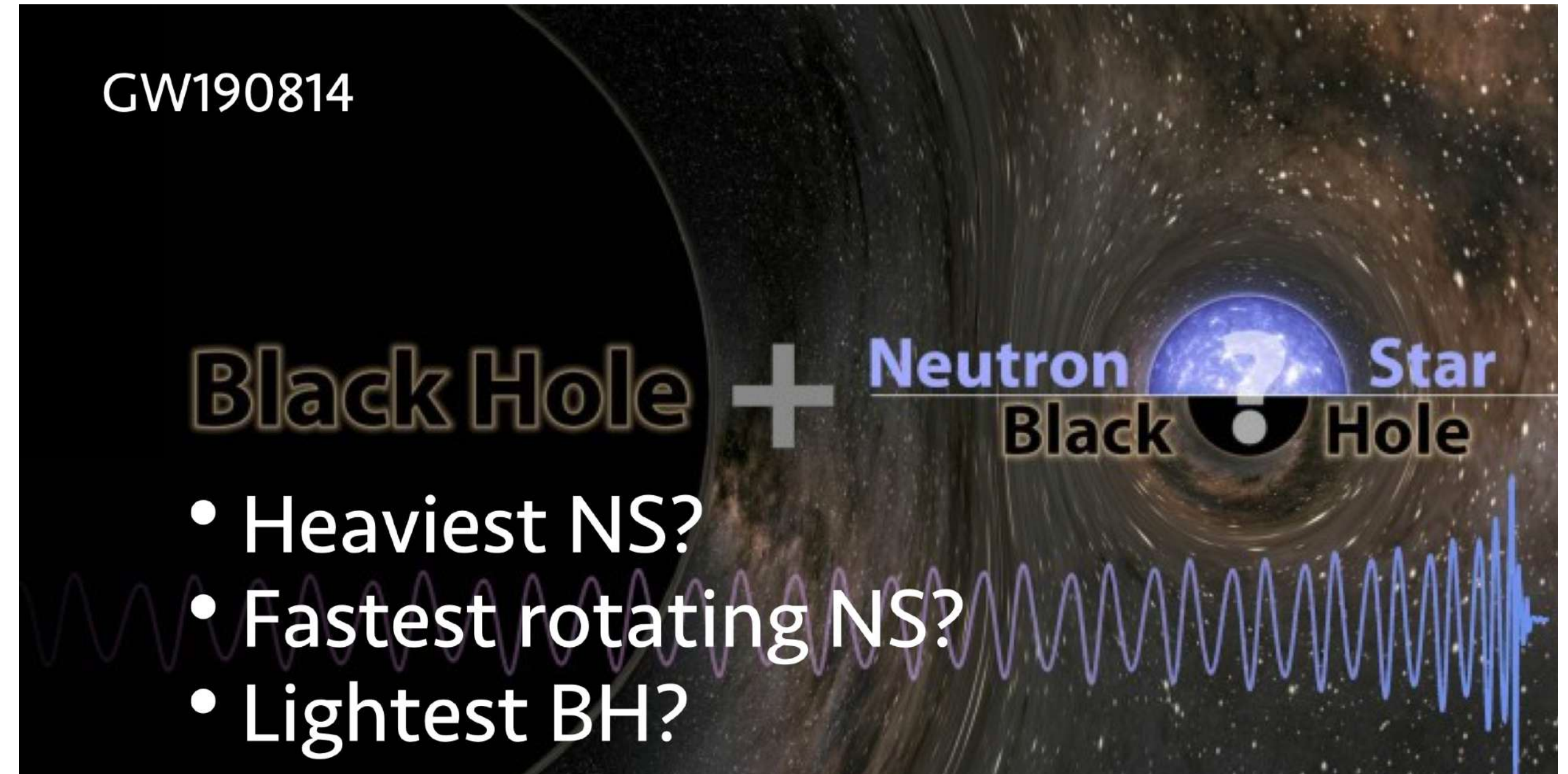
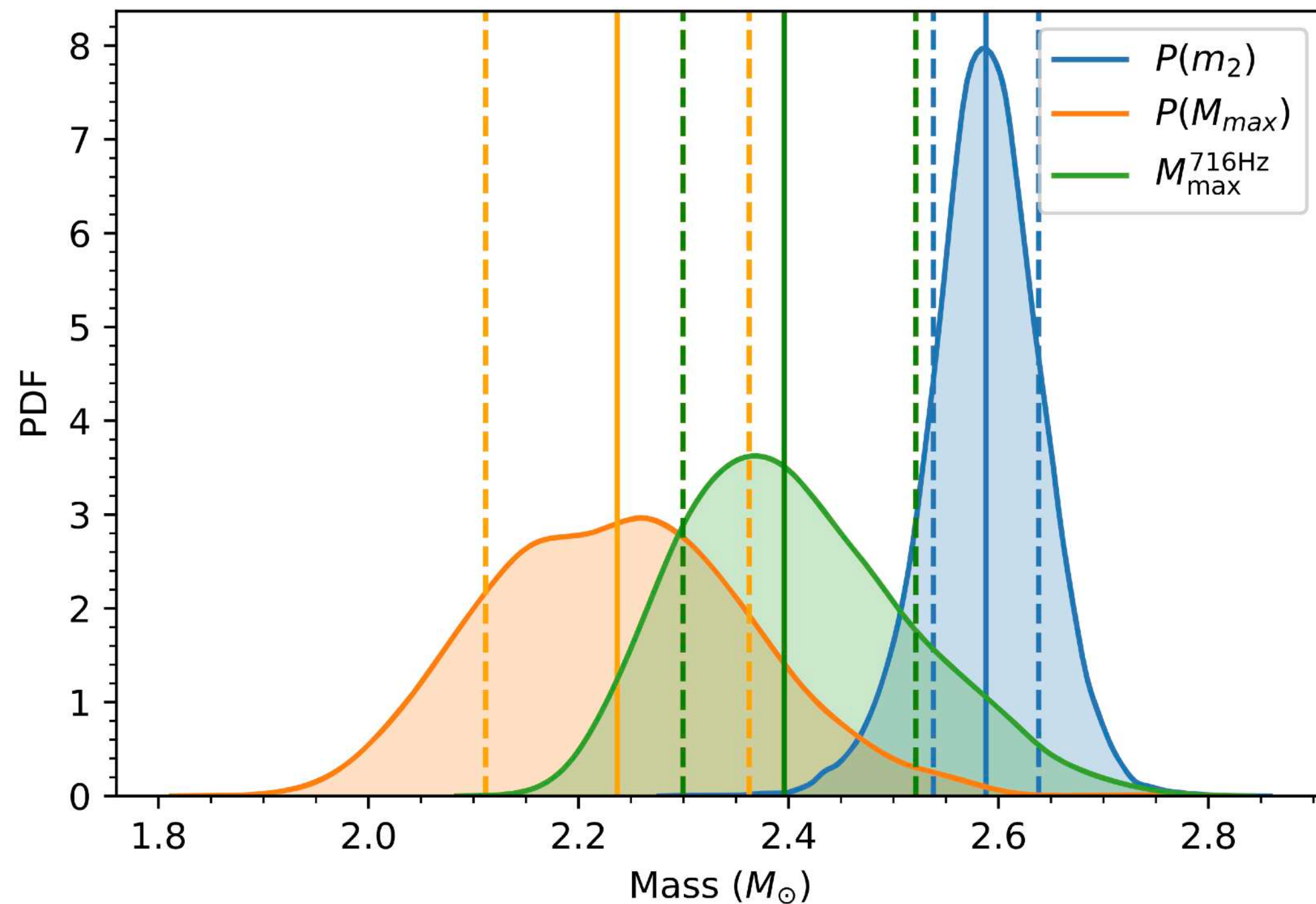
ANN outperforms multivariate linear regression.



PART C.
NEUTRON STAR MODELS IN ALTERNATIVE
THEORIES OF GRAVITY

HIGH MASS NEUTRON STARS?

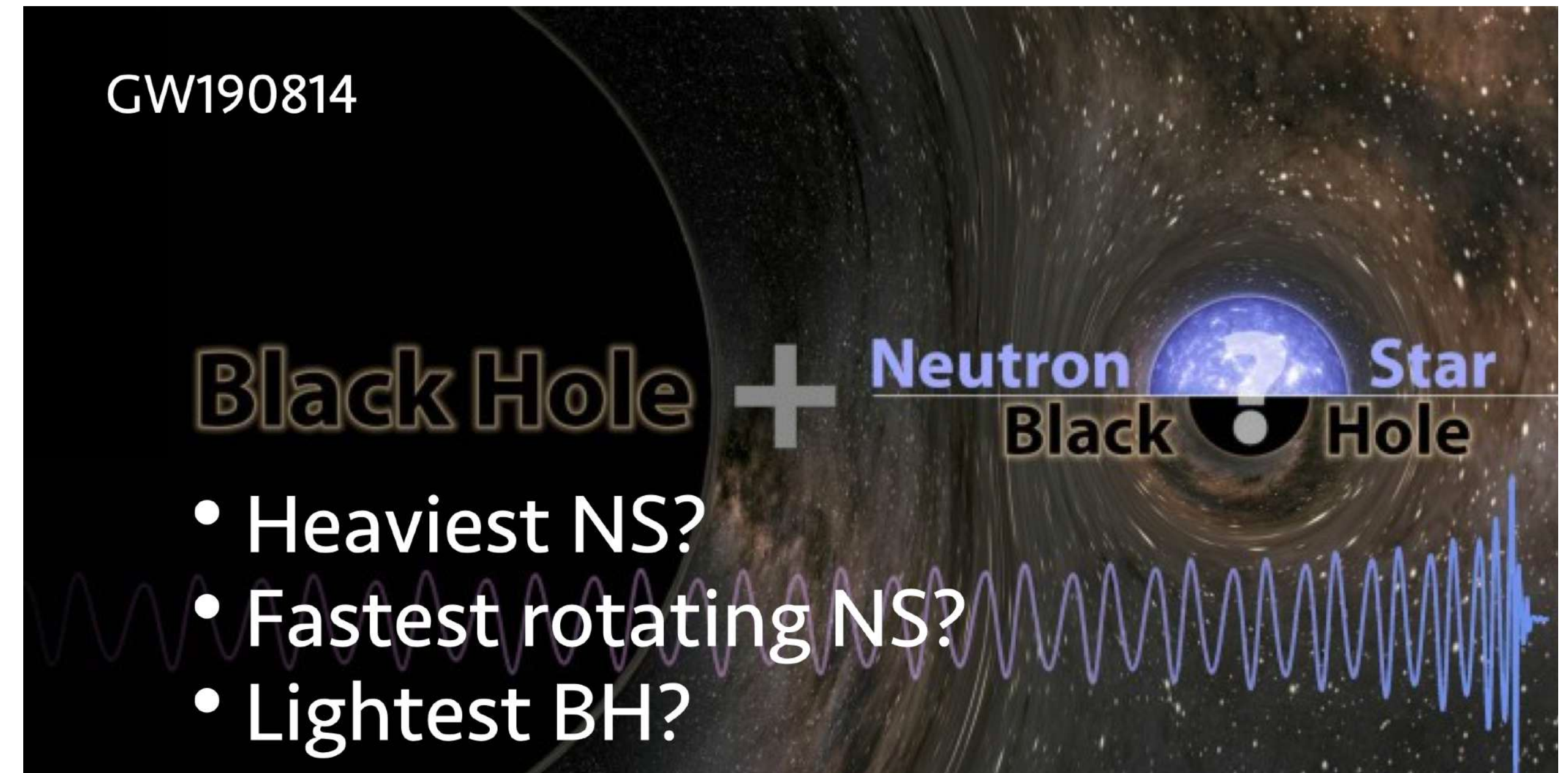
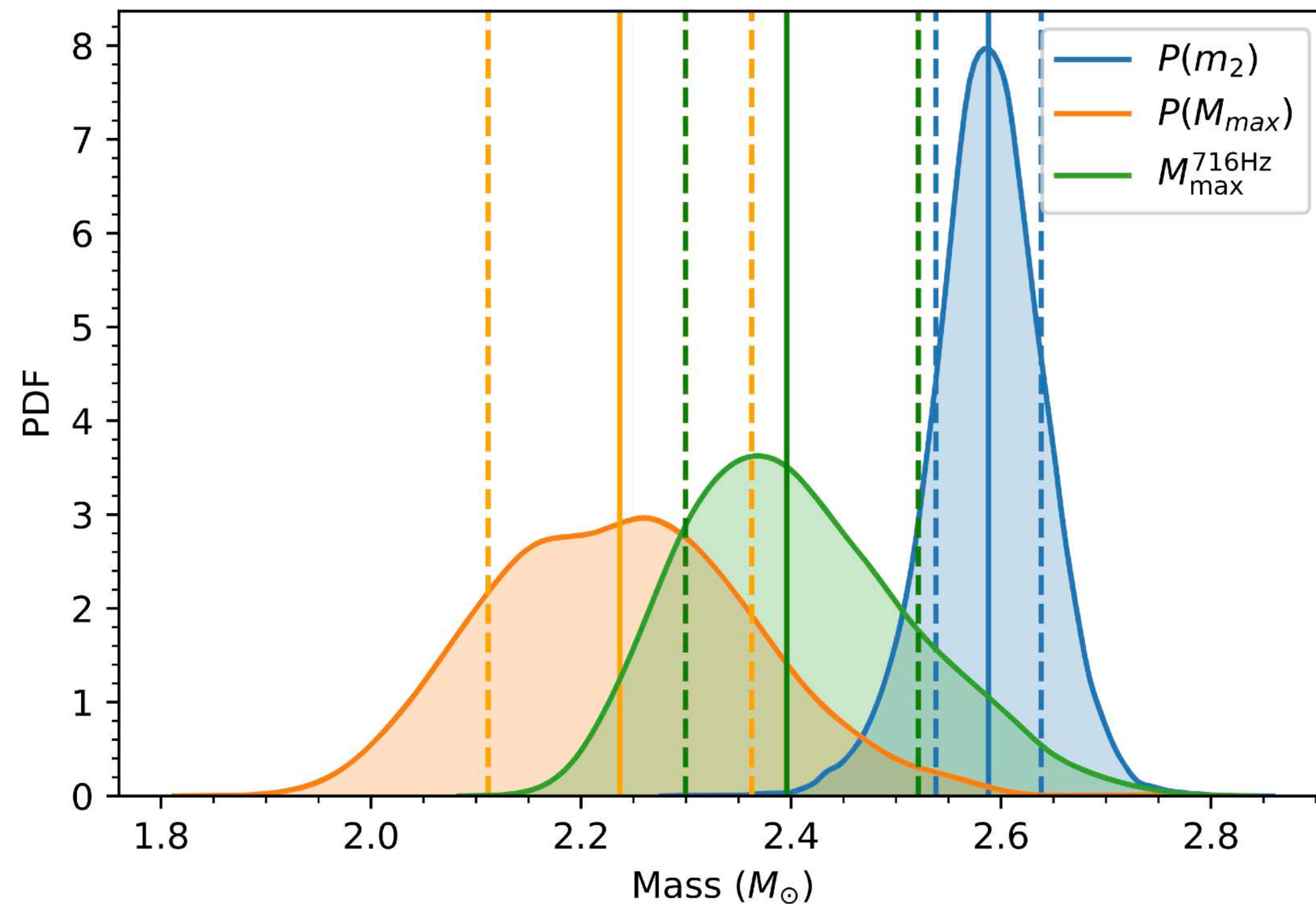
What was the nature of the lighter component in GW190814?



Biswas, Nandi, Char, Bose, Stergioulas (2021)

HIGH MASS NEUTRON STARS?

What was the nature of the lighter component in GW190814?



Biswas, Nandi, Char, Bose, Stergioulas (2021)

Another possibility: if the correct theory of gravity is not GR, then heavier NS might exist!

How can this degeneracy be resolved?

We consider the action

$$S = \frac{1}{2\kappa} \int d^4x \sqrt{-g} \{ R + \alpha [\phi \mathcal{G} + 4G_{\mu\nu} \nabla^\mu \phi \nabla^\nu \phi - 4(\nabla \phi)^2 \square \phi + 2(\nabla \phi)^4] \} + S_m$$

where $\kappa = 8\pi G/c^4$, $\mathcal{G} = R^2 - 4R_{\mu\nu}R^{\mu\nu} + R_{\mu\nu\rho\sigma}R^{\mu\nu\rho\sigma}$ is the Gauss-Bonnet scalar and S_m is the matter Lagrangian.

This theory possesses an exact vacuum solution describing nonrotating, static black holes with line element

$$ds^2 = -h(r)dt^2 + \frac{dr^2}{f(r)} + r^2 d\Omega^2$$

where

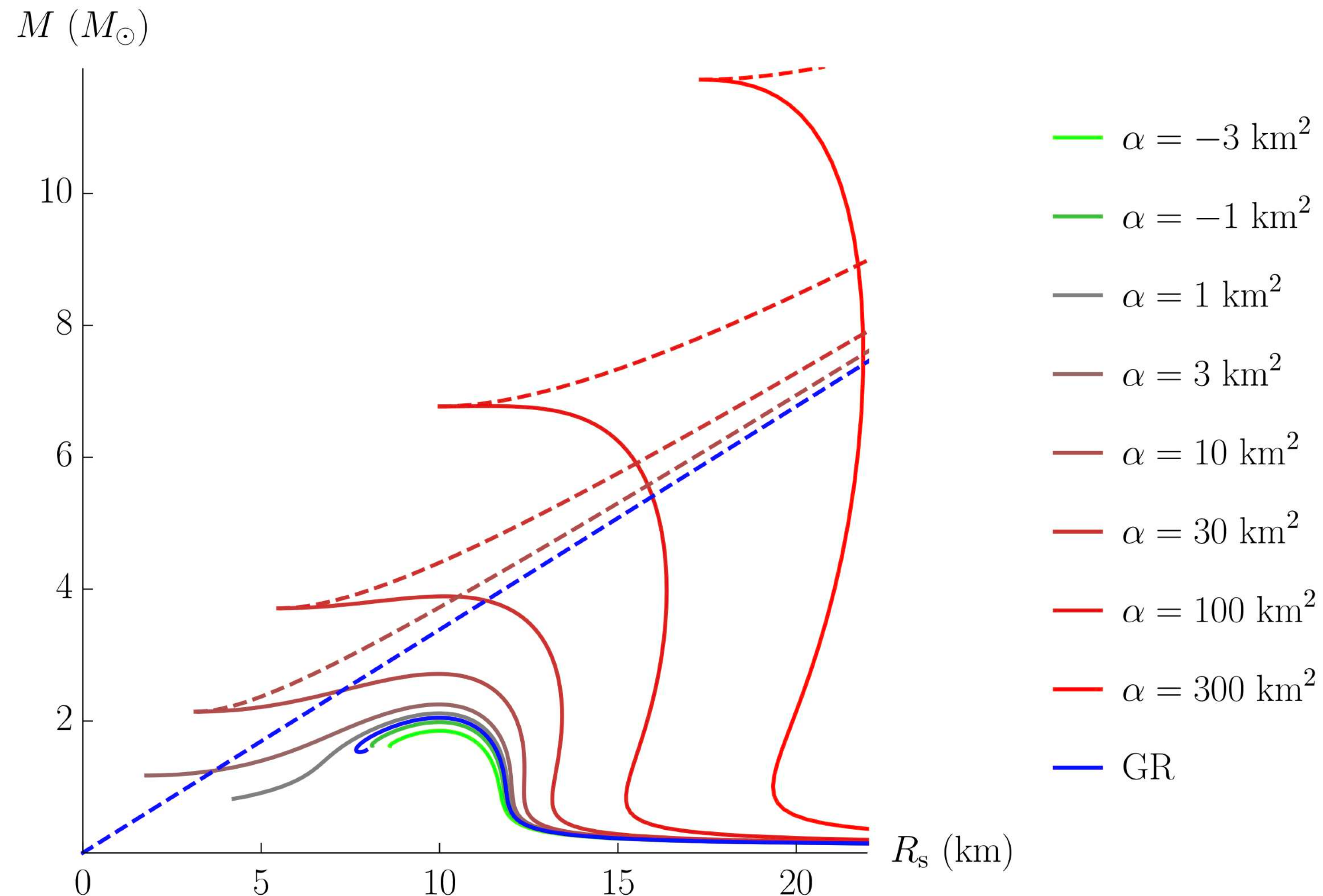
$$h(r) = f(r) = 1 + \frac{r^2}{2\alpha} \left(1 - \sqrt{1 + \frac{8\alpha M}{r^3}} \right) \quad (M \rightarrow \text{ADM mass})$$

and the shift-symmetric scalar field is

$$\phi(r) = \int dr \frac{\sqrt{f}-1}{r\sqrt{f}}$$

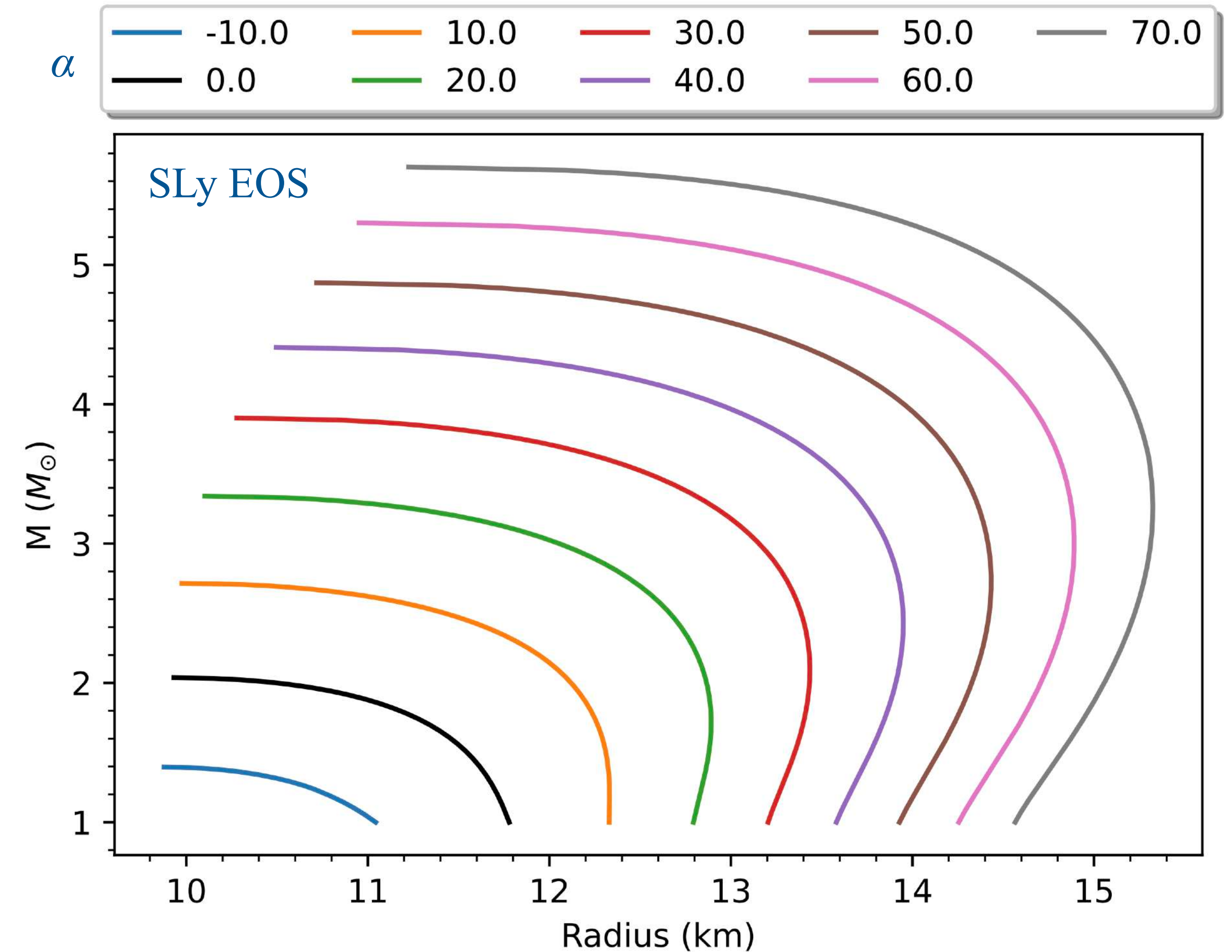
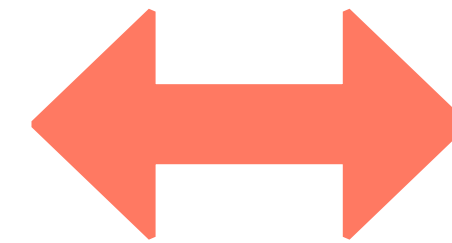
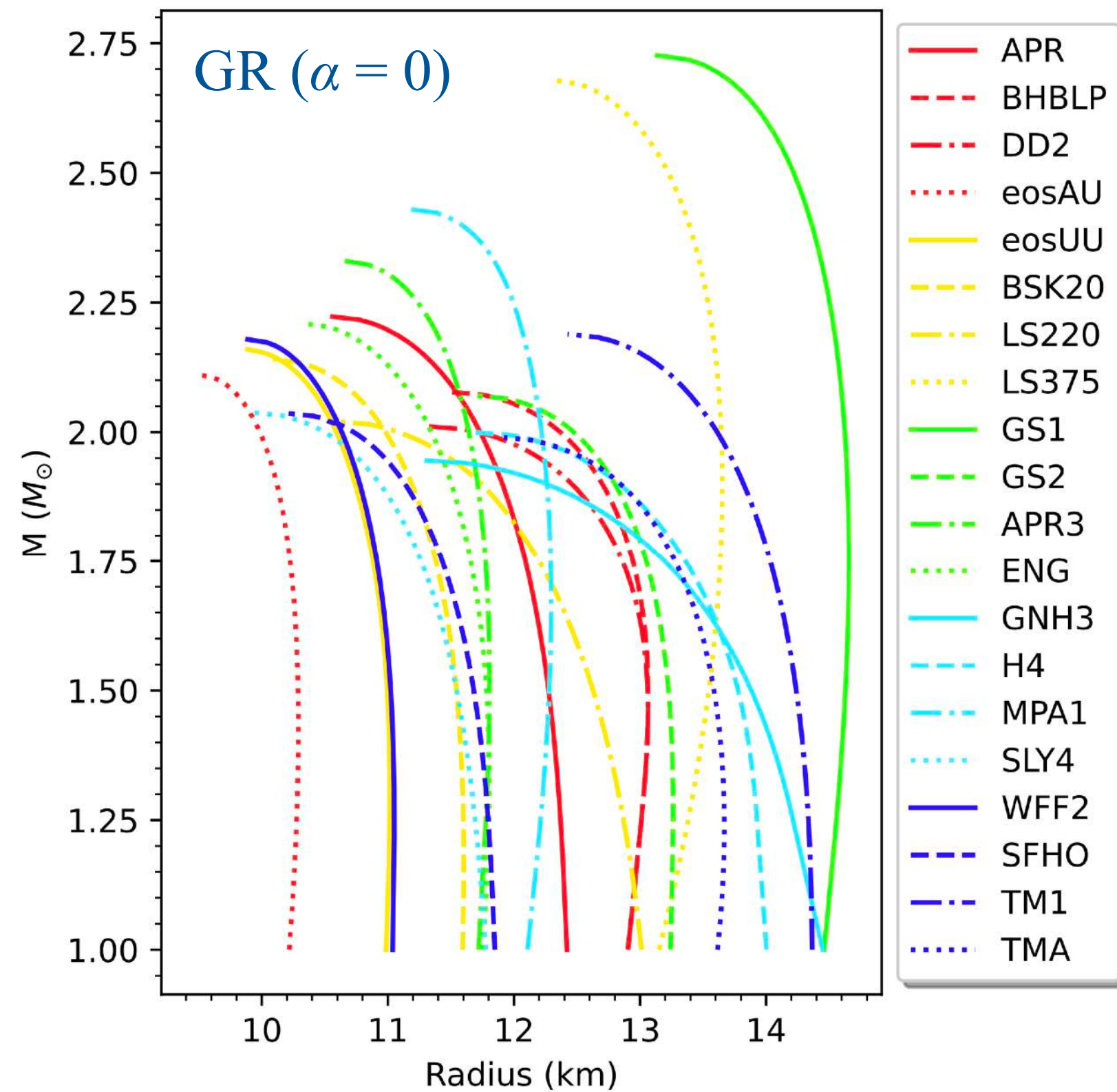
SEQUENCES OF EQUILIBRIUM MODELS

For the **SLy EOS**, we show representative cases of sequences of NS equilibrium models (solid lines) and BHs (dashed lines). For $\alpha > 0$, the NS solutions merge with the minimum mass BH solution.



EOS-GRAVITY DEGENERACY

In this theory, constructing equilibrium sequences for the same EOS, but different α , mimics the effect of using different EOS in GR.



Need to use a large number of observations to break the degeneracy!

ANN SURROGATE MODELS FOR NUMERICAL SOLUTIONS

EOS collection

Name	Number #
APR	1
BHBLP	2
DD2	3
eosAU	4
eosUU	5
BSk20	6
LS220	7
LS375	8
GS1	9
GS2	10
APR3 (PP)	11
ENG (PP)	12
GNH3 (PP)	13
H4 (PP)	14
MPA1 (PP)	15
SLy4 (PP)	16
WFF2 (PP)	17
SFHo	18
TM1	19
TMA	20

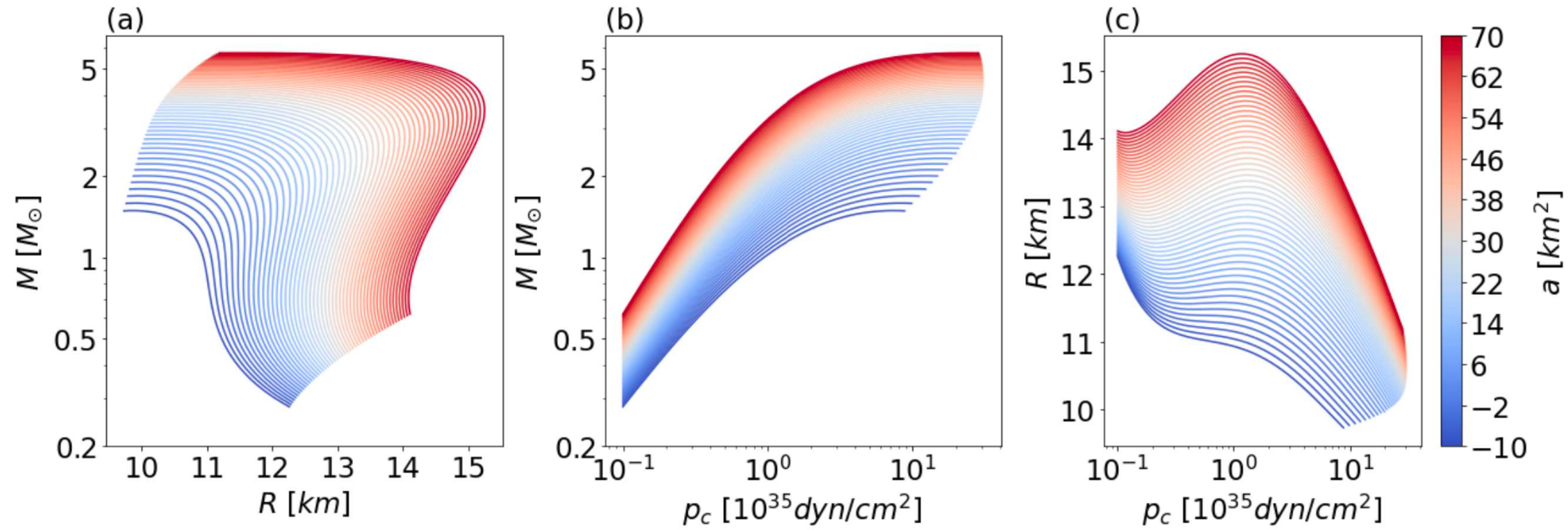
Surrogate models

$$f_1(\text{EoS}; \alpha, p_c) \rightarrow (M, R)$$
$$f_2(\text{EoS}; \alpha, M) \rightarrow R$$

Network architecture for each EOS

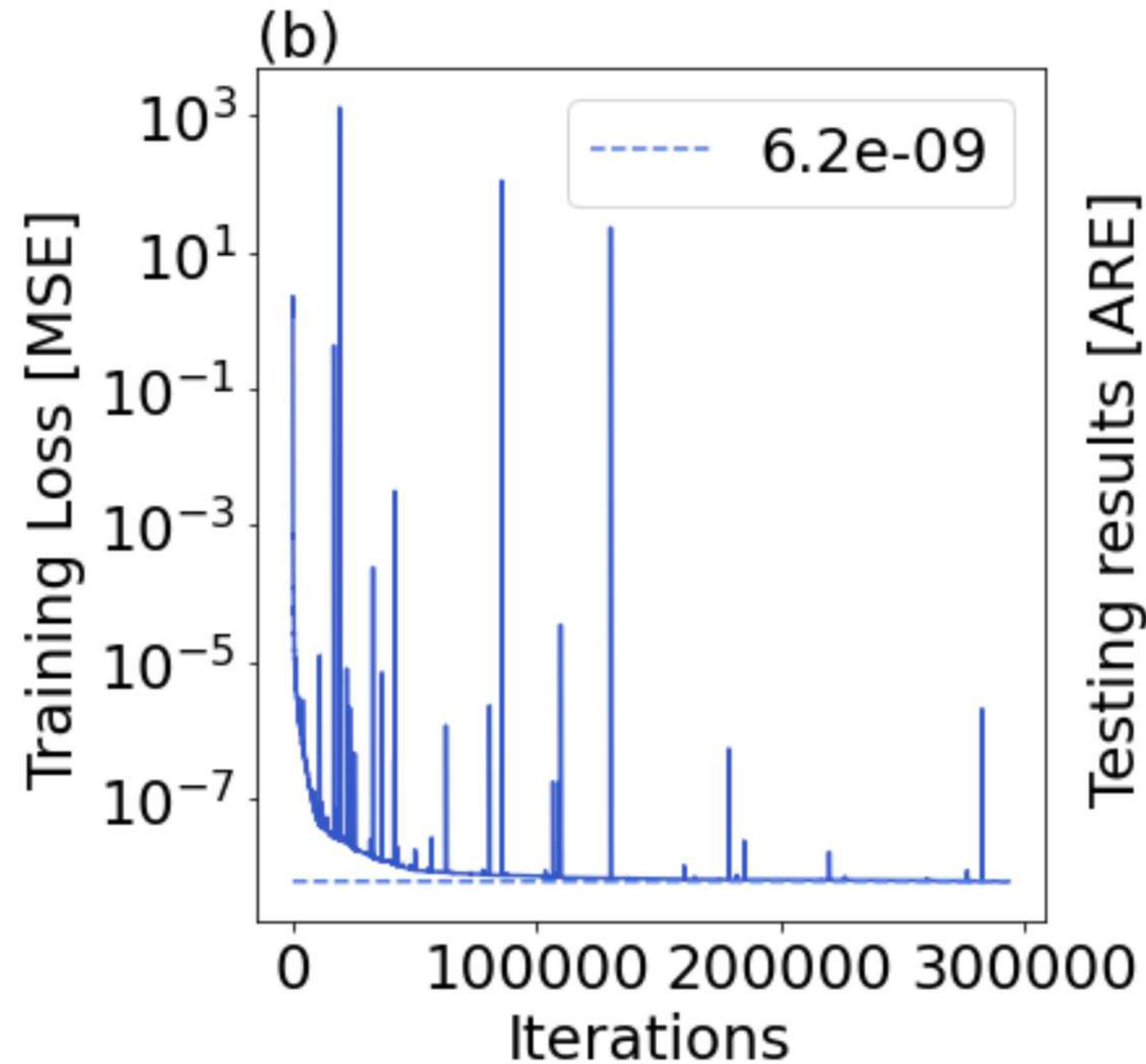
Layer	Type f_1	Type f_2
Input layer	(α, p_c)	(α, M)
Hidden layer 1	25-tanh	25-tanh
Hidden layer 2	35-relu	35-relu
Hidden layer 3	25-tanh	25-tanh
Output layer	(M, R)	R

Training set for each EOS: 200 (p_c) x 51 (α) = 10200 equilibrium models

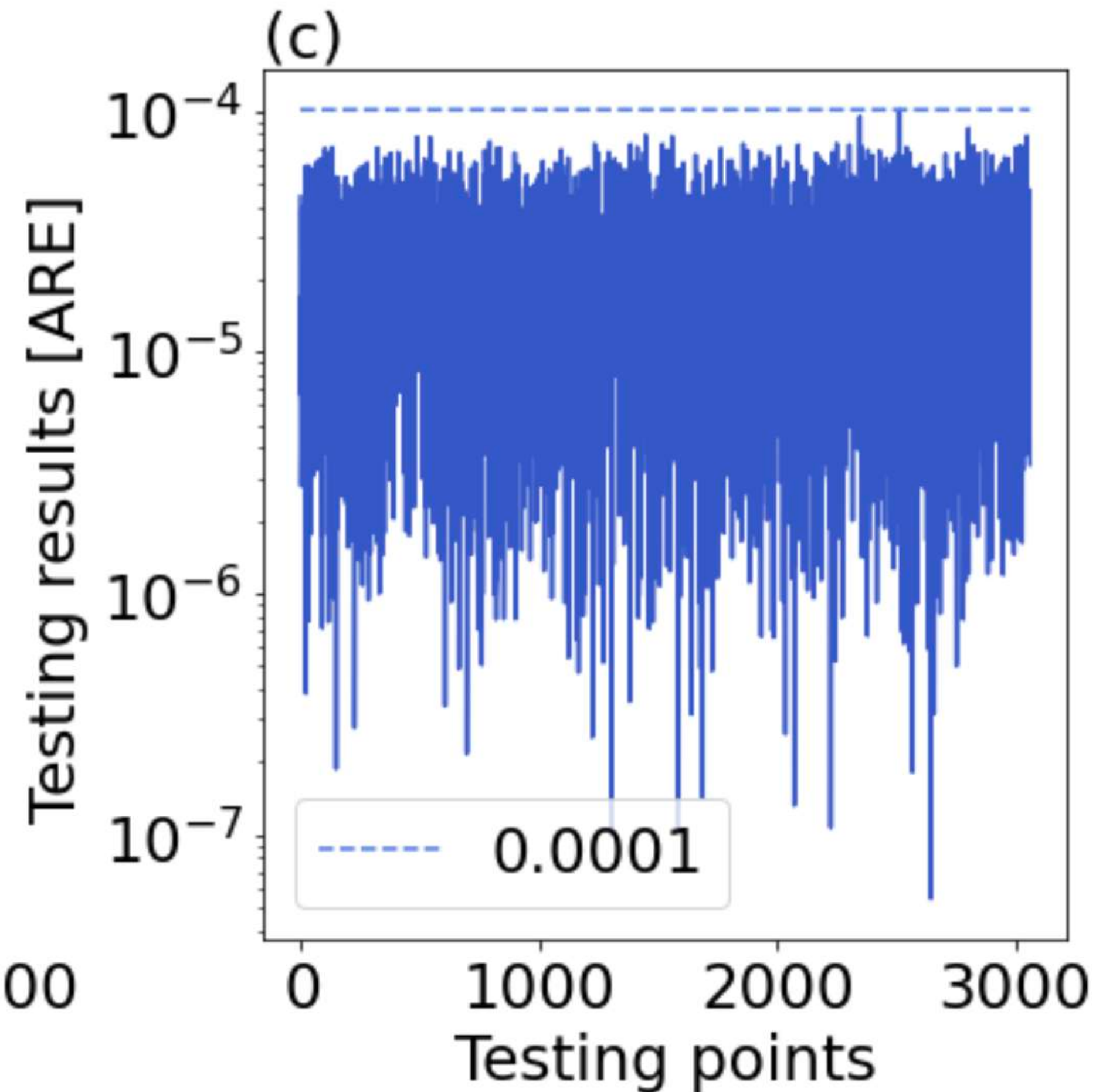


ACCURACY OF f_1 ANN SURROGATE MODEL FOR EOS BSk20

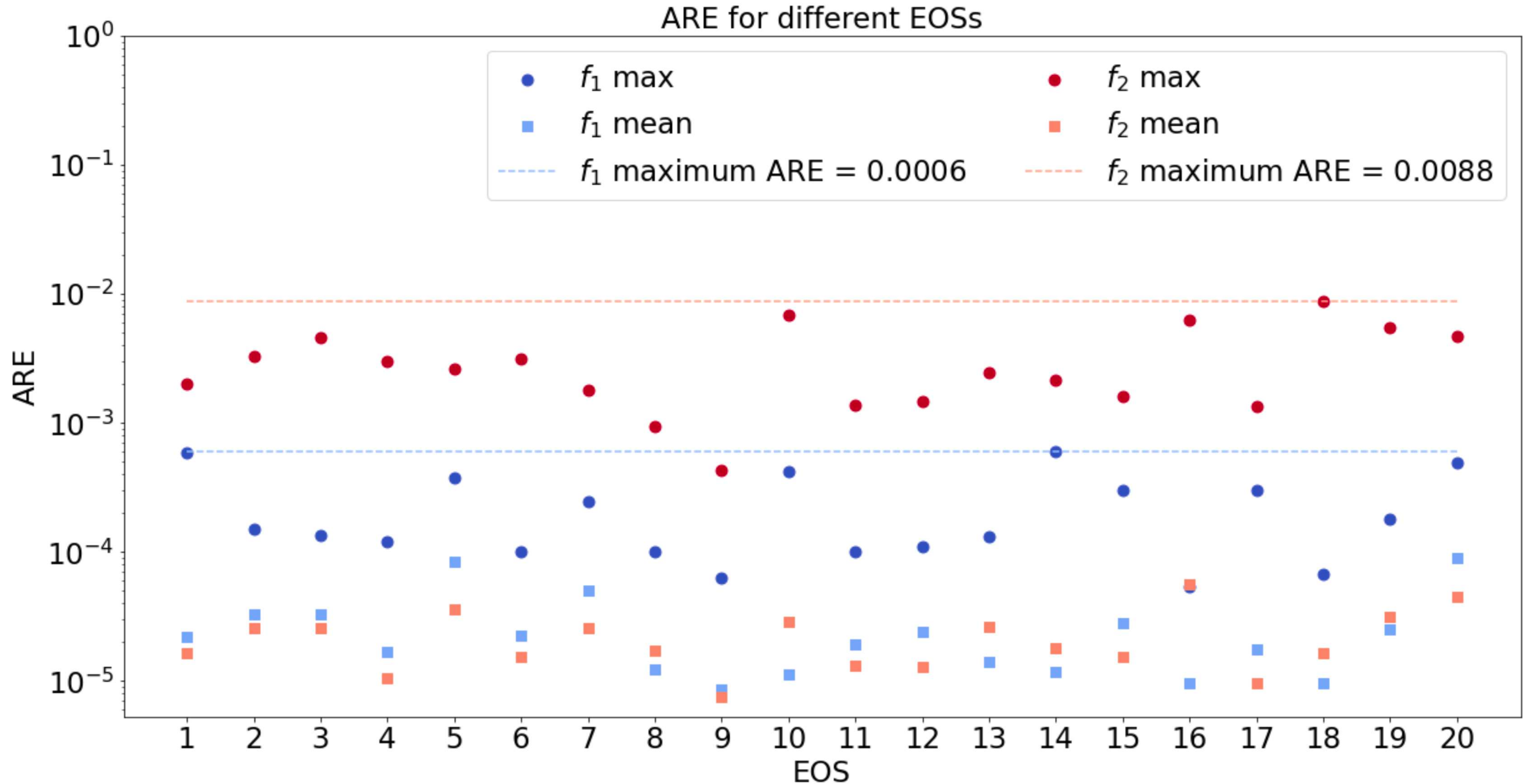
Loss function:
Mean Square Error (MSE)



Accuracy test:
Absolute Relative Error $\text{ARE}_i = \frac{1}{m} \sum_{j=1}^m \left| \frac{Y_i^j - Y_{i,\text{true}}^j}{Y_{i,\text{true}}^j} \right|$



ACCURACY OF ANN SURROGATE MODELS FOR ALL EOS



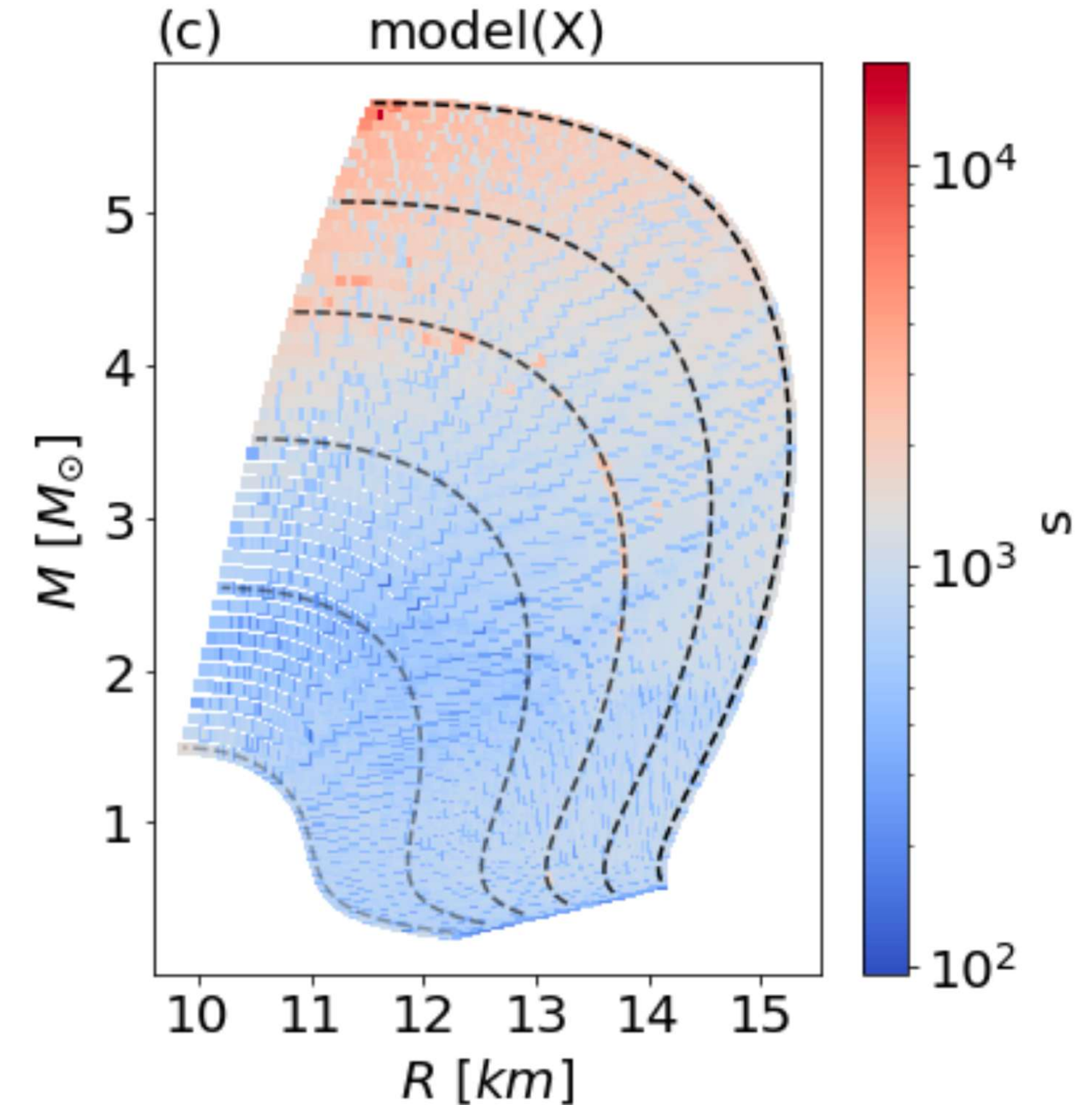
SPEED-UP ACHIEVED WITH THE ANN SURROGATE MODELS

Speed-up of ANN surrogate model compared to original numerical code

$$s = \frac{\Delta t_{\text{ANN}}}{\Delta t_{\text{num}}}$$

Numerical code	(Mean)	(Min)	(Max)
run time:	1003.5 ms	147.96 ms	18122.4 ms
Output method	Speed Up (Mean)	Speed Up (Minimum)	Speed Up (Maximum)
model.predict(X)	25.12	0.97	464.56
model(X)	921.9	95.6	18102.1
model.predict($\mathbf{X}$)	31295.5	4614.5	565157.2

The achieved speed-up allows for millions of MCMC calls in a Bayesian inference computation with minimal overhead.



THANK YOU FOR YOUR ATTENTION



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Hellenic Foundation for
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